Are there Differences in Reflective Thinking Between Male and Female Prospective Mathematics Teachers?

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ABSTRACT
Reflective thinking is a thinking process involves re-investigations to overcome confusion for problem solving. This type of thinking is important for prospective mathematics teachers because the thinking can be a competence for them to teach mathematics effectively. In Indonesia, in the last three years there have been more female prospective mathematics teachers than male. Geometry is one of the difficult topics for the prospective teachers. There are four aspects of reflective thinking, namely techniques, monitoring, insight, and conceptualization. This study examines the differences in reflective thinking of male and female prospective mathematics teachers in solving analytical geometry problems in the four aspects. This research approach is qualitative. The research instrument was developed by the researchers and already valid. This research conducted at the Universitas Negeri Malang and Universitas Muhammadiyah Surakarta. The amount of the subjects were 83 prospective mathematics teachers who have taken analytical geometry courses in 2019/2020. Researchers collected data through test and interview techniques. The instrument validation and triangulation processes are carried out as an effort to validate the data. Data analysed through the stages of reduction, presentation, and verification. The results of this study indicate that the differences in reflective thinking of both lies in the three aspects.

Keywords: Reflective thinking, prospective mathematics teachers, analytical geometry, problem solving.

1. INTRODUCTION
The development of mathematics has many roles for the discovery of other sciences [1]. Mathematics is an abstract patterned science to solve problems as a guide in studying other sciences and technology [2]. The problem solvers’ ability to solve mathematical problems does not match the demands of solving new problems. Discrepancy is that problem solvers are not able to relate new problems with the knowledge and experience they have [3]. In solving a problem, they must employ a thinking process. Thinking as a mental activity that aims to make decisions or draw conclusions [4,5]. Furthermore, to obtain new knowledge, problem solvers need to employ attributes in thinking such as abstraction, logic, imagination, and problem solving [6]. Moreover, thinking is considered as a process of understanding in solving problems [7].

Prior studies say that there are differences in thinking skills in problem solving between male and female problem solvers. First, male problem solvers show better performance in solving problems employee spatial skills [8]. It is relevant to a statement that male problem solvers have a better strategy in solving mathematical problems in terms of insight [9]. Third, statistically men are able to solve mathematical problems better than women in terms of attitude [10]. The attitude mentioned is open-mindedness. To sum up, the studies revealed that there are differences in thinking skills between male and female problem solvers. Unfortunately, there are no studies that focus on comparing reflective thinking skills between male and female problem solvers.

Reflective thinking as an active, persistent, and thoughtful thinking activity based on own knowledge in making decision [11]. Reflective thinking begins with confusion and re-evaluation for problem solving [12]. Reflective thinking is important for prospective mathematics teachers, it can be a competence for them to teach mathematics effectively. The authors have reviewed several studies related to reflective thinking. In general, these studies are grouped into three focuses. First, studies that produce instruments related to reflective thinking
The instruments developed include: 1) the scale of reflective thinking, 2) the reflective thinking questionnaire, 3) the guidelines table for checking reflective thinking, and 4) the rubric for evaluating reflective thinking (REPORT). Second, research on the role of reflective thinking on problem solvers’ performances [15, 18–23]. The results concluded that reflective thinking: 1) minimizes problem solvers’ weaknesses in overcoming difficulties, 2) encourages problem solvers to obtain logical solutions, and 3) encourages problem solvers to re-evaluate the strategies used. Third, research that results in: 1) the category of reflective thinking [24], 2) the level of reflective thinking [15], and 3) aspects of reflective thinking [25].

Based on these studies reviewed, there is an opportunity to conduct research related to differences in reflective thinking between male and female prospective mathematics teachers. In Indonesia, in the last three years there have been more female prospective mathematics teachers than male. Data from Indonesian Ministry of Education shows that over the last three years the percentage of female teachers is around 66%. Data presented in Figure 1.

Figure 1 Percentage of teachers in Indonesia in terms of gender.

