A Forward-secure Grouping-proof Protocol for Multiple RFID Tags

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Abstract
Designing secure and robust grouping-proof protocols based on RFID characteristics becomes a hotspot in the research of security in Internet of Things (IoT). The proposed grouping-proof protocols recently have security and/or privacy omission and these schemes afford order-dependence by relaying message among tags through an RFID reader. In consequence, aiming at enhancing the robustness, improving scalability, reducing the computation costs on resource-constrained devices, and meanwhile combing Computational Intelligence (CI) with Secure Multi-party Communication (SMC), a Forward-Secure Grouping-Proof Protocol (FSGP) for multiple RFID tags based on Shamir’s \((n, n)\) secret sharing is proposed. In comparison with the previous grouping-proof protocols, FSGP has the characteristics of forward-security and order-independence addressing the scalability issue by avoiding relaying message. Our protocol provides security enhancement, performance improvement, and meanwhile controls the computation cost, which equilibrates both security and low cost requirements for RFID tags.

Keywords: RFID; Grouping-proof; Forward-secure; Order-independent; Secret Sharing

1. Introduction
With the wide spread of RFID tags and its cheap implementations, the need for providing secure and privacy-preserving authentication protocols in extremely resource-constrained environments is evident. Ari Juels first introduced yoking-proof\(^1\), which involves generating evidence of the simultaneous presence of two tags in the range of an RFID reader. The proof can then be verified by a verifier which holds all the secret keys of tags. Then he extended this notion and envisioned the concept of grouping-proofs\(^2,4\), which allows multiple RFID tags to provide evidence that they are scanned simultaneously in an identification session by one or more readers within its broadcast range. Other improved variants of yoking-proof were also proposed in\(^3,6,7\). As Juels\(^1\) already pointed out, there are several practical scenarios where grouping-proofs could significantly expand the capabilities of RFID-based systems, such as manufacturing, supply chains, access control, e-ticketing and counterfeit prevention, etc. Motivated by the potential applications, several grouping-proofs for RFID tags are developed in recent years\(^2,8\).

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RFID tags are severely constrained in terms of storage resources, computational capabilities and power supply, and therefore the protocols that involve high computational and storage burdens are not attractive. Computational intelligence (CI) has been successfully used in recent years to address various challenges such as data aggregation, security, optimal deployment and localization, which brings about broad applicability, flexibility, self-optimization capability and robustness against malicious attacks in dynamic environments. CI is an area of fundamental and applied research involving numerical information processing in contrast to the symbolic information processing techniques of artificial intelligence (AI), which is defined as the computational models and tools of intelligence capable of inputting raw numerical sensory data directly, processing them by exploiting the representational parallelism and pipelining the problems, generating reliable and timely responses and withstandng high fault tolerance. CI studies adaptive mechanisms that enable or facilitate intelligent behavior in complex and changing environments, which encompasses neural networks, genetic algorithms, reinforcement learning, swarm intelligence, evolutionary algorithms, fuzzy logic and artificial immune systems, etc.

Different from the common techniques of CI that is addressed above, we focus on the applications of CI into this rapidly growing area of grouping-proof protocols for RFID tags by combing CI with Secure Multi-party Communication (SMC). In this paper we first evaluate these proposed grouping-proofs recently to observe security demand and analyze security weaknesses. Then we propose a lightweight forward-secure grouping-proof protocol based on Shamir’s \((n, n)\) secret sharing to improve scalability, robustness, especially order-independence by avoiding relaying message. In comparison with the previous grouping-proofs, our contributions can be summarized as follows:

(i) Guarantees session unlinkability with forward security by auto-update mechanism for secret and state information within a tag.
(ii) Ensures the protocol order-independent by avoiding relaying message through RFID reader using Shamir’s \((n, n)\) secret sharing.
(iii) Addresses the scalability issue which makes a single authentication protocol in combination with a grouping-proof protocol properly by controlling round-trip time of a challenge-response cycle and applying the technique of CI properly.
(iv) Enhances the robustness, which makes the protocol thwart man-in-the-middle attack, replay attack, counterfeit attack in a formal security framework and meanwhile possess tag anonymity and untraceability.
(v) Meets the requirement of lightweight on resource-constrained devices by only using MAC and PRNG operation on RFID tags.

