

# Comparative Analysis on Chinese and Canadian Primary School Mathematics Estimation Education Differences

Zhihuan Shao<sup>1,a</sup>

<sup>1</sup>University of Toronto, 27 King's College Cir, Toronto, ON M5S, Canada

<sup>a</sup>Corresponding author. Email: shaozohihuan 1997@gmail. com

## ABSTRACT

Mathematics is one of the most important topics in school and in the community in twenty-first century, a pupil who is good at mathematical seems to have the capacity to alter the progress of their very own state's financial, governmental, and social issues[1]. Estimation is regarded as among the top 3 objectives of teaching maths since it is "an action that pervades both kid's and grownups' lifestyles" [2], [3]. In concerns of shaping a student's ' attitudes regarding mathematics, caregivers play an essential part in the primary level[2]. The aim of this study is to look at mathematics estimation education differences in Canada and China in general to find out the differences between the two systems. This article analyses the national mathematics curriculum of obligatory schools for Canada and China for estimating opportunities for students, recognizing that the capacity to evaluate has significant implications both for subsequent mathematics learning and for real world functions. Framed by four modes of evaluation (number line, quantity, computation and, measurement) that are theoretically and technically distinct, each using mathematics differently [2]. Findings are that both countries' curriculum, especially those in Canada, provide students with ample and clear chances to acquire whatever kind of estimating abilities they may need. A comparison of the two educational methods also indicates that a hybrid of the two approaches should be explored in order to optimize students' results.

**Keywords:** Canada, China, estimation skill, primary math education

## 1. INTRODUCTION

Given the shift toward a global economy that is reliant on technological and digital innovations, it is becoming clearer that in order to succeed in future employment marketplaces, learners may require excellent math proficiency. Estimation is regarded as the math education's 3 primary objectives for the reason that it is "a popular habit in both kid's and seniors' everyday living." Nonetheless, despite its importance, estimate is often disputed. Comparing the mathematics curriculum to that of another nation or system is a good approach to learn more about it. Comparative studies are used to identify a curriculum's strengths and shortcomings. Mathematics is generally regarded a good subject for comparative study, since it is seen as a "widespread" subject that relies largely on logic and symbolic notation and is thus relatively language-independent and so easiest to compare. Various techniques are presently in use in different settings and

areas to encourage students to develop critical estimation mathematical skills.

The two groups of data collected are data on the contexts of the estimation mathematics system and curricula in both China and Canada. Information and data on estimation mathematics education system, and history of development of the two curricula were gathered through documents, and a review of the relevant literature. Observations into elements that impact learners' enthusiasm, conduct, and accomplishment in mathematics estimations may be gained through a detailed examination of these two educational settings. Furthermore, a contrast between the two instructional techniques shows that a blend of both the approaches should be explored in order to optimize learners' performance.

## 2. BACKGROUND

As per findings of a survey of pre-service elementary instructors' perspectives on estimations

taken in the U. S. four decades ago, the "cursory approach provided to estimating in most mathematics curriculum is inadequate to produce any meaningful estimation." According to a recent study, preservice teachers in the United States have weak estimating concepts at both the elementary and secondary levels. Estimation is a subject that is seldom covered in depth in textbooks all around the globe. Estimation may be used to evaluate the validity of survey responses in addition to selecting the best answer from a collection of choices. The ideal scenario is for pupils to grasp the approximate size of a solution so that they can immediately reconsider the problem if the answer they received was incorrect.

Chinese students often outperform their Canadian counterparts in international math examinations. Chinese teachers' capacity to communicate concepts in their courses in a flexible way is believed to be directly related to their students' mathematical performance, which is thought to be influenced by the country's mathematics curriculum and policies. The authors undertake a thorough review of relevant literature in order to examine this theoretical assumption and attempt to establish a link between Chinese students' mathematical performance and the factors that influence their capacity to succeed in mathematics. As a consequence of their results, the authors' review challenges this assumption and proposes research that may lead to a better understanding of the relationship between students' mathematics learning quality and their learning environments [4].

To inculcate the necessary mathematical abilities in learners, China is using an exam-oriented, and teacher-centred technique [5], while Canada supports a multi-assessment, and student-centred method, as seen by the techniques used in regions like in the Province of Ontario [2].