Reflective thinking begins with confusion by the problem solvers [26]. Thus, the type of question employed to understand problem solvers’ reflective thinking is a question that can stimulate confusion. It may be a non-routine problem-solving question. A non-routine problem-solving question is an unfamiliar problem for prospective mathematics teachers so it causes a confusion to stimulate the emergence of reflective thinking[3,27]. The type of question can be encountered in analytical geometry content. Furthermore, in solving analytical geometry problem they need to have a good understanding [28,29]. A non-routine question in analytical geometry content is an unfamiliar problem so that it can stimulate confusion. Moreover, a non-routine problem-solving question employee knowledge and experience. Thus, it is very compatible for understanding problem solvers’ reflective thinking.

There are four components of reflective thinking [30], namely: (1) techniques, (2) monitoring, (3) insight (ingenuity), and (4) conceptualization. Authors conducted preliminary research to explore the indicators of each aspect. The indicators employed for this study presented in Table 1.

Table 1. Indicator of reflective thinking

<table>
<thead>
<tr>
<th>Aspects</th>
<th>Indicators</th>
</tr>
</thead>
<tbody>
<tr>
<td>Techniques</td>
<td>1. Finding how to understand the information</td>
</tr>
<tr>
<td></td>
<td>2. Finding how to understand the question</td>
</tr>
<tr>
<td></td>
<td>3. Selecting an effective and efficient solution</td>
</tr>
<tr>
<td>Monitoring</td>
<td>1. Monitoring the steps of solution</td>
</tr>
<tr>
<td></td>
<td>2. Monitoring the answer whether correct or not</td>
</tr>
<tr>
<td>Insight</td>
<td>1. Being ready to correct wrong answers</td>
</tr>
<tr>
<td></td>
<td>2. Understanding how to avoid difficulties</td>
</tr>
<tr>
<td>Conceptualization</td>
<td>1. Thinking about an alternative solution</td>
</tr>
<tr>
<td></td>
<td>2. Relating concepts to question</td>
</tr>
</tbody>
</table>

The research aims to describe the differences in reflective thinking between male and female prospective mathematics teachers based on components of techniques, monitoring, insight, and conceptualization in solving a non-routine analytical geometry problem. The objective will be described qualitatively.

2. METHODS

2.1. Design

The research describes the differences in reflective thinking between male and female prospective mathematics. Data described the fact of prospective mathematics teachers’ reflective thinking without any manipulation, it means the study employees a descriptive design [31].

2.2. Participants

The subjects were prospective mathematics teachers from Universitas Muhammadiyah Surakarta and Malang State University, totalling 83 participants (23 male and 60 female). The sampling employed is purposive method [32]. Subjects are prospective mathematics teachers taken analytical geometry courses, employee reflective thinking in solving problems, and have good communication skills. In this paper, data presented on two male subjects and two female subjects because their data represent the entire data.
2.3. Instruments

The instruments employed in this study are: 1) test, 2) observation sheet, and 3) interview guidelines. The test contains an item of non-routine question. The question facilitates in measuring reflective thinking indicators. Moreover, observation sheet is a piece of sheet to check whether reflective thinking indicator satisfied or not. Researchers put a checklist sign (√) in column “YES” if the subjects satisfy the indicator, in column “NOT” if the subjects do not satisfy the indicator, and in column “GREY” if the researchers’ feeling doubt whether the subjects satisfy the indicator or not. The doubt will be confirmed by in-depth interview. The focus of questions in in-depth interviews is to explore the subject's reflective thinking in solving problems more deeply. Besides that, in-depth interviews conducted to confirm whether the indicators of reflective thinking were carried out by the subject or not. The instruments declared as valid instruments by validators expert in mathematics, mathematics education, and thinking skill research.

2.4. Data Collection Method

Data collection techniques in this study are test, video recordings, interviews, and observation sheet. The test employed to understand prospective mathematics teachers’ reflective thinking. Think aloud technique is the most effective method employed in solving problems to understand problem solvers’ reflective thinking [33]. The problem presented in Figure 2.