The remainder of this paper is organized as follows. We present a critical review of the related work in Section 2. In Section 3 we then review some preliminaries briefly. Next our forward-secure grouping-proof protocol (FSGP) is described in Section 4. The Section 5 addresses the presentation of security and performance analysis. Finally, Section 6 concludes this paper.

2. Related Works: RFID Grouping-Proofs

2.1. Review of existing protocols

The idea of grouping proofs originated from Juels in 2004. His proposal for this type of identification protocol, so-called yoking proof, relies on interleaving MACs of two tags using a reader as a communication medium and utilizing a timeout mechanism to guarantee the validity of yoking proof generated at each session.

(1) Yoking-proof attack and improvements

Nevertheless, Saito & Sakurai were the first to point out the weaknesses in the work of Juels. They indicated that yoking-proof is not immune to replay attacks. Yoking-proof has been extended to prove simultaneous presence of a group of tags in the range of an RFID reader in Saito & Sakurai. Burmester et al. pointed out two additional weaknesses in Saito & Sakurai: Denial-of-Service (DOS) and impersonation attacks. In addition, in 2006 Piramuthu showed Saito’s protocol with timestamps is also vulnerable to replay attack. Accordingly, he proposed another variant of yoking-proof which does not use timestamp to prevent replay attack. But Piramuthu did not resolve security threats such as privacy disclosure, forward secrecy divulgence, authentication sequence disorder and DOP attack.

(2) Anonymous grouping-proof schemes

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The idea of anonymous grouping-proofs was first introduced by Bolotnyy and Robins in 2006, which accommodated a group of RFID tags by extending Juels’ yoking proof, so-called Generalized Yoking-proofs. Unfortunately, this proposed Anonymous Yoking scheme suffers from forward secrecy disclosure and tag privacy divulgence. In 2007 Peris-Lopez et al. discovered Piramuthu’s protocol is vulnerable to malicious tracking. In 2008 Burmester et al. pointed out weaknesses in Bolotnyy’s scheme and presented a security model based on the Universal Composability framework. In 2009 Chien and Liu proposed an anonymous tree based yoking protocols. However, this protocol is vulnerable to malicious tracking.

3. Preliminary

3.1. RFID Deployments and Assumption

A typical deployment of an RFID system involves three types of legitimate entities: Tags, Readers and a Verifier (or a Backend Server). Throughout this paper, we assume the following characteristic of grouping-proof:

(1) The tags are passive and have very limited computation and communication capabilities. It is common assumed that they are able to perform basic cryptographic operations such as generating pseudo-random numbers and evaluating pseudo-random functions. The tags do not maintain clocks while the verifier controls a challenge-response cycle.

(2) The readers establish communication channels that link the tags to manage the interrogation of tags and keep a record of proofs for each session which cannot be manipulated by the adversary.

(3) The verifier is the only trusted entity that may share some secret information with the tags such as cryptographic keys. The verifier has a secure channel that links to the readers. In contrast, the channels between tags and the reader are considered insecure.

(4) A qualified RFID grouping-proof protocol should comply with several essential security and privacy requirements, such as data confidentiality, tag anonymity, forward security, defending against malicious attacks and untraceability.

(5) RFID grouping-proof protocols are mainly concerned with security issues at the protocol layer and not with physical or link layer issues.

