



Analysis of the State-of-art Portfolio Theory

Zheng Ying

School of Mathematics and Physics, Xi'an Jiaotong-liverpool University, Suzhou, 215000,
China

zheng.ying20@student.xjtlu.edu.cn

Abstract. Portfolio theory is a fundamental concept in investment management that aims to optimize risk and return by diversifying investments across different assets. This study explores portfolio theory, including its key concepts and methodologies, such as mean-variance optimization and alternative strategies like Risk Parity and factor-based allocation. This study highlights the importance of portfolio diversification and asset allocation in achieving optimal risk-return trade-offs. The Markowitz mean-variance optimization approach provides a foundation for constructing efficient portfolios. Alternative strategies like Risk Parity and factor-based allocation offer additional perspectives for balancing risk contributions and capturing systematic risk factors. However, the limitations of these approaches, e.g., reliance on historical data and modeling assumptions, should be considered. This study provides insights into portfolio theory, empowering investors to make informed decisions when constructing investment portfolios. By understanding the principles of diversification and asset allocation, investors can effectively manage risk and optimize returns. These results contribute to the ongoing development of investment management practices, encouraging further research and innovation in portfolio construction methodologies and risk management techniques. The research's significance lies in its practical application for individuals and institutional investors seeking to maximize their investment outcomes while effectively managing risk.

Keywords: Portfolio theory, asset allocation, risk-return trade-off.

1 Introduction

Portfolio theory has a rich research history, and its significance lies in its ability to guide investment decisions, manage risks, and optimize portfolio performance. It emphasizes how crucial diversification is and how building a portfolio involves balancing risk and return. The seminal paper by Harry Markowitz introduced Modern Portfolio Theory (MPT) laid the foundation for quantitative portfolio [1]. William Sharpe introduced the Capital Asset Pricing Model (CAPM), which revolutionized the understanding of asset pricing and market equilibrium. CAPM provided a framework for assessing systematic risk and determining expected returns [2]. Another study introduces the Fama-French three-factor model. It expanded the CAPM by incorporating additional risk factors, namely size and book-to-market ratio, to explain stock

returns [3]. Recent research has focused on various aspects of portfolio construction and performance. The study examines the persistence of mutual fund performance using robust portfolio optimization techniques. It investigates the mutual fund performance's short-term durability in the major European markets from January 1990 to December 2022. [4]. The research explores portfolio choice with high-dimensional state variables using deep learning techniques. The study demonstrates the potential of deep learning models in improving portfolio performance and risk management [5]. Moreover, the article discusses factor investing and its application in portfolio optimization. It highlights the benefits of incorporating factor-based strategies in portfolio construction to capture risk premia across different asset classes [6].

The motivation behind this study is to investigate the current state of portfolio theory, considering recent developments and performance trends. The aim is to provide an updated understanding of portfolio construction and management in light of evolving market dynamics and advancements in research methodologies. the motivation to study asset allocation and portfolio optimization stems from the desire to enhance investment outcomes, achieve optimal risk-return profiles, and adapt to the changing dynamics of the financial markets. By employing effective asset allocation strategies and utilizing advanced portfolio optimization methods, investors can strive to build robust portfolios that align with their financial goals and withstand market uncertainties. Continued research and exploration in this field hold the potential to unlock new insights and strategies that can further improve investment decision-making processes and generate superior risk-adjusted returns.

In the following paper, it will introduce some commonly used optimal methods for asset allocation and portfolio. Define asset allocation and its significance in portfolio management. Explain the concept of portfolio optimization and its goal of achieving an optimal risk-return tradeoff. Talk about how asset allocation is the main factor influencing the performance of a portfolio. Describe the idea of optimal portfolio methods and how portfolio construction uses them. Analyze the limitations of the current approaches in asset allocation and portfolio optimization. Discuss potential future developments and advancements in the field, such as incorporating machine learning or alternative data sources.