The Canadian education system is built around a modernist, student-centred approach to learning and teaching. A constructivist learning method challenges the notion that learning is communicated or supposed to be assimilated. In contrast, constructivist approach embraces the concept that students learn and construct knowledge. Mathematics education in China is predicated, and progresses via sequential and revolving levels. The foundation of China simple mathematics includes "figures and algebraic figures; spatial and geometrical figures; probability theory; linkages and formulation," as per the National mathematics this the curriculum guidelines for 9 years primary education [6].

### **3. LITERATURE REVIEW**

According to the study's results, the significance of estimation in children's arithmetic learning may be explained in two ways. The first is the developmental

function of the child in children's learning in a variety of mathematical disciplines as well as its ability to detect cognitive issues with student development from different math areas. The first is naturally psychological. Second, and more pragmatically, the next part addresses the importance of different types of estimations within different realistic conditions: These mentioned sections concentrates mainly on the first, but does not entirely ignore the second. According to Sowder's earlier research, estimating has historically been classified into three types: computational, measurement, and quantity (or numerosity) estimate, with the latter being the most frequent.

In the almost three decades thereafter, a fourth kind of estimate, number line estimating, has risen to the top of the research agendas of cognitive therapists, math teachers, and learning disabilities instructors from both China and Canada. As far as the scope of this study permits, the following section dives into the literature from Canadian and Chinese math estimation techniques, on these four types of estimates, their features, and their relevance to educational math [9].

#### **3.1. Estimation of Quantity**

The capacity to compute or construct the amount of items in a collection without having to count each is referred to as quantity estimation. It's inversely related to one's counting ability, and as the variety of elements on the panel increases, it gets less precise. There is a sophisticated interrelationship involving set size and maturity that advances with time when it comes to the improvement of quantitative estimation. Younger kid's estimations generally considered to transition from logarithmic to linear techniques, comparable with how they do with number line estimation, implying that they are more skilled with tiny numbers. Some studies think, however, that the logarithmic model for young children should be interpreted as two linear forms, one representing children's more accurate representation of tiny numbers and the other showing their inadequate understanding of big numbers. Many have already discovered also that these models apply to kid's estimations in continuous circumstances, while the logarithm major parameter is applicable in intermittent situations. Elementary kids' do their estimations in a normal manner, that would be, in the right way in comparison to existing backend, regardless of precision[6].

In addition, other findings showed that the influence of quantity estimate is intimately connected to the influence in integer linear programming estimations, and that these two skills are not only related, but also predict simple mathematical ability at the same level. The majority of number estimation studies has been done on adults, whose performance varies depending on the circumstance. Systematic dot designs provide

reasonable estimations as compared to ones, as well as grouped estimate amounts greater accurately than individual numbers [10].

### ***3.2. Estimation based on a number line***

Although ability to estimate values in number lines increases with age, young kids have a propensity to see large values as less widely spread than small numbers, resulting in a logarithmic pattern similar to quantity estimating. The use of reference points to improve numerical line estimation is critical for the development of mathematical skills in general, as well as the acquisition of arithmetical skills and the learning of fractions in particular. It also predicts children's algebraic aptitude and equation-solving skills, as well as mathematical learning difficulties, such as developmental dyscalculia. Furthermore, decimal number line estimation competence more closely predicts algebraic competency compared to both fraction number line and integer number line estimations' competence.

Intervention enhances number line estimation, especially when logarithmic patterns are substituted with linear patterns. On bounded tasks (they are usually ones in which an upper limit is put upon on a number-line to help with estimation) Kids make proportional judgement on number lines and magnitude-based judgments on unbounded tasks, with children utilizing proportional judgments on the former. Grown ups' number-line estimation test scores are not only inconsistent, but also task dependent. When it comes to high numbers, about one out of two individuals place almost 1,000,000 in the middle of one thousand and one billion, suggesting a population-wide lack of knowledge of enormous numbers[10], [11].

