

The Calculation of Product Combination by Using Linear Programming Simplex Method to Profit Maximize at Roti Sahabat Palembang City

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ABSTRACT

This research discussed about the calculation of product combinations by using a linear program simplex method to calculate product combinations maximize profits at Roti Sahabat. The data for the preparation of this research was obtained through interviews with business owners to obtain primary data. Product of Roti Sahabat was located in Palembang City such as Pia bread and sponge bread which price of them IDR 900 per pack. Roti Sahabat produces 24,000 pia bread and 28,800 sponge bread in every month. The production volume is only calculated based on customer demand. To calculate product combination research used the maximum simplex method of linear programming and obtained 0 combinations of pia bread and 62,207 for sponge roti, with profit of 30,109,768.2 for a month. The income earned before and after by using the maximum method was very different. Therefore the research has suggestion that Roti Sahabat must use product combination first to calculate the profit.

Keywords : *Product Combination, Program Linear, Maximum Simplex Method*

1. INTRODUCTION

Development is growing and more people have decided to become entrepreneurs, either by buying a brand or creating as a personal business in form of service or goods. In addition, the opportunity to market products through social media is now wider, making it easier for the public to present their business. Many of UMKM in the communities will make Indonesian people further advance rather than always relying on work prepared by government. Job opportunities that government prepared were shrinking day by day. In this case, the people can realize the revival of government that goal of Indonesian national income is through from entrepreneur.

Currently, many of business was moving in their production basic needs. One of them is in field food or cooking production. Because of production is a small form of business so the risk will have small too and its often easy to expand quickly. Basic food needs were basic needs for everyone. Production is all activities that created to increase in use of goods or services. In economics the elements of production activities are needed of land labor and skills. Production

of activities are the pioneers of the company, because the company can carry out all the activities within company through production product such as promotional activities, distribution of goods or services and making processes[1]. Through these productive activities company which can make customer satisfy needs and fulfill market needs.

Roti Sahabat Palembang city is a bakery company that was founded in 2001 and located on Jalan Tunas Harapan Lorong Mawar RT. 10 RW.06 Sako district Sukamaju Palembang. Based on the result interview with the owner Roti Sahabat, they did not account how many production product by detail to achieve level of profit, nor they calculated production cost in detail. Therefore the management of a company must be able to decide how to use resources to obtain the highest production volume, so if the product was sold, it will definitely get a lot of sale and get profit.

In the linear model program, there are two functions, namely the objective function and the constraint function. The objective function is a function that describes the goals or objective in linear problem programming which related to resources optimization management

[2]. The constraint function is the resource with the higher benefit or lower cost. When modelling had a purpose to be achieved in a linear mathematical function.

Based on the data from this research was obtained in last two years such as the output (volume), product sale and price of Roti Sahabat Palembang.

Table 1. Estimated Average Production Cost, Production Volume, Total Sale Revenue and Profit Pia Bread Each Years 2018 till 2020

Year	Production Cost	Production Volume	Sales Volume	Total Sales Revenue
2018	Rp 158.112.000	345.600	344.500	Rp 311.040.000.
2019	Rp 131.328.000	259.200	258.000	Rp 233.280.000.
2020	Rp 103.968.000	216.000	214.300	Rp 194.400.000.

Source: Roti Sahabat, 2021

Table 1. showed estimated cost for making pia bread at least 3 years anyway, and there is also a table estimated cost of sponge (bolu) cake for last 3 years also.

Table 2. Estimated Average Production Cost, Production Volume, Total Sale Revenue and Profit Sponge (Bolu) cake Each Years 2018 till 2020

Year	Production Cost	Production Volume	Sales Volume	Total Sales Revenue
2018	Rp 158.112.000	345.600	344.500	Rp 311.040.000.
2019	Rp 131.328.000	259.200	258.000	Rp 233.280.000.
2020	Rp 103.968.000	216.000	214.300	Rp 194.400.000.

Sources: Roti Sahabat, 2021

As can be seen from the table above, we know the production and sale of profit from Roti Sahabat must be achieved, how to avoid losses and how to plan for the future profitability of the company, so it will prevent the company from experiencing a decline in profitability as it is today. According to the combination of linear production program to increase the profit or to find out decrease in profits therefore doesn't make the store lose. The title of this research is Calculation of Combination Product By Using Linear Programming Simplex Method to Profit Maximize At Roti Sahabat Palembang.