2 Basic Descriptions

Asset allocation and portfolio management are essential components of investment strategies aimed at achieving optimal risk-return profiles. This section provides a basic description of asset allocation and portfolio optimization, along with an overview of commonly used optimal method. Asset allocation is the process of dividing an investment portfolio among various asset classes, including cash, bonds, stocks, and alternative investments. Creating a diversified portfolio that strikes a balance between risk and return based on an investor's time horizon, risk tolerance, and goals is the aim of asset allocation. By distributing investments among various asset classes, investors can potentially reduce the impact of individual security or sector-specific risks on their overall portfolio performance. Portfolio optimization, on the other hand,

involves constructing an optimal portfolio by selecting the most favorable combination of assets. The goal of portfolio optimization is to maximize returns or minimize risk, taking into account the investor's preferences and constraints. This process typically involves identifying the optimal asset allocation weights, considering factors such as historical returns, volatilities, correlations, and risk-adjusted performance measures. Several optimal methods are commonly used in asset allocation and portfolio optimization. These methods aim to provide efficient and effective portfolio construction strategies. The modern portfolio theory (MPT) brought about a complete transformation in portfolio management. The core tenet of MPT is that investors can construct portfolios that offer the lowest risk at a given expected return level or the highest expected return at a given risk level. By considering the trade-off between return and risk, MPT emphasizes the importance of diversification and the benefits of combining assets with low or negative correlations [7]. The Capital Asset Pricing Model (CAPM), a popular framework for asset pricing and portfolio optimization, is covered in another article. CAPM estimates the expected returns of assets based on their systematic risk, as measured by beta. It suggests that investors allocate their funds among different securities based on the risk-free rate, market risk premium, and beta in order to achieve a market equilibrium [8].

In addition to these foundational methods, there are some other commonly used optimal techniques:

- **Mean-Variance Optimization (MVO):** Based on the mean and variance of asset returns, this method seeks to determine the portfolio allocation that offers the highest expected return for a given level of risk or the lowest risk for a given level of expected return.
- **Risk Parity:** This approach focuses on allocating investments based on risk contributions rather than market values. It seeks to balance risk across different asset classes by assigning weights that equalize their contribution to the overall portfolio risk.
- **Black-Litterman Model:** This model determines the ideal portfolio allocation by fusing the perspectives of investors with the presumptions of market equilibrium. It incorporates subjective views on expected returns and adjusts them based on market expectations and risk profiles.
- **Factor-Based Investing:** This strategy involves allocating investments based on specific risk factors, such as value, growth, momentum, or quality. It aims to capture the risk premiums associated with these factors and construct portfolios that offer enhanced risk-adjusted returns.

To sum up, portfolio optimization and asset allocation are key ideas in investment management. Investors may enhance risk-adjusted returns and accomplish their financial goals by diversifying across asset classes and employing the best strategies. The modern portfolio theory, CAPM, mean-variance optimization, risk parity, the Black-Litterman model, and factor-based investing are among the commonly used methods that provide frameworks for constructing optimal portfolios. These methods continue to evolve, incorporating advancements in quantitative techniques and incorporating

new factors, offering investors a broader toolkit for portfolio construction and management.

3 Modern Portfolio Theory

The foundational framework for portfolio management known as Modern Portfolio Theory (MPT) offers a methodical way to build investment portfolios that are effective. MPT was developed in 1952 by Harry Markowitz and heavily emphasizes the trade-off and the diversification between risk and return. This section will provide a detailed explanation of MPT. The foundation of MPT is the idea that investors are mainly interested in the risk and return aspects of their portfolios. Whereas return is a measure of the possible gains or losses, risk is determined by the volatility or standard deviation of an asset's returns. Finding the ideal portfolio that minimizes risk for a target level of returns or maximizes returns is the aim of MPT.

According to MPT, investors can diversify their holdings across a range of asset classes with little to no correlation in order to create optimal portfolios. By combining assets that do not move in perfect synchronization, the overall portfolio's risk can be reduced without sacrificing potential returns. This concept is illustrated by the efficient frontier, which displays the set of portfolios that offer the highest expected returns for each level of risk or the lowest risk for each level of expected returns [9]. To find the best asset allocation, MVO takes into account the variances (or standard deviations) and expected returns of the assets. Finding the allocation that minimizes risk for a target level of returns or maximizes returns for a given level of risk is the goal [10]. It's crucial to remember that, despite offering a useful framework for portfolio construction, MPT has faced criticism and changed over time. Extensions to MPT have been developed to address some of its limitations, such as the assumption of normal distribution and correlation stability [11]. Regarding the performance of different asset class combinations, it is essential to consider the specific characteristics and dynamics of each asset class. The performance of different asset class combinations can vary over time and depend on various factors, including economic conditions, market trends, and investor sentiment. To provide a visual representation, an efficient frontier graph, which displays the trade-off between risk and return for various asset allocations, could be included. The graph can demonstrate how portfolios with different asset class combinations can achieve different risk-return profiles.

