How are Student’s Spatial Intelligence for Geometry Problem-Solving?

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ABSTRACT

The purpose of this study was to describe the problem-solving skills students viewed from spatial intelligence. Problem-solving skills are an important component that students must have to solve a problem appropriately. This study is a qualitative study in which the main instrument is the researcher itself. The subject selection technique in this study used purposive sampling. The research data were obtained from the test data description and interview results. Data analysis techniques used in data reduction, data presentation, and conclusion. The validity of the data is obtained through the validation and triangulation method. This study shows that students with high spatial intelligence can identify a given problem, create a plan to solve the problem, and implement a problem-solving plan. Students with intelligence can understand a given problem, make a problem-solving plan, but in implementation. It is still not appropriate. Students with low spatial intelligence cannot identify problems precisely and do not create a completion plan, resulting in not implementing a completion plan.

Keywords: Spatial intelligence, Geometry, Problem-solving ability.

1. INTRODUCTION

Mathematics is a science that is studied at every level of education [1]. Mathematics can also be a complex science, where there are standards of ability that students need to have in learning mathematics. Problem-solving is one of the standard processes in mathematics learning [2]. This statement implicitly explains that problem-solving skills are an important part of mathematical learning [3]. [4] States that solving mathematical problems is a basic ability that must be embedded in students. Problem-solving skills become an important aspect in students’

Table 1. Indicators of problem-solving

<table>
<thead>
<tr>
<th>No</th>
<th>Indicators</th>
<th>Activities</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Understanding The Problem</td>
<td>Students can identify what is known about the problem.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Students can identify what to look for.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Ignored things that were irrelevant to the problem.</td>
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<tr>
<td>2</td>
<td>Create a Completion Plan</td>
<td>Students can interpret problems in the form of mathematical symbols.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Students design problem-solving plans using mathematical formulas.</td>
</tr>
<tr>
<td>3</td>
<td>Implementing the Plan</td>
<td>Students begin to solve problems using the way they consider most appropriate.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Students can do the calculations precisely.</td>
</tr>
<tr>
<td>4</td>
<td>Summing Up the Answer</td>
<td>Students can interpret the answers obtained.</td>
</tr>
</tbody>
</table>
lives, especially in mathematics learning [5]. This ability includes reading and counting through specific procedures [6]. Solving is the ability to get the correct answers to unknown problems and synthesize knowledge from previous experience [7]. Problem-solving capabilities include the ability to understand problems, draw up plans, execute plans, and the ability to look back [8], [9]. Five stages must be taken in the process of problem-solving, among others reading and thinking, exploring and planning, choosing and strategy, finding answers, and reflecting and extending [10]. Indicators of problem-solving skills include applying problem-solving strategies outside or in mathematics; solve mathematical models and real problems; explain and interrogate the results; identify known, questionable, and adequate elements; create mathematical models [11]. The problem-solving indicator will be presented in table 1 below.

In the process of learning mathematics, there are several aspects learned. One such aspect is geometry. Geometry is a material that has always existed in mathematics because it has become an inseparable entity. Geometry helps to understand every shape in the real world [12]. However, geometry is also a difficult material for students to learn [13]. One of the important abilities in geometric problem solving is spatial intelligence [14] [15]. Students have quality spatial-visual intelligence by using their imagination to create creative and innovative thinking skills to solve geometric problems [16]. Spatial intelligence is the ability to mentally organize, understand, and visualize spatial relationships between objects [17]. In addition, spatial intelligence also plays an important role in various aspects, including math problem solving, geometric problem solving, and geometric reasoning [15]. There are five components of spatial intelligence: spatial perception, visualization, mental rotation, spatial relationships, and spatial orientation [18].

Identification needs to be done to find out how the geometry problem-solving capabilities. Teachers will find it easier to know how students understand a geometry concept when they solve geometry problems. The study used spatial intelligence to review students’ mistakes.

Identification of problem-solving of student geometry is required as a reference in choosing appropriate learning models and media based on the student’s spatial intelligence on geometric materials. Therefore, research is needed to find out how student problem solving is reviewed from spatial intelligence.

