

Modeling the optimal distribution of profits for risk management of oil and gas enterprises

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Abstract— The article discusses the optimal management of the distribution of net profit of oil and gas enterprises in order to minimize its risks. The constructed utility function acts as a criterion of optimality. Management parameters are fractions of net profit aimed at achieving the final predicted value of the studied variables. To solve this problem, a mathematical apparatus was used, based on the theory of the Pontryagin maximum principle. As a numerical experiment, some options are proposed for optimal management of the distribution of net profit of the National Joint Stock Company Naftogaz of Ukraine for the period 2018-2022. Numerical results are given taking into account the discounting of financial flows. The proposed algorithm allows to obtain the optimal distribution of net profit within one oil and gas enterprise, which includes structural units, as well as on the scale of a group of enterprises united by one governing body that distributes financial resources for risk management.

Keywords—profit, oil and gas enterprises, optimal management, utility function, risk

I. INTRODUCTION

The modern system of economic relations requires significant changes in the content and forms of risk management in the activities of oil and gas enterprises. Today, the development of fuel and energy enterprises in Ukraine is in a state of uncertainty and risk. Instability of the environment negatively affects the activities of enterprises and their financial and economic situation. Insufficient attention to the issues of the influence of various factors on the production and economic activities of enterprises, the timeliness of measures for risk management leads to an inadequate reaction of individual enterprises to the dangers and threats that arise in the modern economic environment, and, as a result, the adoption of unjustified management decisions. Babenko et al. [1] consider multivariate regression models to make informed management decisions. Today, risk management measures are financed in the same amount regardless of the level of risk and the changing factors of the internal and external environment. All this contributes to the emergence of significant threats to the activities of enterprises, their limited mobility and the loss of potential opportunities. Therefore, there is a need to

develop a new risk management approach based on modeling the optimal distribution of net profit to minimize risks and improve the management of oil and gas enterprises. Oliinyk & Bielova [2] uses portfolio theory to optimize risk management of an enterprise's finances.

II. LITERATURE REVIEW

The strategic basis for improving the financial and economic condition and development of enterprises is strategic planning. The most important role in this is played by risk management and ensuring an adequate level of enterprise security. Problems of the theory, methodology and practice of risk management were devoted to the scientific works by domestic and foreign economists: Donecz & Prudnikova [3], Horal & Fadievskaya [4], Shumilova & Karataev [5], Panyagina [6], Nechaev & Prokopyeva [7], Kaverina [8], Matviychuk et al. [9], Sudomyr [10], Shandova [11], V. Lukianova, V. Vitlinskyi, V. Lopatovskyi, A. Starostina, N. Khokhlova and other scientists. The need to create and implement a risk management mechanism is confirmed by the works: Ustenko & Rishhuk [12], Konovalov & Mironov [13], Sydoruk & Baldyniuk [14], Sementsov [15], Kalashnykova [16], Khvostina et al. [17], Li [18], Mensah & Gottwald [19], Xu [20], Rogers & Ethridge [21], Lambrechts & Blomquist [22], Berlin et al. [23], N. Havadzyn, N. Yurchenko, L. Neykova, T. Pakhomova, Y. Tyuleneva and other scientists. Paying tribute to the scientific excellence of scientists, it should be noted that in the economic literature does not find a proper solution complex approach to enterprise risk management. In particular, there is no defined system of distribution of financial resources taking into account different levels of risk, as well as different efficiency of investment of financial resources, taking into account the specific activity of enterprises. The scientific-theoretical and practical significance of these problems necessitates further research into risk management issues.

III. METHODS

The methodological basis of this study is the following scientific research methods: statistical analysis; correlation

and regression analysis; factor analysis; simulation modeling; Pontryagin maximum principle.

IV. DISCUSSIONS AND RESULTS

This study proposes a mathematical model of the distribution of net profit of the enterprise. The independent variables are indicators that reflect the direction of use of net profit. It is assumed that, based on historical data, one can find a regression equation for the dependence of the net profit of the enterprise $P(t)$ on these variables, namely:

$$P(t) = a_0 + \sum_{i=1}^n a_i X_i(t) \quad (1)$$

where a_0 is the free term in the regression equation; a_i - regression coefficients ($i = \overline{1, n}$); $X_i(t)$ - independent variables ($i = \overline{1, n}$). We assume that the regression equation (1) is adequate relative to the resulting result. If the linear regression equation does not allow to obtain the desired result, then it is necessary to use a nonlinear regression equation with respect to independent variables.

For further research, it is necessary to find the distribution of independent variables for the forecast period. We assume that on the basis of historical data, the rate of change of these variables obeys some distribution law. The form of this equation depends on the numerical values obtained both on the historical period and on the final necessary result.