To sum up, MPT is a fundamental component of portfolio management that highlights the significance of both diversification and risk-return equilibrium. By constructing portfolios along the efficient frontier, investors can aim to achieve optimal risk-return profiles. However, MPT has its limitations, and extensions to the theory have been developed to address these shortcomings. The performance of different asset class combinations is dynamic and influenced by various factors, making ongoing analysis and adaptation crucial for successful portfolio management.

4 CAPM

In the context of portfolio management, the Capital Asset Pricing Model (CAPM), a commonly used paradigm in finance, offers insights into the link between risk and expected return. The idea that an asset's expected return should be in line with its systematic risk forms the basis of William Sharpe's 1964 Capital Asset Pricing Model (CAPM). This section will provide a detailed explanation of CAPM. CAPM starts with the assumption that investors are primarily concerned with the systematic risk, also known as market risk, of an asset. Systematic risk is the kind of risk that is linked to overall market fluctuations and cannot be mitigated by diversification. The degree of reactivity of a security's earnings to those of the market is represented by its beta value. According to CAPM, an asset's expected return is calculated by multiplying its beta and market risk premium by the risk-free rate. The return on a risk-free investment, usually represented by government bonds, is known as the risk-free rate. The excess return anticipated from investing in the market over the risk-free rate is reflected in the market risk premium [12]. A mathematical framework for estimating expected return is provided by the CAPM, which takes into account the market risk premium and the beta of an asset. Through a comparative analysis between the anticipated and actual returns, investors are able to determine the asset's relative value. The asset is deemed to have outperformed if the actual return is higher than the projected return calculated using the CAPM. [13]. It is crucial to remember that CAPM has its limitations even though it offers a helpful framework for comprehending risk and expected return. Critics contend that the CAPM is predicated on oversimplifying assumptions, like the notion of efficient markets and a linear relationship between returns and beta. These presumptions might not apply in practical situations. [14]. The following formula can be used to determine an asset's expected return using CAPM:

$$\text{Expected Return} = \text{Risk-Free Rate} + \text{Beta} \times (\text{Market Risk Premium}) \quad (1)$$

Investors can use the CAPM, which provides a framework for understanding the relationship between risk and return, to determine whether an asset is excessively priced or underpriced according to its expected return. When an asset's expected return is higher than what the CAPM predicts, it may be considered cheap and a good investment opportunity. However, it is important to note that CAPM has its limitations. Critics argue that CAPM relies on unrealistic assumptions and may not fully capture the complexities of real-world markets. In spite of these drawbacks, the capital asset pricing model (CAPM) is still a useful financial tool for determining an asset's expected return and comprehending the correlation among risk and return. In summary, the widely used CAPM financial model sheds light on the connection of risk and the expected return. Based on an asset's beta and the risk-free rate, it aids investors in estimating its expected return. While CAPM has its limitations, it continues to be a fundamental tool for analyzing investment opportunities and constructing portfolios.

5 Risk Parity

Risk Parity is an investment strategy that aims to allocate capital in a portfolio based on the risk contributions of different assets, rather than their market values or capital weights. The goal of Risk Parity is to achieve a balanced risk exposure across asset classes, resulting in a more diversified and potentially less volatile portfolio. The risky features of the assets determine how capital is allocated in a Risk Parity portfolio. The strategy seeks to equalize the risk contribution of each asset by allocating a larger portion of capital to assets with lower risk and a smaller portion to assets with higher risk. This approach recognizes that different assets have different volatilities and correlations, and Its goal is to distribute capital in a method that equalizes exposure to all possible risks.