3.2. Shamir’s $(t, n)$-SS

Secret sharing schemes were originally introduced by Blakley and Shamir independently as a solution for safeguarding secret keys. Shamir’s $(t, n)$ secret sharing is denoted as $(t, n)$-SS. In particular, $(t, n)$-SS is called $(n, n)$-SS when $t = n$. $(t, n)$-SS is based on Lagrange interpolating polynomial and is in formation-theoretically secure without any computational assumption. $(t, n)$-SS consists of two algorithms:

1. **Share generation algorithm**: The mutually trusted dealer $D$ first selects a random polynomial $f(x)$ of
degree \( t-1 \): \( f(x) = a_0 + a_1x + \ldots + a_{t-1}x^{t-1} \), such that \( s = a_0 \) and all coefficients \( a_0, a_1, \ldots, a_{t-1} \) are in a finite field \( F_p = GF(p) \) with \( p \) elements. \( D \) computes \( n \) shares \((s_1, s_2, \ldots, s_n)\) as \( s_1 = f(1), s_2 = f(2), \ldots, s_n = f(n) \). \( D \) distributes each share \( s_i \) to corresponding shareholder \( P_i \), secretly.

(2) Secret reconstruction algorithm: For any \( t \) share \((s_1, s_2, \ldots, s_n)\) where \((i_1, i_2, \ldots, i_t) \subseteq \{1,2,\ldots,n\}\), the secrets can be reconstructed using Lagrange interpolating formula.

4. Our Protocol FSGP

To enhance the robustness, reduce the computation costs and avoid order-dependent, we propose a forward-secure grouping-proof protocol for multiple RFID tags based on Shamir’s \((n, n)\)-SS, which is the new application of combining CI with SMC to construct grouping-proof protocol. FSGP addresses the scalability issue properly by avoiding relaying message among tags through RFID reader and realizes the direct challenge-response among readers and tags. Moreover the protocol guarantees session unlinkability by adding forward security. Our protocol FSGP sets a single authentication proof being a typical example of a forward-secure sub-grouping-proof protocol in one session cycle. The procedure is described as follows:

1. Initial Setup Phase

TDS selects a PRNG \( g: \{0,1\}^k \rightarrow \{0,1\}^{2k} \) based on \( k \) and sets \( ID \), as the initial seed of \( g \). All tags in Grouping-Proof have the ability of computing \( g \) and meanwhile TDS initializes the current state \( s_{t0} = g(ID) \) of \( T_i \). After that TDS stores the triples \((ID, s_{t0}, K_{00})\) of \( T_i \).

2. Challenge-Response Phase

(1) \( V \rightarrow R \): \( V \) generates \( n \) couples of sub-random-number \((x_i, y_i)\) by \( f(x) \) and sends them to \( R \) \((i = 1, 2, \ldots, n)\). \( V \) stores TS and \( x \) of this grouping-proof session in

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<th>Table 1. Notations of FSGP</th>
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4.1. Notations

We use the notations based on Juel\(^1\) for entities and operations as summarized in Table 1 to simplify description.

4.2. Forward-Secure Grouping-Proof (FSGP)

In the following, we will construct FSGP based on Shamir’s \((n, n)\)-SS, which can recover the original secret \( x \) by collecting \( n \) legitimate (or not forging) sub-secret. Our protocol controls a challenge-response session cycle by timestamp TS and \( \Delta T \). FSGP is invalid when the time of challenge-response exceeds one session cycle. The procedure is described as follows:

1. Initial Setup Phase

TDS selects a PRNG \( g: \{0,1\}^k \rightarrow \{0,1\}^{2k} \) based on \( k \) and sets \( ID \), as the initial seed of \( g \). All tags in Grouping-Proof have the ability of computing \( g \) and meanwhile TDS initializes the current state \( s_{t0} = g(ID) \) of \( T_i \). After that TDS stores the triples \((ID, s_{t0}, K_{00})\) of \( T_i \).

2. Challenge-Response Phase

(1) \( V \rightarrow R \): \( V \) generates \( n \) couples of sub-random-number \((x_i, y_i)\) by \( f(x) \) and sends them to \( R \) \((i = 1, 2, \ldots, n)\). \( V \) stores TS and \( x \) of this grouping-proof session in
(3) $R \rightarrow T_i$: $R$ queries $T_i$ by sending sub-random-number $x_i \in \{1, 2, \ldots, n\}$. 