2. LITERATURE REVIEW

2.1. Product Definition

Product is the result of production activities carried out by producers to satisfy needs and desires of consumers. Products sold by consumers must be good quality, affordable, easy to obtain and involved in promotional activities, so that consumers can be interested in buying the company's product. Products can be sold in large quantities will provide income and make profit for the company. [3] states that a product is anything that can be offered to a market for attention, acquisition, use and consumption that can satisfy a want or need. Products are more than just things that can be measured. Products include physical goods, services, people, organizations, ideas or combination of these.

2.2. Production Combination

Product can be produced in various ways and technologies, although there are many production processes, they can be broadly divided into two categories, namely: companies are organizations whose activities are producing. Production activities are activities that change the form of raw materials into final products (goods and services) [8]. Companies need raw materials, machine tools and labor. The company cannot be separated from its production and operation functions because one of the company's tasks is to produce goods and services. The company by raw and auxiliary materials and processes them manually into final products.

According to [4] combination of product is a comparison of the amount between one product and another that must be produced within a certain period in order to obtain optimal income. Product combination problems occur in companies that produce more than one product. The problem is how to determine the quantity of each product and what type of product will be produced so that the company can take advantage of existing resources and get as much profit as possible. Therefore, it can be concluded that product mix is a way of determining the amount of various products produced by using production factors such as machinery, labor and raw materials. The company must be able to determine

the number and type of product to be produced firmly in order to obtain the best results. The number of types of products to be produced must be determined by calculating the cost and value of the product itself based on the ability of business resources to determine the best product combination for the highest profit.

2.3. Linear Programming

According to sweeney and colleagues in his book “introduction and Management Science” linear programming is a mathematical technique develop to assist a manager for making decisions. As [5] linear programming (LP) is used to solve problems that require solving in the process or maximally or minimally by using mathematic techniques in the form of linear inequalities. Based on the linear programming theory above, it can be concluded that linear programming is a technology that solves problems in a maximum or minimum process to help companies. Linear programming the mathematical modality of product combination problems can be described in the form of a linear curve (straight line). The implication of the linear nature requires proportionality and additivity.

2.4. Simplex Method

The simplex method is the process of repeating system procedures (literacy) until desired results is achieved. Therefore, this method replaces difficult question with a series of simple questions. According to [6] the simplex method is one of the solutions of linear programming which the process of finding a solution is using the literacy path, namely determining feasible point of the goal to be achieved with the help of table until the optimal solution is obtained.

Table 3. Initial Simplex Table

asis	X ₁	X ₂	S ₁	S ₂	S _n	olusi
Z	-C ₁	-C ₂	0 ₁	0 ₂	0 ₃	0
S ₁	a ₁₁	a ₁₂	1	0	0	b ₁
S ₂	a ₂₁	a ₂₂	0	1	0	b ₂
...
S _n	a _{m1}	a _{mn}	1	b _m

Source: Zuhria Nasution, 2016

Information: Z = the objective function to be searched for the maximum or minimum value

C_n = Coefficient value of the objective decision variable X_n

X_n = nth decision variable

S_n = nth slack variable

A (mn) = resource request for every X_n m

B_m = number of resource provide

n = number of decision variables starting from 1,2,3...n

m = number of types of resource used

starting from 1,2,3, m

teh objectives of fuctions a follows:

$$\text{maximize } Z = X_1 C_1 + X_2 C_2 + S_1 0 + S_2 0 + S_3 0$$

$$\text{with limited : } a_{11} C_1 + a_{12} C_2 + 1 0_1 + 0 0_2 + 0 0_3 = b_1$$

$$a_{21} C_1 + a_{22} C_2 + 0 0_1 + 1 0_2 + 0 0_3 = b_2$$

3. ANALYSIS

3.1. Calculation of the Optimal Production Result Combination

Calculation of the optimal combination production results in Roti Sahabat using linear program analysis tool, with the maximum simplex method. From calculation above, several functions are obtained to determine the optimal production area, including