The task is to determine the optimal use of net profit for transferring the system from an initial state to a given final state. The utility function is the utility function of the enterprise under study. Management parameters are the shares of net profit aimed at fulfilling the task. To solve the problem of optimal management of the distribution of net profit of the enterprise, it is necessary to solve the following system.

1. The system of differential equations:

$$\frac{dX_i(t)}{dt} = \mu_i X_i(t) + V_i(t), (i = \overline{1, n}) \quad (2)$$

where μ_i is the intensity of the change of the investigated variable $X_i(t)$; $V_i(t) = v_i P(t)$ - management functions;

v_i - control parameters ($0 \leq v_i \leq 1, i = \overline{1, n}; \sum_{i=1}^n v_i \leq 1$).

2. Initial conditions :

$$X_i(t_0) = X_i^0 \quad (3)$$

3. Utility function for the enterprise:

$$\int_{t_0}^T \exp(-\delta t) \{1 - \sum_{i=1}^n \exp[-v_i(t)P(t)]\} dt + \sum_{i=1}^n b_i X_i(T) \rightarrow \max \quad (4)$$

where b_i are the coefficients of the studied variables at a finite instant of time T (obtained from the transversality condition); $\delta = \ln(1+i)$ - interest accrual rate; i - interest rate (discount) (%).

As a result, we obtain a mathematical model of the optimal distribution of net profit of the enterprise. It is assumed that independent variables are transferred from a given initial state to a given final state along an optimal path relative to control parameters. To solve the resulting system (1) - (4), we use the Pontryagin maximum principle [24, 25]. The type of solution depends on the number of independent variables and the regression equation (1).

We find a solution to the problem for the case of the distribution of net profit in four directions and a linear regression equation. The main directions of using net profit: X_1 - reinvestment in assets; X_2 - deductions to reserve capital; X_3 - amount to prevent possible risks; X_4 - deduction to the State budget of Ukraine. In the model, we assume that the deduction to the State budget of Ukraine is a constant percentage of the company's net profit. In the further enumerated implementation, we will consider several possible options (30%, 40%, 50%).

To solve this problem, we construct the Hamiltonian function:

$$H(t) = \sum_{i=1}^3 \Psi_i(t)(\mu_i X_i(t) + v_i(t)P(t)) + \exp(-\delta t) \{1 - \sum_{i=1}^3 \exp(-v_i(t)P(t))\} \quad (5)$$

where $P(t) = (1 - v_4)\pi(t)$; $\Psi_i(t)$ - auxiliary functions found from the system of differential equations (6):

$$\begin{aligned} \frac{d\Psi_j(t)}{dt} = & -\{\mu_j \Psi_j(t) + \\ & + (1 - v_4) a_j [\sum_{i=1}^3 \Psi_i(t) v_i(t) + \\ & + \exp(-\delta t) \sum_{i=1}^3 v_i(t) \exp(-v_i(t)P(t))]\} \end{aligned}, (j = \overline{1, 3}) \quad (6)$$

Auxiliary functions must satisfy the transversality condition:

$$\Psi_i(T) = -b_i, (i = \overline{1, 3}) \quad (7)$$

The optimal control parameters are:

$$v_i^* = -\frac{\ln(-\Psi_i(t)) + \delta t}{P(t)}, (i = \overline{1, 3}) \quad (8)$$

As a numerical implementation of the proposed algorithm, we consider the National Joint Stock Company Naftogaz of Ukraine. We will use the results of their activities in 2018 as initial data. Consider the options for the distribution of net profit for a five-year period. To solve this problem, it is necessary to set the numerical values of the independent variables in 2022. The initial data for the calculation are presented in Table 1.

TABLE I. DATA OF ACTIVITY OF NAFTOGAS UKRAINE, UAH MILLION

	Indicators	2018	2022
$\pi(t)$	Net profit	13613,258*	84129
$X_1(t)$	Assets	495025,674*	1089056
$X_2(t)$	Allocation to reserve capital	1960,507*	3034
$X_3(t)$	Amount to prevent possible risks	1000,000	3253
$X_4(t)$	Deduction to the State Budget of Ukraine	4083,977*	25238

Note: * - balance sheet data of NJSK Naftogaz of Ukraine, [26].

Consider several options for the optimal distribution of net profit, depending on a fixed amount of distribution to the State budget of Ukraine and the discount coefficient. For numerical implementation, we assume that the initial conditions (3) have the following form: $X_i(2018)=1$, ($i=\overline{1,3}$). We transform the regression equation (1) to the form:

$$\pi(t) = 8,44 + 2,14X_1 - 14,15X_2 + 4,57X_3 \quad (9)$$

Table 2 shows the optimal distribution of net profit in three directions, taking into account a discount coefficient of zero and deductions to the State budget of Ukraine of 30% of the net profit.