(4) $T_i \rightarrow R$: $T_i$ computes $m_i = \text{MAC}_{K_{ij}}(x_i)$ and sends the response $(s_{ij}, m_i, (x_i))$ for period $j$ to $R$. ($j=TS$) 

(5) $R \rightarrow V$: $R$ combines $(s_{ij}, m_i, (x_i))$ with another sub-random-number $y_i$ to form $(s_{ij}, m_i, (x_i, y_i))$ and forwards $(s_{ij}, m_i, (x_i, y_i))$ to $V$. 

(6) $V$: $V$ stores $l$ responses $(s_{ij}, m_i, (x_i, y_i))$ ($l<=n$) for period $j$ in the time of $\Delta T$ and meanwhile forms the grouping-proof $P$ of this session $P = (s_{ij}, m_i, (x_i, y_i), s_{ij}, m_2, (x_2, y_2), \ldots, s_{ij}, m_i, (x_i, y_i))$, which proceeds with Validity Authentication Phase. 

3. Validity Authentication Phase 

$V$ searches the triples $(ID_j, s_{ij}, K_{ij})$ in TDS by $s_{ij}$ and checks whether $m_i$ is a valid MAC or not as follows: 

If $m_i$ is valid, $V$ keeps $(s_{ij}, m_i, (x_i, y_i))$ in $P$. Then $P$ will proceed with Legitimacy Authentication Phase. Otherwise, $V$ removes $(s_{ij}, m_i, (x_i, y_i))$ from $P$ and puts $T_i$ into $S$, which shows that $T_i$ is attacked in the form of forging or interpolating the challenge-response by $A$. Then $T_i$ in $S$ will return the second phase of Challenge-Response and wait for proceeding with the next grouping-proof session. 

4. Legitimacy Authentication Phase 

If $P \neq \phi$, the third phase is valid and then $V$ will proceed with this phase to authenticate legitimacy. 

$V$ gets $l$ couples of sub-random-number $(x_i, y_i)$ from $P$ and proceeds with the following steps: 

(1) If $l=n$, $V$ recovers the secret $x'$ based on $(n, n)$-SS and compares $x'$ with the main-random-number $x$. 

If $x'=x$, $P$ is valid, and that means all of the tags $(T_1, T_2, \ldots, T_n)$ are legitimate, and $V$ puts $(T_1, T_2, \ldots, T_n)$ into $H$. Otherwise $P$ is invalid, and that means there are suspicious tags in $(T_1, T_2, \ldots, T_n)$ and $V$ puts $(T_1, T_2, \ldots, T_n)$ into $S$. Then $T_i$ in $S$ will return the second phase of Challenge-Response and wait for proceeding with the next grouping-proof session. 

(2) If $l<n$, $V$ checks $l$ couples of sub-random-number $(x_i, y_i)$ by the polynomial $f(x)$ as follows: 

If $f(x)$ is equal, $T_i$ is legitimate and $V$ puts $T_i$ into $H$. Otherwise $T_i$ is a suspicious tag and $V$ puts $T_i$ into $S$. Then $T_i$ in $S$ will proceed with the same to (1). 

Note: This case indicates that the grouping-proof will convert into a single authentication proof. 

5. State and Key Updating Phase 

(1) If $H \neq \phi$, $V$ computes every $T_i$ in $H$ by $D_i = g(K_{ij} + s_{ij})$ and after $V$ sends $D_i$ to $T_i$ by $R$, $V$ will update $s_{ij}$ and $K_{ij}$ by $s_{ij+\Delta T} = g(s_{ij})$ and $K_{ij+\Delta T} = g(K_{ij})$. TDS stores $(ID_i, s_{ij+\Delta T}, K_{ij+\Delta T})$ and sets $TS = j+\Delta T$. 

After receiving $D_i$, $T_i$ computes $D_i = g(K_{ij} + s_{ij})$ and checks the relation between $D_i$ and $D_i$ as follows: 

If $D_i$ is equal to $D_i$, $T_i$ will update $s_{ij}$ and $K_{ij}$ by $s_{ij+\Delta T} = g(s_{ij})$ and $K_{ij+\Delta T} = g(K_{ij})$. After that $T_i$ deletes $s_{ij}$ and $K_{ij}$. 

Otherwise, $T_i$ will keep $s_{ij}$ and $K_{ij}$ unchanged. 