<table>
<thead>
<tr>
<th>Category</th>
<th>Spatial intelligence scores</th>
<th>Number of students</th>
</tr>
</thead>
<tbody>
<tr>
<td>High</td>
<td>X &gt; 57.864</td>
<td>14</td>
</tr>
<tr>
<td>Moderate</td>
<td>30.278 &lt; X ≤ 57.864</td>
<td>38</td>
</tr>
<tr>
<td>Low</td>
<td>X ≤ 30.278</td>
<td>17</td>
</tr>
<tr>
<td>Total</td>
<td></td>
<td>69</td>
</tr>
</tbody>
</table>

2.2. Subjects

The study used three subjects using high, medium, and low spatial intelligence levels. The subject is selected using purposive sampling techniques. Purposive sampling, also called assessment sampling, is a deliberate selection of samples due to the quality of the subject and chosen not random without the need for the underlying theories or some participants set [21]. The selection of subjects is based on the grades obtained from the student’s spatial intelligence test results. The study used averages and standard deviations to categorize students with high, moderate, and low spatial-visual intelligence. The category results are presented in Table 2 below.

In this study, a spatial intelligence test was conducted by testing 69 students then taken subjects with three high categories, three moderate categories, and three low categories but researchers only presented selected subjects who could represent them.

2.3. Instrument

The study used geometry problem-solving skills tests and structured interviews. The instruments of geometry problem solving and interviews are validated by three experts in mathematics, while four experts in psychology validate spatial intelligence test instruments. The validity used content validity to ensure that the operationalization is relevant to the content to be measured [22]. The math problems will be presented in Figure 1 below.
2.4. Data Collection and Analysis

The data collection techniques used in this study include spatial intelligence tests, geometry problem-solving tests, and structured interviews. In this study, spatial intelligence tests were used to categorize students' spatial intelligence based on the grades they had obtained, problem-solving geometry tests were used to explore students' problem-solving skills, and interviews were used for data triangulation. Data analysis techniques are used in data reduction, data presentation, and conclusion [23]. Triangulation conducted in this study is triangulation techniques by comparing the test results of students' problem-solving skills and interview results with students. The indicators to be used in this study will be presented in table 1. Indicators of problem-solving.

3. RESULTS

The results showed differences in geometry problem-solving skills between students with high, medium, and low spatial intelligence that will be described as follows.

3.1. Subject S-1

Based on figure 2, it is seen that the subject of S-1 can identify the problem of what is known by writing the volume of the bathtub by 315,000 cm$^3$, the length of the bathtub is 90 cm, the height of the bathtub is 70 cm then writes that above the bathtub is installed a water tap with a height of 10 cm right between point H and G. Subject S-1 is also able to identify what to look for and ignore irrelevant information to solve geometric problems. To dig deeper into the understanding of the problem given to the subject of S1, the researcher presents the following interview excerpt.

P : Explain what you know about it.
S-1 : It is known that a bathtub has a volume size of 315,000 cm$^3$, the length of the bathtub is 90 cm, the height of the bathtub is 70 cm. Above the bathtub will be installed a water tap with a height of 10 cm right in the middle of points H and G.

P : What is being asked?
S-1 : Tap distance to disposal.

Furthermore, when viewed from figure 2, the subject of S-1 can also make a plan that is then appropriately implemented. The subject of S-1 makes a plan by writing $V = p \times l \times t$ and implements the formula correctly. In the answer sheet of subject S-1, it can be known that to determine the distance of the water tap to the sewer, first look for the width of the bathtub. After the bathtub's width is obtained, the subject S-1 continues his work by writing the Pythagorean formula $KS = \sqrt{SJ^2 + JK^2}$. Then, do the calculation of the formula that has been written. The subject of the S-1 also involves drawing to make it easier to solve problems by depicting a triangle in the beam image illustration. To dig deeper into the plan and implementation that the subject of S-1 has corrected, the researcher conducts an interview and presents the following excerpts.