1. Purpose Function

Based on the previous calculation of the contribution margin, the objective function is

$$\text{Max } z = 321.03 x + 484.03 y$$

2. Limit Function

$$\text{Raw Material} = 503 x + 340 y \leq 21.864.00$$

$$\text{Machine Capacity} = 0,2 x + 0,15 y \leq 9.120$$

$$\text{Labor} = 0,006 x + 0,0083 y \leq 52.800$$

$$\text{Working capital} = 578,97 x + 415,97 y \leq 25.876.000$$

To create a matrix table in calculating the combination of production results using the maximum simplex method linear program. The following things need to be done before entering the value of the objective functions and limit function into the table as follows:

1. Changing the objective function, the variables that are to the right of the equation sign are moved to the left. So that, the form of the equation becomes:

$$Z = 321,03 x + 484,03 y$$

$$Z - 321,03 x - 484,03 y = 0$$

2. Change the shape of boundary function from the inequality (\leq) into equation ($=$) by adding slack elements of variables S₁, S₂, S₃ and S₄ so that the boundary function becomes

$$503 x + 340 y + 1 S_1 + 0 S_2 + 0 S_3 + 0 S_4 = 21.864.000$$

$$0,22 x + 0,13 y + 0 S_1 + 1 S_2 + 0 S_3 + 0 S_4 = 9.120$$

$$0,006 x + 0,0083 y + 0 S_1 + 0 S_2 + 1 S_3 + 0 S_4 = 52.800$$

$$578,97 x + 415,97 y + 0 S_1 + 0 S_2 + 0 S_3 + 1 S_4 = 25.876.000$$

where $x \leq 0$ and $y \leq 0$

After making these two changes, the objective and constraint function variables can be entered into the first simplex table as follows:

Table 4. First table Simpleks

Basic	X	Y	S1	S2	S3	S4	RHS/Solution
Z	-321,03	-484,03	0	0	0	0	0
S1	503	340	1	0	0	0	21.864.000/340 = 64.305,8824
S2	0,22	0,13	0	1	0	0	9.120/0,13 = 70.153,85
S3	0,006	0,0083	0	0	1	0	52.800/0,0083 = 6.361.445,78
S4	578,97	415,97	0	0	0	1	25.876.000/415,97 = 62.206,4091 Pivot Row

Source : processed data, 2021

Account and fulfill the table of second simpleks with do two ways:

$$\begin{array}{r}
 \text{Old Z} \quad (-321,03 \quad -484,03 \quad 0 \quad 0 \quad 0 \quad 0 \mid 0) \\
 (-484,03) \times \text{NPR} \quad (-673,6971 \quad -484,03 \quad 0 \quad 0 \quad 0 \quad -1,161672 \mid -30.109.768,2) - \\
 \hline
 \text{New Z} \quad (352,6671 \quad 0 \quad 0 \quad 0 \quad 0 \quad 1,161672 \mid 30.109.768,2)
 \end{array}$$

$$\begin{array}{r}
 \text{Old S1} \quad (503 \quad 340 \quad 1 \quad 0 \quad 0 \quad 0 \mid 21.864.000) \\
 (340) \times \text{NPR} \quad (473,229 \quad 340 \quad 0 \quad 0 \quad 0 \quad 0,816 \mid 21.150.179,1) - \\
 \hline
 \text{New S1} \quad (229,771 \quad 0 \quad 1 \quad 0 \quad 0 \quad -0,816 \mid 713.820,9)
 \end{array}$$

$$\begin{array}{r}
 \text{Old S2} \quad (0,22 \quad 0,13 \quad 0 \quad 1 \quad 0 \quad 0 \mid 9.120) \\
 (0,13) \times \text{NPR} \quad (0,1809 \quad 0,13 \quad 0 \quad 0 \quad 0 \quad 0,000312 \mid 8.086,8331) - \\
 \hline
 \text{New S2} \quad (0,0391 \quad 0 \quad 0 \quad 1 \quad 0 \quad -0,000312 \mid 1.003,1669)
 \end{array}$$

$$\begin{array}{r}
 \text{Old S3} \quad (0,006 \quad 0,0083 \quad 0 \quad 0 \quad 1 \quad 0 \mid 52.800) \\
 (0,0083) \times \text{NPR} \quad (0,01155 \quad 0,0083 \quad 0 \quad 0 \quad 0 \quad 1,992 \mid 516,3131) - \\
 \hline
 \text{New S3} \quad (-0,00555 \quad 0 \quad 0 \quad 0 \quad 1 \quad -1,992 \mid 52.283,6869)
 \end{array}$$