(2) If $S \neq \phi$, $V$ computes every $T_i$ in $S$ by $E_i = g(s_{ij})$ and then sends it to $T_i$ by $R$. After receiving $E_i$, $T_i$ computes $D_i = g(K_{ij} + s_{ij})$. Because $E_i$ is not equal to $D_i$, $T_i$ and $V$ will keep $s_{ij}$ and $K_{ij}$ unchanged. 

(3) If $h=n$, $P$ is a valid grouping-proof and that means all of the tags are simultaneously scanned and FSGP terminates. 

Otherwise, there are suspicious tags in this session. $V$ sets $n=n-h$ and returns the second Challenge-Response Phase to proceed with the next grouping-proof session. 

Notes: I. The Validity Authentication result of the third phase is described as follows: 

(1) The case of $m_i$ being valid MAC 

① Legitimate $T_i$ with $K_{ij}$ and of not being attacked. Its response is $(s_{ij}, \text{MAC}_{K_{ij}}(x_i), (x_i, y_i))$. 

② Legitimate $T_i$ with $K_{ij}$ and of being interpolated $x_i$ in the Query command from $R$ to $T_i$. Its response is $(s_{ij}, \text{MAC}_{K_{ij}}(x'_i), (x'_i, y_i))$. 

③ Illegitimate $T_i$ without $K_{ij}$ and of being forged $x_i$ in Query command from $R$ to $T_i$. Its response is $(s_{ij}, \text{MAC}_{K_{ij}}(x_i), (x_i, y_i))$. 

(2) The case of $m_i$ being invalid MAC 

① Illegitimate $T_i$ without $K_{ij}$ and of not being attacked. Its response is $(s_{ij}, \text{MAC}_{K_{ij}}(x_i), (x_i, y_i))$. 

② Legitimate $T_i$ with $K_{ij}$ and of being interpolated Response message from $T_i$ to $R$. Its response is $(s_{ij}, \text{MAC}_{K_{ij}}(x_i), (x'_i, y_i))$ or $(s_{ij}, \text{MAC}_{K_{ij}}(x_i), (x_i, y_i))$. 

③ Illegitimate $T_i$ without $K_{ij}$ and of being interpolated Query command or Response message between $T_i$ and $R$. Its response is $(s_{ij}, \text{MAC}_{K_{ij}}(x_i), (x'_i, y_i))$ etc. 

II. The result of Legitimacy Authentication Phase is described as follows:
V puts the legitimate $T_i$ with $K_{ij}$ and those haven’t been attacked into $H$, but others are viewed as suspicious tags and are put into $S$. Then $T_i$ in $S$ will proceed with the same to (1) of Legitimacy Authentication Phase.

The generation process of FSGP is shown in Fig.1. The outputs of FSGP are the legitimate $T_i$ in $H$ and the suspicious $T_i$ in $S$.

5. Evaluation

In this section, we present the security and performance analysis of our protocol FSGP. In addition, we compare FSGP with previous research works based on the typical characteristics of the existing grouping-proof protocols.

5.1. Security analysis

(1) Tag Anonymity: Instead of transmitting static tag $T_i$ identity in plaintext over R-T insecure communication channel, FSGP utilizes a dynamically generated random number $x_i$ by using PRNG and a constructed polynomial $f(x)$ in $(n, n)$-SS to challenge each tag $T_i$ directly during one session to achieve tag anonymity. The response of $T_i$ is the triples $(x_i, m_i, (x_i, x_i))$ which combine MAC of the challenge message $x_i$ with the current state $s_{ij}$ of $T_i$ and only $V$ has the right to verify this session. The responses computed by the tags do not leak any information interrelated with $ID_i$ to any third-party who does not know the private key of $T_i$ in the whole authentication session. Even though the transmitted message $x_i$ or MAC$_{K_{ij}}$ ($x_i$) over the insecure wireless channel can be eavesdropped, it is impossible to obtain the relevant information about $ID_i$ of the legitimate tag $T_i$. The security robustness of $ID_i$ embedded in transmitted messages $x_i$ will not be compromised. Hence, tag anonymity can be guaranteed in our scheme.