### ***3.3. Estimation of the Measurement***

Using various forms of mental reference to measure the subject in question, the measuring estimate is commonly used in "everyday situations when accurate calculations and measurements have the simple definition of being unnecessary and impossible contextually " according to the National Institute of Standards and Technology. The measurement is known as measuring without measuring instruments. In contrast, although grown-ups and kids are usually not very accurate in estimations, the measurement estimate is probably the most frequent method utilized in many areas, including science-based learning; such as technology and engineering. However, it is poorly taught when it comes to class mathematics, frequently due to a lack of confidence in the instructors. Finally, to highlight the meaning of the context, distance estimations are often shaped by time rather than the difference between places [10], [11].

In general, middle-school children are poor judges, but are more precise when utilizing substandard units instead of traditional measures. Moreover, while there is no indication of maturation over the same timeframe, youngsters are becoming increasingly capable of measuring things over the same period. In general, high-school pupils utilize a certain kind of individual reference framework while generating estimates. This is an aspect of a complicated interplay in between perspectives of students of their own physique as well as their own environment. According to a recent research, kids that utilize points of reference are more accurate than kids who do not utilize points of reference. Finally, the measurement estimate has proven to be related to better mathematical performance and is a popular method employed by experts working with mathematics every day [12].

### ***3.4. Estimation based on computation***

Estimation is frequently considered of as a tool to aid in the calculation of numbers, which is incorrect. Indeed, in contrast to other subjects, Sowder's renowned assessment focused nearly entirely on computational estimating's methods and objectives. "The procedures of clarifying the issue of mathematics by certain norms to have a math computations that are approximate as well as sufficient," "more crucial and pragmatic unlike precise estimation for several utilizations of maths," Computational estimation is delineated as "a method of easing the difficulties of mathematics through some rules and procedures that provide a numerical simulation which is equivalent and adequate." as it "needs less time and attention than accurate calculation and can therefore be used" It forecasts total mathematical skills and is a positive connection of one's opinion of one's own aptitude to mathematics. It is an expertise which builds on a broad range of tactics and depends on both the maturity of the estimator and the difficulty of the assignment, not least because it offers a variety of experiences supporting a wider array of suitable methods and the complexity of the assignment. The size of the numbers usually does not influence the calculational estimations of children as long as the activities remain within their arithmetical limits. They provide superior estimates when activities are conducted in a contextual and aesthetically attractive way than to convey them verbally. However, invitations to estimate may lead youth to get confused, partly due to instructional notions that answers to problems should be precise. As a consequence, youngsters may use standard algorithms mentally. Finally, the calculation skills of people are influenced by their concern about mathematics, their educational background and cultural background [12].

#### **4. DIFFERENCES IN EVALUATION AND EDUCATION BETWEEN CHINA AND CANADA**

Above-mentioned review of literature on the form and function of various kinds of estimates was presented for independent examination of the two national curricula, one in China and one in Canada, both developed in the 1980s. This section compares and contrasts these two curricula based on how likely they are to help children develop key skills [5], [8], [9]. Both China and Canada emphasize kids' skills for autonomous independent reasoning and problem solving, as outlined in Canada's mathematics teaching techniques and Confucius's teaching practices. Instructors' autonomy, program design, class capacities and style of teaching, and the direction of mathematics test and materials varies between Chinese and Canadian schools.

Firstly, the emphasis placed on estimations in the curriculums of the two countries was vastly different. Despite the fact that estimates play a role in children's learning in many different ways, the Chinese curriculum seems to be the most apparent reference to this function in children's learning, regardless of its numerous variations. While the Canadian curriculum is based almost exclusively on computation and measurement, it is clear that the expectations are overstated. As a consequence, there really was no evidence of systematic requirements in terms of quantity estimations or line numbers in any of the two curricula [1].

For the second occasion, the Chinese materials have little to contribute in terms of computational estimates, apart from its implicit function in the expectation of critical thinking and assessment. In addition, the Canadian curriculum stipulates that computational estimates be provided for "difficult practical circumstances" and "everyday conditions," respectively, when dealing with "difficult practical circumstances." Both of these methods of justifying computations, although in distinct ways, are used to validate calculations produced in other ways. In contrast to the Canadian curriculum, which motivates kids more on "reflecting as well as assessing the rationality of tougher arithmetics and estimations, in daily events," Additionally none of the two curriculums contains anything other than the implied notion that computational estimates may require "less time and attention than accurate calculations and, as a result, may helpful in situations in which resources and time of attention have a constraint." A further point to note is that, with the exception of the Chinese invocation, there were no assumptions regarding the manner by which computation estimates could be done in any curriculum that was found. In addition, none of the curriculum materials, including but not limited to the different non-statutory recommendations, gave any clear evidence that

the computation estimation abilities were engaged in the future development of mathematical skills, whether in specific areas, mathematics in general, or problem-solving skills and techniques. If there were any expectations of this kind, they were kept under wraps [2], [5].