P : Can you create a mathematical model to solve the geometry problem?
S-1 : Yes, you can, sir.
P : Try explaining the mathematical model you created.
S-1 : I created a volume formula to find width because the width of the bathtub is not yet known.
P : Which bathtub width means which one?
S-1 : The BC sir.
P : Continue after you get wide from the bathtub. What is the next step?
S-1 : Determine the distance of the tap to the sewer.
P : How do you do that?
S-1 : It uses the Pythagorean formula.
P : Which Pythagorean formula?
S-1 : $KS = \sqrt{SJ^2 + JK^2}$
P : How much is SJ?
S-1 : 50 cm continues his JK 80 cm
P : It got from where
S-1 : SJ 50 cm because SJ = BC continues JK it from the height of the bathtub plus the
height of the faucet from the bathtub is 70 + 10 = 80

From the interview results, it can be known that the subject of S-1 makes a plan that is then implemented precisely through a straightforward calculation process. Subject S-1 explains that the use of volume formulas to determine the width. After determining the width, it can find the distance between the tap to the sewer by using the Pythagorean formula. Then the subject of S-1 also includes a conclusion to end the answer to the problem-solving geometry.

When viewed from the answer sheet and the results of the interview. The subject of S-1 can solve the problem. Even the subject of the S-1 creates the image in detail by creating a dotted line on the image.

3.2. Subject S-2

![Image](https://example.com/image.png)

Figure 3 Answer of sheet S-2

Based on figure 3, it appears that the subject of S-2 can identify the problem by writing down important information from the given problem. Subject S-2 writes \( V = 315,000 \text{ cm}^3, p = 90 \text{ cm}, t = 70 \text{ cm} \). However, there is precise writing where the subject S-2 writes, "P. water tap = 10 cm" It is certainly not appropriate considering that 10 cm should be the height of the water tap from the bathtub. The subject of S-2 also writes down a matter of geometry, namely the distance of taps and waterways. It shows a less clear question so that to dig into more in-depth information. Researchers conducted interviews on the subject S-2. Here is the interview excerpt.

P : Try explaining the formula you made?
S-2 : It is a volume formula for looking for width because the width of the bathtub is unknown, so it must be searched first.

P : Once the width of the bathtub has been obtained, what is the next step?
S-2 : Find the distance of the tap to the sewer.

P : What formula to find it?
S-2 : Pythagorean formula.

P : Which Pythagorean formula?
S-2 : \( PQ^2 = PX^2 + QX^2 \).

P : What is looking for a sloping side?
S-2 : Yes, sir.

P : On your answer sheet, you wrote that \( \sqrt{8900} = 94.3 \text{ cm} \). Is it like that?
S-2 : Yes, it is true.

From the results of interview excerpts, it can be known that the subject of S-2 can make a plan and implement it to solve geometry problems even though as the result, there are errors due to lack of understanding of concepts in mathematics. The concept error was identified when asked, "On your answer sheet, you wrote that \( \sqrt{8900} = 94.3 \text{ cm} \). Is it like that?" Then the subject of S-2 confirmed the answer.
When viewed from the answer sheet and the results of the interview. The subject of S-2 has used problem-solving indicators, although some steps are still not appropriate. The images created are also not precise enough to be involved in solving geometric problems.

### 3.3. Subject S-3

**Figure 4 Answer of sheet S-3.**

Based on figure 4, it appears that subject S-3 identifies the problem, but only a little information is passed in the answer sheet. The subject of S-3 only writes the volume: 315,000, then the length: 90, and the height: 70. Images made by the subject of S-3 also still do not indicate that the subject of S-3 understands the problem of geometry given. The subject of S-3 only draws a beam without any other information or other important information. To deepen the information, the researcher interviewed on the subject of S-3. Here are the interview excerpts.

| P | : | What do you know about this? |
| S-3 | : | volume 315,000, length 90, height 70 |
| P | : | Is that all? |
| S-3 | : | Yes sir |
| P | : | What is being asked about this? |
| S-3 | : | Long water tap. |
| P | : | Are you sure? |
| S-3 | : | That seems to be the case. |
| P | : | What makes you doubt? |
| S-3 | : | Because I do not understand this. |
| P | : | Can you create a mathematical formula to solve this problem? |
| S-3 | : | Cannot. |
| P | : | Why can’t you create a mathematical formula to solve this problem? |
| S-3 | : | Because I do not know how to do it. |
| P | : | Do you think this problem can be solved? |
| S-3 | : | Can. |
| P | : | Do you know the Pythagorean formula? |
| S-3 | : | I have forgotten. |

From the results of the interview, it can be known that the subject of S-3 can not work on geometry problems. When asked, "Are you able to solve this problem?" the subject of S-3 explained that he did not know how to solve the geometry problem. Then when asked the formula that will approximately be used to solve a given geometry problem, the subject S-3 states that he does not know. From this, researchers have an idea that the subject of S-3 can solve that is still lacking.