(2) Untraceability: On concern of the privacy, FSGP randomizes the direct challenge-response among readers and tags in one session. Since FSGP offers privacy protec­tion against an adversary, the transmitted message over R-T channel and the current state value $s_{ij}$ of $T_i$ depend on the dynamically generated random number $x_i$ which is randomized in different proof sessions. Moreover $V$ changes every Timestamp $TS$ after a successful verification, which adds the difficulties for an attacker to trace tags. On account of the triples $(s_{ij}, m_i, x_i)$ not being the same in different sessions, the adversary cannot obtain the same responses from the same tag $T_i$ by interfering with two or more dependent challenge-response. So the adversary cannot track the legitimate tag $T_i$ and untraceability can be guaranteed. This feature ensures location privacy protection of the tagged objects.

(3) Forward Security: In FSGP, forward security is naturally embedded because $K_{ij}$ shared between $V$ and $T_i$, and $s_{ij}$ of the legitimate tags $T_i$ in $H$ will be automatically updated after each valid grouping-proof session. $V$ sends the message $D_i$ to $T_i$ in $H$ and after $T_i$ checking $D_i$ valid, $T_i$ and $V$ will update $s_{ij}$ and $K_{ij}$ by the updating algorithm $s_{ij+\Delta T} = g(s_{ij})$ and $K_{ij+\Delta T} = g(K_{ij})$. Meanwhile $TDS$ stores the updated triple ($ID_i, s_{ij+\Delta T}, K_{ij+\Delta T}$). $s_{ij}$ and $K_{ij}$ are generated by PRNG and $(s_{ij}, m_i, x_i, K_{ij})$ are updated according to the different sessions. Even if $(s_{ij}, m_i, x_i, K_{ij})$ is eavesdropped, the adversary is not able to obtain the transmitted valid message between reader and tags for the prior period. It is known from $m_i = MAC_{K_{ij}}$ ($x_i$) that $m_i$ is constructed by $K_{ij}$ and the challenge $x_i$ which depends on the sub-random-
number \((x_i, y_i)\) according to the different sessions. It is obvious that \((s_{ij}, m_i, x_i, K_{ij})\) has the characteristic of random and periodic and the adversary cannot obtain \((s_{ij-\Delta T}, m_{i-\Delta T}, x_{i-\Delta T}, K_{ij-\Delta T})\) for period \(j \triangleq T\) by \((s_{ij}, m_i, x_i, K_{ij})\) for period \(j\). The difficulty of obtaining \(s_{ij-\Delta T}, K_{ij-\Delta T}\) by \((s_{ij}, m_i, x_i, K_{ij})\) is equivalent to attacking PRNG. Therefore, even if \(T_i\) was compromised in period \(j\), the grouping-proof before period \(j\) is valid. Hence, the evolutions of \(K_{ij}, s_{ij}\) and the grouping-proof all have forward security which protects past communications of a compromised tag.

(4) Resistance to Replay Attack: It was a specific design feature of FSGP that only the trusted verifier can check the correctness of the grouping-proof. FSGP uses the randomized direct challenge-response, MAC computation of the dynamically generated random number \(x\), with \(K_{ij}\) to defend against replay attack and meanwhile \(V\) stores \((s_{ij}, m_i, (x_i, y_i))\) in TDS. Because of this feature, \(V\) will accept the response only when the two responses \((s_{ij}, m_i, (x_i, y_i))\) of \(T_i\) are different. That is if two or more responses of \(T_i\) are the same in one session, \(V\) will refuse to accept. Additionally, even if the triples \((s_{ij}, m_i, x_i)\) are eavesdropped, an adversary cannot impersonate the legitimate tag \(T_i\) by replaying the response of \(T_i\) and \(V\) can identify the adversary. Hence, our protocol can resist replay attacks.

(5) Resistance to Man-In-The-Middle Attack (MITM): In order to obtain valid message of tags in a successful session, an adversary tries to intercept the transmitted message over R-T channel and interfere in the challenge-response but V-R-T cannot detect.