Thirdly, measurement assessments were often concentrated on timeliness in both settings and the visible attributes of things provided in expectation patterns that signal progress of development, was the common thread in both Canadian and Chinese curricula. Although it is impractical to expect teachers to be aware of the implications of poor measuring and estimating abilities, It will not be illogical to anticipate that instructional assistance aids would do so. Nonetheless, it might be argued that the Canadian system failed to promote research material warning teachers that overestimation of time and time accuracy in children with arithmetic learning difficulties tends to be an indicator for math competencies in the first instance. To put it another way, including query justifications and evidence of the expected competence's significance in curricular support materials may be helpful, at least in terms of measurement estimates [2], [4], [5], [6].

Lastly, both curricula are severely lacking in quantitative estimation, while the latter is only marginally present in Chinese education owing to its relationship to subitise (assumptions about quantities and numbers). They seem to be misleading, not least since the capacity to count is inversely related to the ability to reason and is a predictor of future arithmetical competence. A mathematical estimation of the number lines is successfully integrated into the curriculum of both countries. Although this omission seems to be disappointing, it should be noted that the estimated number-lines are the best predictors of future arithmetic and mathematics learning difficulties.

Finally, the one common thread running across both curriculums is the usage of un-standardize units in measurement estimates, that have been proven in studies to serve as a solid foundation for future conceptual and procedural abilities. However, whereas the Canadian curricula clearly connected non-standard units with estimates, the Chinese curricula promoted the wide use of non-standard units while providing little guidance on how to make estimates. To put it another way, the degree to which non-standard units are anticipated to become evident in child evaluation is not only variable, but also unpredictable.

#### **5. CONCLUSION**

Estimation can assist in determining the proper answer from a set of alternatives and determining the reasonableness of responses. Kids should have a concept of the approximate magnitude of a solution in

order to rethink the issue quickly if they discover that the result they received is wrong. The study concludes that there are several kinds of estimates used in mathematics: numerical estimates, measured estimates, observational estimates, and computational estimates .

To summarize, both countries' curriculum, especially those in Canada, provide students with ample and clear chances to acquire whatever kind of estimating abilities they may need. It also aligns with Canada and China's expectations for Smart's historical perspective on number evaluation and the use of quantities to calculate and measure them. It is past math, not math that does not accept the two main kinds of estimates, namely numbers estimate and quantity estimates, both curricula have a significant effect on the subsequent learning of other areas of mathematics and science. The use of computational estimate as a means of verifying computations is emphasized in Canadian curriculum whereas Chinese primary school has rounding, and there is only simple number calculation, but has lesser emphasis on estimation.

The following statements demonstrate this emphasis: 'Use estimation to check solutions to computations and decide an appropriate degree of accuracy in the context of an issue,' according to Canadian kids. In worldwide comparisons of estimation mathematics ability at both the elementary and secondary school levels, Chinese students have regularly outperformed Canadian students.

Chinese-speaking children perform better on number line estimate and mathematics generally than Canadian children and other children worldwide (as shown in the figure 1 below), supporting the concept that languages with a straightforward counting system enhance the acquisition of numerical understanding.

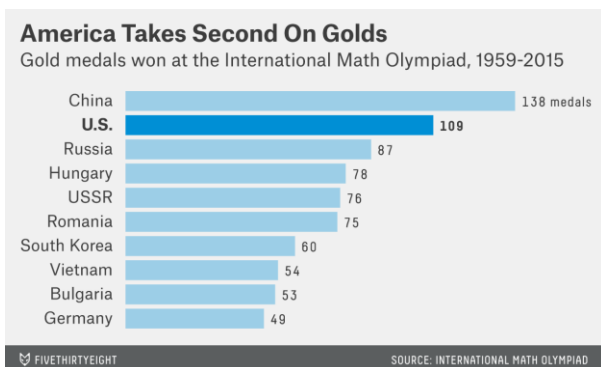


Figure 1. America takes second on golds.