TABLE II. TABLE 2. DYNAMICS OF FINANCIAL FLOWS OF NAFTOGAS UKRAINE 2018-2022, ($\delta = 0$, $\nu_4 = 0,3$)

Indicator	2018	2019	2020	2021	2022
$\pi(t)$	1	1,463	2,387	3,904	6,18
$X_1(t)$	1	1,136	1,374	1,726	2,2
$X_2(t)$	1	1,064	1,174	1,333	1,543
$X_3(t)$	1	1,235	1,667	2,328	3,253

Table 3 presents the optimal share distribution of net profit in the proposed areas of use without taking into account the discount coefficient when deducting 30%, 40% and 50% of the net profit of the enterprise to the State budget of Ukraine.

TABLE III. SHARED DISTRIBUTION OF PURE PROFIT OF NAFTOGAS UKRAINE 2018-2022, ($\delta = 0$)

Indicator	2018	2019	2020	2021	2022
$\nu_4 = 0,3$					
$\nu_1(t)$	0	0,085	0,104	0,096	0,081
$\nu_2(t)$	0	0,04	0,05	0,046	0,039
$\nu_3(t)$	0	0,143	0,176	0,162	0,137
$\nu_4 = 0,4$					
$\nu_1(t)$	0	0,099	0,122	0,111	0,094
$\nu_2(t)$	0	0,047	0,059	0,054	0,046
$\nu_3(t)$	0	0,166	0,205	0,189	0,159
$\nu_4 = 0,5$					
$\nu_1(t)$	0	0,119	0,146	0,134	0,113
$\nu_2(t)$	0	0,056	0,07	0,065	0,055
$\nu_3(t)$	0	0,2	0,246	0,226	0,191

Table 4 shows the optimal distribution of the share distribution of net profit on the proposed variables and the trajectory of financial flows, taking into account the rate of interest and deductions to the State budget of Ukraine, 30% of net profit.

TABLE IV. DYNAMICS OF FINANCIAL FLOWS OF NAFTOGAZ UKRAINE 2018-2022, ($\delta = 0,05$; $\nu_4 = 0,3$)

Indicator	2018	2019	2020	2021	2022
$\pi(t)$	1	0,898	1,64	3,351	6,18
$X_1(t)$	1	1,208	1,474	1,802	2,2
$\nu_1(t)$	0,134	0,208	0,146	0,087	0,056
$X_2(t)$	1	1,137	1,274	1,409	1,543
$\nu_2(t)$	0,136	0,14	0,071	0,032	0,016
$X_3(t)$	1	1,306	1,766	2,406	3,253
$\nu_3(t)$	0,126	0,296	0,247	0,163	0,111

Tables 1-4 show the optimal distribution of the company's net profit for the period 2018-2022 depending on the contributions to the State Budget of Ukraine and the discount factor. An analysis of the results shows that the maximum value of deductions from net profit excluding discounting flows falls on 2020, and taking into account the discount factor falls on 2019.

V. CONCLUSIONS

In this paper, we consider the problem of optimal management of the company's net profit. The distribution of net profit occurs in the most important areas of its use. One of the main areas is the use of profits to prevent possible damage from various risks. In this statement, an obligatory deduction to the State Budget of Ukraine is assumed. The optimal profit management of the enterprise is simulated, with these deductions in the amount of 30%, 40% or 50%. Tables 2 and 3 show the distribution of net profit for the period up to 2022 without taking into account the discount factor. Table 4 shows the dynamics of financial flows and the share distribution of net profit of NJSK Naftogaz of Ukraine, taking into account the discount factor and deductions to the State budget of Ukraine in the amount of 30% of the net profit ($\delta = 0,05$; $\nu_4 = 0,3$).

Thus, the effective operation of oil and gas enterprises requires the use of modern approaches to risk management with the obligatory consideration of external and internal factors causing risks in the economic activities of enterprises. The solution to the problem ensures the optimal distribution of profits at oil and gas enterprises and the development of alternative risk management options in a highly dynamic environment. Continuous science-based monitoring of current processes at the enterprise, their assessment and forecasting of changes is the basis for optimizing the development of managerial decisions aimed at improving the overall performance of the oil and gas enterprise. In this regard, an integral part of modeling the optimal profit management of an enterprise is the operational monitoring of the current activity of the enterprise and risk factors.

This mathematical model can be used as a guideline for adoption by the top management of the enterprise of a long-term plan for its development.

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