



P66 Mathematical Model of the Renal Microcirculation and Effects of Chronic Kidney Disease

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ABSTRACT

Background: Diabetes is one of the leading causes of chronic kidney disease (CKD) worldwide. CKD is directly linked to increased morbidity and mortality. The role of vascular changes in diabetes and underlying mechanism of kidney disease is not well understood.

Methods: We present a mathematical model of the small arteries in the kidney incorporating anatomical and dynamic features. It consists of a symmetrical bifurcating tree self-similar in length, cross-sectional area and wave speed. Each generation is related to the previous one by the scaling factors e.g. $\ln + 1 = \lambda \ln$, this gives properties (e.g. surface area, resistance) for each generation by a priori knowledge of the renal artery. We assume the flow is one-dimensional and laminar. Vessel walls are treated as porous media to find the glomerulus transmural flux. Effects of compliance are introduced by a pressure-area relationship based on circumferential stress in thin vessel walls. The set of ordinary differential equations is solved numerically.

Results: The results are in accordance with physiological measurements and indicate that pressure in the vasculature is highly sensitive to changes in vessel geometry, which also affects the transmural flux in the glomerulus. Changes in the structure of the arterial wall (e.g. Young's modulus) alter the dynamics of the flow with an increased effect in the micro-circulation.

Conclusion: This is a functional model describing the behaviour of the small vasculature in the kidney. The model is computationally inexpensive, can be used for analysis and tested with *in vivo* data in pathological conditions.

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