Case(1) Supposing that an adversary eavesdrops one or more challenges \(x_i\) during the challenge phase and interpolates it into \(x_i'\). To this case, MITM attack is described as follows:

(I) If the adversary sends \(x_i'\) to the legitimate \(T_i\), the response of \(T_i\) is \((s_{ij}, \text{MAC}_{K_{ij}}(x_i'), x_i')\) and then \(R\) sends \((s_{ij}, \text{MAC}_{K_{ij}}(x_i'), (x_i', y_i))\) to \(V\). According to Validity Authentication Phase, it is clear that \(\text{MAC}_{K_{ij}}(x_i')\) is invalid by \(x_i'\) and \(K_{ij}\). Therefore, Validity Authentication Phase will not be allowed, that means MITM attack cannot succeed.

Case(2) Supposing that an adversary eavesdrops one or more responses of \(T_i\) during the response phase and interpolates them. To this case, MITM attack is described as follows:

(I) If the adversary interpolates the response of legitimate \(T_i\) into \((s_{ij}, \text{MAC}_{K_{ij}}(x_i), x_i')\) or \((s_{ij}, \text{MAC}_{K_{ij}}(x_i), (x_i', y_i))\) and then \(R\) sends \((s_{ij}, \text{MAC}_{K_{ij}}(x_i), (x_i', y_i))\) or \((s_{ij}, \text{MAC}_{K_{ij}}(x_i), (x_i', y_i))\) to \(V\). According to Validity Authentication Phase, it is clear that \(\text{MAC}_{K_{ij}}(x_i)\) and \(\text{MAC}_{K_{ij}}(x_i)\) are invalid MAC by \(K_{ij}\). Therefore, Validity Authentication Phase will not be allowed, that means MITM attack cannot succeed.

Based on the analysis of Case(1,2), the interference of FSGP will not be successful. Furthermore, even if the adversary eavesdrops all of \(n\) challenge \(x_i\) of this current session, he cannot be able to reconstruct the main-random-number \(x_i\) of his current session without knowing \(y_i\). Hence, FSGP are immune to MITM attack.

(6) Resistance to Counterfeit Attack: To defend against counterfeit attack, FSGP utilize a timeout mechanism to ensure that all the proof-involved tags coexist at a specific and limited time period. \(V\) will not accept the response which is forged or reaches out of TS in the current session. The detailed analysis is described as follows:

Case(1) \(T_i\) Impersonation Resistance: An adversary tries to impersonate a legitimate \(T_i\) within the broadcast range of \(R\) in this session by forging the legitimate response \((s_{ij}, \text{MAC}_{K_{ij}}(x_i), x_i)\). On account of \(K_{ij}\) only shared by \(V\) and \(T_i\), even if the legitimate response \(\text{MAC}_{K_{ij}}(x_i)\) is eavesdropped from R-T channel, the difficulty of obtaining \(K_{ij}\) of the legitimate \(T_i\) by \(\text{MAC}_{K_{ij}}(x_i)\) is equivalent to attacking MAC \(^{1}\). Supposing that the adversary impersonates a tag \(T_i'\) with the secret key \(K_{ij}\), the corresponding response of \(T_i'\) is \((s_{ij}, \text{MAC}_{K_{ij}}(x_i), x_i)\) to the challenge \(x_i\) from \(R\).
and then R sends \((s_{ij}, \text{MAC}_{K'_{ij}}(x_i), (x_i, y_i))\) to V. Since \(K'_{ij} \neq K_{ij}\), V utilizes \(K_{ij}\) to proceed with Validity Authentication Phase and then gets the result \(\text{MAC}_{K'_{ij}}(x_i) \neq \text{MAC}_{K_{ij}}(x_i)\) which indicates \(\text{MAC}_{K'_{ij}}(x_i)\) is invalid MAC. It is clear that Validity Authentication Phase cannot be validated. Even though the adversary tries to modify the received challenge \(x_i\) into \(x'_i\) to meet the requirement of \(\text{MAC}_{K'_{ij}}(x'_i) = \text{MAC}_{K_{ij}}(x_i)\), this difficulty is also equivalent to attacking MAC\(^1\). Therefore, Ti Impersonation Resistance will not succeed.