Pivot Row or S4 change by Y cause of pivot column, Y value have negative higher, so that NPR more value for Y

Table 5. Second table Simpleks

Basic	X	Y	S1	S2	S3	S4	RHS/Solution
Z	352,6671	0	0	0	0	1,161672	30.109.768,2
S1	229,771	0	1	0	0	-0,816	713.820,9
S2	0,0391	0	0	1	0	-0,000312	1.003,1669
S3	-0,00555	0	0	0	1	-1,992	52.283,6869
Y	1,39185	1	0	0	0	0,0024	62.206,4091

Source : processed data, 2021

From the results of the calculation of the linear analysis of the maximum simplex method program in the second simplex table, it can be seen that all numbers on the Z line are positive [9]. This means that the second simplex table are optimal and showed the combination of production of x (Pia bread) an y (sponge bread). The RHS / solution table describes the amount of production produced by Roti Sahabat with each amount as follow

$$\begin{array}{r}
 X \text{ (Roti Pia)} \quad = 0 \text{ unit} \\
 Y \text{ (Roti Bolu)} \quad = 62.206,4091 \text{ unit} \\
 \text{Pia bread (x) has a value of 0, because in the second} \\
 \text{simplex table, row of Z there are no more negative} \\
 \text{number, so there is no need to calculated the third} \\
 \text{simplex table which to find the value of X. The positive} \\
 \text{X value is 0}
 \end{array}$$

The advantage obtained by Roti Sahabat use the optimal production combination above are:

$$\begin{aligned}
 Z &= 321,03 x + 484,03 y \\
 Z &= 321,03 (0) + 484,03 (62.206,4091) \\
 Z &= 0 + 30.109.768,2 \\
 Z &= 30.109.768,2
 \end{aligned}$$

3.2. Comparison of Product Combination and Production Profits Real with Product Combinations and production Advantages Simplex maximum Method

From the calculation results above, we can compare the number of combination of real products with results of simplex calculation or compared real profits with the results of simplex calculation. For comparison the following table lists the real situation and simplex calculations.

Table 6. Comparison of real product and product combinationsion Simpleks Methode

Product Combination	Production cost		Production Volume		Profit
	Roti Pia	Roti Bolu	Roti Pia	Roti Bolu	
Real	Rp 12.072.000	Rp 9.792.000	24.000	28.800	Rp 21.644.784
Simplex Method	-	Rp 21.864.000	-	62.207	Rp 30.109.768,2

Source : processed data, 2021

From the data above, it can be explained that in real conditions the combination of Roti Pia and Sponge bread are 24.000 and 28.800 respectively and the monthly profit is idr.21.644.784. however the owner of Roti Sahabat used combination of product by calculated the maximum simplex method. The maximum profit obtained is idr. 30.109.768.2 in a month, where Roti Sahabat does not produce Pia bread and produces 62.206.4091 units or 62.207 units of sponge bread in a month. If used daily the maximum output of Sponge Bread after use the simplex method.

4. CONCLUSION

The results of this reseach and analysis based on the datas described in chapter III as follows

1. The combination of Roti Sahabat products calculated using the maximum simplex method. Linear program from Roti Sahabat only produces Sponge Bread and doesnot Pia Bread. The number of sponge bread must be produced at 62.207.4091 or 62.207 per month, or in a day Sponge bread should produce around 2.592 for maximum profit takes.
2. The maximum profit that can be achieved by Roti Sahabat (Calculated using the maximum simplex method linear program) was idr 30.109.768.2 in a month. This calculated is much higher than the monthly profit obtained by Roti Sahaba. Which was previously calculated based on manual calculations by deduction the entry of spending money. The current profit of Roti Sahabat is only idr. 21644.482 per month

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