![TEST INSTRUMENT ANALYTICAL GEOMETRY PROBLEM](image)

**Figure 2** The non-routine problem-solving question in analytical geometry content.

2.5. Data Analysis

Data analysis through the stage of data reduction, data presentation, and drawing conclusions. In reduction stage, data reduced by referring to the aim of the research. In presentation stage, the data of subjects’ reflective thinking reported. The data triangulation process conducted by matching the subject’s reflective thinking data obtained by the test method, video recordings, interviews, and observation sheets. The data employed at triangulation process are only data that support researchers to draw conclusions. The complete research procedure presented in Figure 3.

![Research Procedure](image)

**Figure 3** Research Procedure.

3. FINDING

In this section data are presented from two male subjects (S-1 and S-2) and two female subjects (S-3 and S-4).

3.1. Subject S-1: data exposure and analysis

Figure 4 depicts the answer sheet of S-1. S-1 rewrote the given information. The direction number of line \( g: x = y = z \) written as \( l_1, l_1, l_1 \). S-1 determined the equation of plane \( V \) where \( V \) throughs point \( P (1,0,2) \) and perpendicular to line \( g \). After obtaining the equation \( V: x + y + z - 3 = 0 \), S-1 thought of a way to determine the intersection between plane \( V \) and line \( g \). At this stage, S-1 employed the parameter \( t \). The intersection should be \( A (1, 1,1) \). Thus, the radius is the distance between \( P \) and \( A \), which is \( r = \sqrt{2} \). S-1 understood that the spherical has \( P (1,0,2) \) and radius \( r = \sqrt{2} \). S-1 determined equation of the spherical is \( x^2+y^2+z^2-2x-4z+3=0 \). In determining the spherical equation, S-1 experienced confusion, this seems to be a graffiti on the answer sheet. S-1 overcome confusion by checking the completion steps and answers.
3.2. Subject S-2: data exposure and analysis

Figure 5 is the answer sheet of S-2. S-2 rewrote the given information. S-2 understands that the directional number of line g:1,1,1. First, S-2 determined the equation of plane V, where V throughs point P (1,0,2) and perpendicular to line g. At this stage the S-2 experiences confusion. He made a mistake in substituting the directional numbers into the plane equation. S-2 overcome confusion by clarifying. It means checking back the direction numbers. He determined equation of V:x+y+z-3=0. Next, he determined the intersection between plane V:x+y+z-3=0 and the line g:x=y=z. In this step, S-1 experienced confusion, this seems to be a graffiti on the answer sheet. The parameter t employed to determine the intersection A. After conducting a calculation, he got the intersection is A (1,1,1).

3.3. Subject S-3: data exposure and analysis

Figure 6 illustrated the answer sheet of S-3. She did not re-write the given information. However, she drew back the given sketches to facilitate solving problem. First, S-3 determines the radius of the spherical. After conducting calculation, she gets $r = \sqrt{3x_1^2 - 6x_1 + 5}$. In determining value r, S-3 experienced confusion, this seems to be a graffiti on the answer sheet. Re-monitoring conducted to overcome the confusion. She understood that the spherical equation is $(x-x_1)^2 + (y-y_1)^2 + (z-z_1)^2 = r^2$. However, S-3 cannot do conceptualization that causes errors in drawing conclusions. She concluded that there is no sphere under centre P (1,0,2) and tangents g:x=y=z.
3.4. Subject S-4: data exposure and analysis

Fig 7 depicts the S-4 answer sheet. In solving analytical geometry problems, she does not rewrite the given information. S-4 understands that the sphere equation \((x-a)^2+(y-b)^2+(z-c)^2 = r^2\) with the center \((a, b, c)\) and radius \(r\). S-4 replaces \((a, b, c)\) by \((1,0,2)\), so that she finds \((x-1)^2+(y-0)^2+(z-2)^2 = r^2\) as equation (1). The next step, S-4 determines \(r\). At the stage, she understands that the radius of the sphere is the distance of the center point with the line \(g: x = y = z\). The value of \(r = \sqrt{3x^2-6x+5}\). S-4 substitutes the value of \(r\) into equation (1) so that she concludes that the sphere equation should be \(-2x^2+y^2+z^2+4x-4z = 0\).