In Chinese curriculum, measuring estimate was a popular theme, usually concentrating on the physical characteristics of things. Expectations about length and area, for example, were consistent across courses, while other characteristics were estimated differently. Consequently, majority of researcher believe that it is beneficial for both countries to introduce and complete

curriculum-supporting documentation that explains and illustrates the various assessment methods in order to help teachers understand why some of these assessment methods are important for curriculum and further learning as well as for the operation of real-world systems.

## ACKNOWLEDGMENTS

Sincere gratitude to all those who contributed directly or indirectly towards the successful completion of this study. Moreover, it is indeed an honour to have taken this step in my academic venture, and it is only fair that the least I can do is to recognize them. First, I thank, my parents for giving me this opportunity, and providing support and endless understanding during the whole period of the study. Second, I am most humble to express my feelings of in-debt to number of persons of good-will both individually and collectively for their contribution towards this report. I wish to thank my dedicated professor for the commitment and guidance in the development of this paper. Lastly, I would like to express my sincere appreciation to my friends for their motivation and faith that was sufficient all through. Thank you.

## REFERENCES

- [1] D. Jarvis. Messy but meaningful: exploring the transition to reform-based pedagogy with teachers of mathematics and coordinators in Ontario, Canada. *Teacher Development*, 2016, 20(1). Doi: 10.1080/13664530.2015.1108928.
- [2] A. Hargreaves. Large-scale assessments and their effects: The case of mid-stakes tests in Ontario. *Journal of Educational Change*, 2020, 21(3). Doi: 10.1007/s10833-020-09380-5.
- [3] K. Yaro, E. Amoah, and D. Wagner. Situated Perspectives on Creating Mathematics Tasks for Peace and Sustainability. *Canadian Journal of Science, Mathematics and Technology Education*, 2020, 20(2). Doi: 10.1007/s42330-020-00083-w.
- [4] J. Rasmussen and M. Bayer. Comparative study of teaching content in teacher education programmes in Canada, Denmark, Finland and Singapore. *Journal of Curriculum Studies*, 2014, 46(6). Doi: 10.1080/00220272.2014.927530.
- [5] M. Finlayson. Addressing math anxiety in the classroom. *Improving Schools*, 2014, 17(1). Doi: 10.1177/1365480214521457.
- [6] A. Peng and L. Cao. How Chinese Teach Mathematics: Canadian Teachers' Perspectives. *Frontiers of Education in China*, 2021, 16(1). Doi: 10.1007/s11516-021-0002-7.

- [7] Q. Li and Y. J. Ni. Debates on the basic education curriculum reform and teachers' challenges in China. *Chinese Education and Society*, 2012, 45(4). Doi: 10.2753/CED1061-1932450401.
- [8] X. Fan, W. Li, Z. Wang, Y. Sun, and L. Su. The analysis of higher mathematics teaching strategy based on the innovative teaching mode. *Advances in Intelligent Systems and Computing*, 2021(1195), AISC. Doi: 10.1007/978-3-030-50399-4\_33.
- [9] H. Hanna. Handbook of education in China. *Compare: A Journal of Comparative and International Education*, 2018. Doi: 10.1080/03057925.2018.1451136.
- [10] Y. P. Ma, C. C. Lam, and N. Y. Wong. Chinese primary school mathematics teachers working in a centralised curriculum system: A case study of two primary schools in North-East China. *Compare*, 2006, 36(2). Doi: 10.1080/03057920600741206.
- [11] W. Lei et al., "Contract teachers and student achievement in rural China: evidence from class fixed effects," *Australian Journal of Agricultural and Resource Economics*, 2018, 62(2). Doi: 10.1111/1467-8489.12250.
- [12] R. Marks. Transforming mathematics instruction: multiple approaches and practices. *Research in Mathematics Education*, 2016, 18(2). Doi: 10.1080/14794802.2016.1164070.