Moreover, FSGP can defend against illegitimate Ti of malicious counterfeit which is activated by a malicious R because Ti is out of the broadcast range of the readers. The detailed analysis process is similar to the above Ti Impersonation Resistance and (5) Case\(^2\). Therefore this kind of malicious attack cannot succeed.

Case\(^2\) R Impersonation Resistance: An adversary tries to impersonate a legitimate R in this session and transmits the challenge-response over V-T by the forged R. Because the transmitted challenge-response over V-T communication channel are not relevant to \(ID_i\) of legitimate Ti and moreover \(s_{ij}\) is generated by PRNG and updated according to the different sessions, the forged R cannot obtain any information about the privacy of Ti. If the forged R tries to eavesdrop and modify the transmitted challenge-response over V–T, the grouping-proof will not be allowed, that means that attacking to R Impersonation cannot succeed. The detailed process refers to the analysis of (5).

Hence, FSGP can resist both Ti and R impersonation attack and has the property of strong unforgeability.

### 5.2. Performance analysis

Since RFID tags are generally low cost with extremely limited resources, it is necessary for tags to achieve authentication by using the lightweight primitives. According to the requirement of resource-constrained devices, in our grouping-proof FSGP, only simple control commands and three primitive arithmetic operations are required, such as Lagrange interpolating polynomial \(f(x)\) construction, random number generator \(\text{PRNG()}\) and minimalist message authentication code \(\text{MAC}[]\) of sub-random-number. Moreover, we put the construction operation of \(f(x)\) over Verifier and the operations of PRNG and MAC are required at the tag end. Based on the research results in\(^{1,4}\) and EPC standard specification\(^2\), it is proved that these computation costs can be afforded by resource-constrained tags. Hence, we think that FSGP is very competitive to be a solution candidate on forward-secure grouping-proof for RFID tags.

### 5.3. Security comparison

In the following, we compare FSGP with previous related works in terms of security and privacy aspects (see Table 2), which shows that security robustness of our protocol is superior to the others by supporting tag anonymity, untraceability, forward security, and resisting to security threats such as replay attack, MITM attack and counterfeit attack.

In summary, based on the above analysis and security comparison, our protocol FSGP has the characteristics of forward-security, robustness, order-

<table>
<thead>
<tr>
<th>Table 2. Security comparison between FSGP and related grouping-proof protocols</th>
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<tbody>
<tr>
<td>Tag</td>
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<tr>
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</tr>
<tr>
<td>Yoking-proofs(^1)</td>
</tr>
<tr>
<td>Grouping-proofs(^2)</td>
</tr>
<tr>
<td>Existences-proofs(^3)</td>
</tr>
<tr>
<td>Generalized Yoking-proofs(^4)</td>
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<td>Clumping-proofs(^5)</td>
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<td>Provably–secure proofs(^6)</td>
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<tr>
<td>Coexistence-proofs(^7)</td>
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<tr>
<td>Order-independent proofs(^8)</td>
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<tr>
<td>FSGP</td>
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</tbody>
</table>
independence and efficiency compared with the previous related protocols.

6. Conclusion

To overcome the weakness of security and/or privacy omission and order-dependence in the previous grouping-proof protocols, in this paper we develop a grouping-proof protocol with forward security for multiple RFID tags based on Shamir’s \((n, n)\) secret sharing, called FSGP, which solves the scalability issue properly by avoiding relaying message among tags through RFID reader and meanwhile achieves security enhancement and robust privacy protection. FSGP can defend against malicious attacks and possess excellent privacy properties and also realizes a single authentication protocol in combination with a grouping-proof protocol properly by the application of CI. In terms of protocol performance measurement, our protocol is lightweight which meets the requirement of resource-constrained RFID tags without increasing much computing burden at both tag end and server end. In the future, as complexity of technology and networks’ services increase new challenging multi-combinatorial problems are emerging and consequently the CI applications are apt to further enhancement in the environment of Internet of things.

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