In the framework of multi-asset portfolios, where conventional methods are used, the idea of risk parity has grown in popularity in recent years, such as market capitalization weighting or equal weighting, may not adequately account for risk. By diversifying risk contributions across asset classes, Risk Parity aims to provide a more stable risk profile and potentially enhance risk-adjusted returns. Implementing a Risk Parity strategy involves several steps. First, the risk measures of each asset in the portfolio need to be determined. Common risk measures used in Risk Parity include volatility, standard deviation, or Value-at-Risk (VaR). Next, the risk contributions of each asset are calculated by dividing the asset's risk measure by the total risk of the portfolio. Finally, the capital allocation is determined based on the calculated risk contributions.

While Risk Parity has gained popularity, it is not without its limitations. Critics argue that the strategy relies heavily on historical risk measures and correlations, which may not accurately reflect future market conditions. Additionally, Risk Parity strategies can be sensitive to the choice of risk measures and the estimation of correlations, which can introduce model risk.

6 Comparison, Limitations & Future Outlooks

Different types of asset allocations offer distinct characteristics and considerations. Traditional asset allocation approaches typically include a mix of stocks, bonds, and cash, with the proportions determined based on the investor's risk tolerance and time horizon. In an attempt to achieve a balance among risk and return, this approach diversifies across asset classes. However, alternative approaches to asset allocation, like factor-based allocation or Risk Parity, are more sophisticated. Risk Parity, as discussed earlier, focuses on balancing risk contributions across asset classes. It aims to achieve a more diversified risk exposure by allocating capital based on the assets' risk characteristics rather than their market values or capital weights. This strategy can be particularly useful in environments where traditional asset allocation methods may result in a concentrated or imbalanced risk profile.

Factor-based allocation involves identifying and allocating capital to specific risk factors, such as value, momentum, or low volatility, that have historically demonstrated the ability to explain asset returns. This approach seeks to capture the systematic

risk premia associated with these factors and construct portfolios that are tilted towards factors with the potential for higher returns. While alternative asset allocation strategies offer potential benefits, they also have limitations. The use of presumptions and historical data is one drawback. Factor-based strategies may undergo moments of failure or struggle to capture expected premia. Historical performance is not always a reliable predictor of future returns. Another limitation is the complexity and implementation challenges associated with alternative asset allocations. These strategies often require more sophisticated modeling techniques, data processing, and ongoing monitoring. Investors need to have a solid understanding of the underlying concepts and access to reliable data and analytical tools.

The future outlook for different types of asset allocations is influenced by ongoing advancements in financial technology, data availability, and research. One area of future development is the integration of machine learning and artificial intelligence techniques in asset allocation strategies. These technologies may enable more robust risk modeling, improved factor selection, and enhanced portfolio construction processes. Additionally, the incorporation of Environmental, Social, and Governance (ESG) considerations in asset allocation is gaining prominence. Investors are increasingly seeking to align their investments with sustainability goals, and there is a growing demand for ESG-integrated asset allocation strategies. The integration of ESG factors into asset allocation models can provide a more comprehensive assessment of risk and return, taking into account not only financial considerations but also sustainability and societal impact. Furthermore, advancements in data analytics and alternative data sources hold promise for refining asset allocation approaches. The availability of high-frequency data, sentiment analysis, and non-traditional data sets can provide valuable insights for identifying market patterns and improving risk estimation.

It is worth noting that all asset allocation strategies, including traditional and alternative approaches, have inherent risks and limitations. The future outlook for different types of asset allocations will be shaped by ongoing research, technological advancements, and the evolving needs and preferences of investors. Continued innovation and a focus on understanding and managing risks will be crucial in developing more effective and resilient asset allocation strategies.