Furthermore, the subject of S-3 also does not make a plan in the form of a formula written on the answer sheet. This certainly raises questions for researchers. Does the subject of S-3 know how to solve a given geometry problem? To dig into more in-depth information, researchers conducted interviews on S-3 subjects. Here is an excerpt of the interview on the subject of S-3.

| P | : | Are you able to solve this problem? |
| S-3 | : | Not |
| P | : | Why? |
| S-3 | : | I do not know-how |
| P | : | What does this using formula? |
| S-3 | : | Do not know |
| P | : | You do not know at all how to solve this problem? |
| S-3 | : | Yes, I do not know. |

From the results of the interview, it can be known that the subject of S-3 cannot work on geometric problems. When asked, "Can you create a mathematical formula to solve this problem?" the subject of S-3 explained that he did not know how to solve the geometry problem. Then when asked the formula that will approximately be used to solve a given geometry problem, the subject S-3 states that he does not know. Then the subject S-3 is also unable to solve the problem of geometry. This is evidenced by the width of the answer that does not write formulas or do calculations to solve the geometry problem that has been given.

### 4. DISCUSSIONS

Based on the results of the description of the data that has been presented, it can be known that each subject has different levels of spatial intelligence has different geometric problem-solving abilities as well. Each subject writes down the completion steps, although the subjects S-1, S-2, and S-3 have different steps. Subjects S-1, S-2, and S-3 make a beam-shaped construction of information obtained to illustrate the problem then involves the image to solve the geometry problem. The subject of S-1 tends to describe a geometric problem solving into visual form well where every detail in the image is noticed, such as creating a dotted line that indicates that it is a line inside the beam. Spatial intelligence helps students to convert accepted material into writing or images. The subject of the S-2 also creates an image but still lacks detail because it should be made a separate line to indicate that the line is behind the side of the beam. For the subject S-3 also makes a beam but the information written is still very minimal. Students with high spatial intelligence have
better problem-solving skills than students with moderate and low intelligence, whereas students with moderate spatial intelligence have better math skills than students with low spatial intelligence [15].

From the interviews conducted by researchers to the subject S-2, ignorance of the concept of encouraging to make mistakes can be known. Problem-solving activities relate to the student experience [24] so that the things taught by the teacher are very important in the problem-solving process. Spatial intelligence correlates with students’ problem-solving abilities [25]. Students with low spatial intelligence cannot deform problems into geometric shapes. This is because transformation and skills are common mistakes students make due to the incomprehension of choosing the procedures to be used in problem-solving [26]. Students with low spatial intelligence tend to make more mistakes, including transformation, encoding, and process skills [27]. The following is an excerpt of an interview that researchers conducted on the subject S-3.

From the interview results, it can be known that the subject S-3 cannot answer the problem given because of the difficulty to identify what to look for, so that the following process is deadlocked.

5. CONCLUSION

Based on the discussion that has been presented, researchers concluded that all students solve geometry problems by constructing images. However, high spatial intelligence students tend to solve geometry problems by making more detailed image construction. Students with moderate spatial intelligence are constructing images, but the form of images that have been made is still not appropriate, which does not include the erased line behind the side of the beam. Students with low spatial intelligence try to solve geometry problems by constructing images but the information written is still not enough to represent the given problem. In the completion step, students with high spatial intelligence also make a plan that is then implemented to solve geometry problems, and calculations are done without difficulty. Students with moderate spatial alignment can also write a research plan, but the implementation is still not appropriate. Students with spatial intelligence are committing to such a problem caused by the misconceptions experienced. Students with low spatial intelligence could only write down a small amount of information given to the problem. Students with low spatial intelligence could also not solve geometry problems, not even knowing the plan to solve them. The results of this study can be used as a reference in subsequent research on the ability to solve geometric problems with different types of problems, such as HOTS or PISA like problems.

ACKNOWLEDGMENTS

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REFERENCES