**Figure 6** Answer sheet of S-3.

**Figure 7** Answer sheet of S-4.

4. DISCUSSION

In the aspect of techniques, males and females are able to screen out information and question. However, males prefer to rewrite information while females do not. Another difference that stands out is that males tend to employee an efficient and effective way in solving problems because they have good ability in technical matters and strategies [34]. Moreover, males have a deep understanding of problem patterns and approaches for problem solving. They can see the problems clearly and solve in the simplest way [35,36]. This is caused by several factors, for example cognitive ability and speed in processing information [9]. Females prefer to redraw the sketches to facilitate problem solving, on the one hand. On the other hand, males do not because they have better visual spatial abilities in making visualization in their cognitive [37–39]. This is closely related to the level of testosterone is more dominant in males than those in females [39], and they also have the better right hemisphere [40].

In the aspect of monitoring, males and females showed the same tendency to re-monitor the steps and the conclusion. Re-monitoring conducted to ensure that the steps and answers are correct. The results of monitoring presented by the graffities in their answer sheets. This is a part of the problem-solving process in creating a sense of confidence about their answers [30]. This is relevant to the statement that in solving problems the prospective mathematics teacher checks their steps in ensuring the answers are correct [41,42]. Monitoring usually appears in open-ended problems [43,44], but this study shows that the monitoring aspect also appears in non-routine problems. This is because non-routine problems can cause
confusion to the problem solver and stimulate them to conduct monitoring [45,46].

In the aspect of insight shows that prospective mathematics teachers have the willingness to correct errors answers. Improvements are indicated by the graffities on the answer sheet. A striking difference is that males look enthusiastic and have good self-confidence. This statement is relevant to the results of research that men are more confident in their mathematical abilities [47]. Additionally, the researchers discovered that females often doubt their work and experience more mathematical anxiety. However, females are greater in solving open-ended problems where processes are more important than correct solutions [38]. This is because females prefer to think of different processes to solve similar problems. In other words, it is easier for males to construct knowledge in their cognitive development than females [48,49] because males have cognitive capacities that are more flexible in the hemisphere [50].

In the aspect of conceptualization, male and female subjects tend not to think of other alternatives to solve problems. They only solve problems by memorizing formulas and steps [51]. This is relevant to the results of research which states that prospective teachers tend to solve problems procedurally without developing alternative solutions [46]. In the indicators relating among concepts, males can relate concepts because they are able to arrange networks or patterns of concepts that have been acquired [50]. Concepts are presented as vertices. The information that connects among concepts establishes a pattern of concept network. If a concept or vertex recalled, the connected vertex or concept will be easier to remember [52]. Recall is the process of remembering the concepts that have been structured in both knowledge and experience [53].

5. CONCLUSION

In general, both male and female prospective mathematics teachers bring up all four aspects of reflective thinking. However, males do reflective thinking more leverage than females. The difference lies in the aspects of techniques, insight, and conceptualization. Male prospective mathematics teachers prefer to employ the simplest way to solve problems. Furthermore, they have consistent problem-solving patterns and connected concepts. This is because biological factors, they have a bigger right hemisphere, on the one hand. On the other hand, females’ problem-solving patterns tend to fluctuate due to doubt and mathematical anxiety factors.

The difference in reflective thinking between male and female prospective mathematics teachers suspected due to the type of non-routine problem. Researchers recommend further researches employee another question type for instance HOTS problem types, open-ended problems, and application problems. Other research approaches need to be employed such as measuring reflective thinking between both in quantitative design.

AUTHORS’ CONTRIBUTIONS

All authors actively participate in exploring ideas, reviewing literature, collecting the data, analysing the data, and compiling all body articles.

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