7 Conclusion

In summary, portfolio theory is a framework for designing investment portfolios that aim to balance risk and return. It provides insights into the benefits of diversification and asset allocation strategies. This article provided an overview of portfolio theory, including its key concepts such as risk, return, and correlation. It discussed the Markowitz mean-variance optimization approach and introduced alternative strategies like Risk Parity and factor-based allocation. The limitations of portfolio theory were also discussed, such as the reliance on historical data and assumptions, as well as the challenges associated with accurately estimating risk and correlations. Looking ahead, the future outlook for portfolio theory involves advancements in risk modeling techniques, the integration of new data sources, and the incorporation of additional factors

such as ESG considerations. Ongoing research and innovation will continue to refine portfolio construction methodologies and enhance risk management practices. This study's contribution to the field of investment management makes it significant. By understanding and applying portfolio theory, investors can make more informed decisions in constructing their portfolios, considering risk factors, and optimizing their risk-return trade-offs. Both investors of all kinds who want to reach their financial objectives while successfully managing risk will find this information useful.

References

1. Rodríguez, Y. E., Gómez, J. M., Contreras, J.: Diversified behavioral portfolio as an alternative to modern portfolio theory. *The North American Journal of Economics and Finance*, 58, 101508 (2021).
2. Zerbib, O. D.: A sustainable capital asset pricing model (S-CAPM): Evidence from environmental integration and sin stock exclusion. *Review of Finance*, 26(6), 1345-1388 (2022).
3. Atodaria, Z., Shah, D., Nandaniya, J.: An Empirical Investigation of the CAPM and the Fama–French Three Factor Model in Indian Stock Market. *International Journal of All Research Education and Scientific Methods (IJARESM)*, 9(5), 1454-1459 (2021).
4. Hammouda, A., Saeed, A., Vidal, M., & Vidal-García, J.: On the short-term persistence of mutual fund performance in Europe. *Research in International Business and Finance*, 65, 101963 (2023).
5. Ma, Y., Han, R., Wang, W.: Portfolio optimization with return prediction using deep learning and machine learning. *Expert Systems with Applications*, 165, 113973 (2021).
6. Bessler, W., Taushanov, G., Wolff, D.: Factor investing and asset allocation strategies: a comparison of factor versus sector optimization. *Journal of Asset Management*, 22(6), 488-506 (2021).
7. Karnik, S., Sudhamathi, R. K., Tamilarasi, K., Krishnakumar, P., Thomas, R.: Risk Assessment And Portfolio Diversification Strategies In A Volatile Global Economy. *Boletín de Literatura Oral-Tradition Oral Literature*, 10(1), 1363-1373 (2023).
8. Abad, P.: An Analytic Solution to the CAPM Equilibrium. Available at SSRN 3939960 (2021).
9. Agarwal, S., Muppalaneni, N. B.: Portfolio optimization in stocks using mean–variance optimization and the efficient frontier. *International Journal of Information Technology*, 14(6), 2917-2926 (2022).
10. Sood, S., Papasotiriou, K., Vaiciulis, M., Balch, T.: Deep Reinforcement Learning for Optimal Portfolio Allocation: A Comparative Study with Mean-Variance Optimization. *FinPlan 2023*, 21 (2023).
11. Schmidt, O., Erdfelder, E., Heck, D. W.: Tutorial on multinomial processing tree modeling: How to develop, test, and extend MPT models. *Psychol. Methods*, 10 (2022).
12. Vergara-Fernández, M., Heilmann, C., Szymanowska, M.: Describing model relations: The case of the capital asset pricing model (CAPM) family in financial economics. *Studies in History and Philosophy of Science*, 97, 91-100 (2023).
13. Rui, K. X., Rasiah, D., Yen, Y. Y., Ramasamy, S., Pillay, S. D.: An analysis of the relationship between risk and expected return in Malaysia stock market: Test of the CAPM. *International Journal of Engineering & Technology*, 3(21), 161-170 (2018).

14. Erdinç, Y.: Comparison of CAPM, three factor Fama-French model and five-factor Fama-French model for the Turkish stock market. Financial management from an emerging market perspective, 4(1), 69-92 (2017).

Open Access This chapter is licensed under the terms of the Creative Commons Attribution-NonCommercial 4.0 International License (<http://creativecommons.org/licenses/by-nc/4.0/>), which permits any noncommercial use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons license and indicate if changes were made.

The images or other third party material in this chapter are included in the chapter's Creative Commons license, unless indicated otherwise in a credit line to the material. If material is not included in the chapter's Creative Commons license and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder.

