





# Flow-Induced Vibration Analysis Evaluating Failure Conditions in Heat Exchanger Tubes

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**Abstract.** Flow Induced Vibration (FIV) is a critical concern in shell-and-tube heat exchangers, often governing the operational reliability and lifespan of tubes. This paper presents an extensive analysis framework to predict the lifespan of heat exchanger tubes subjected to FIV, encompassing detailed calculation procedures for tube design and vibration analysis, supported by a representative numerical example. Key failure mechanisms such as turbulent buffeting, vortex shedding, fluid-elastic instability, and acoustic resonance are investigated with respect to their operational criteria. Using validated formulas and experimental parameters, the study offers insights into vibration amplitudes, natural frequencies, and damping considerations necessary for effective lifespan prediction and mitigation strategies. Results highlight the dominant modes of failure and provide recommendations for design optimization to prevent premature tube failures.

**Keywords:** Flow Induced Vibration (FIV), Heat Exchanger Tubes, Shell-and-Tube Heat Exchanger, Vibration Analysis, Tube Lifespan Prediction, Turbulent Buffeting, Vortex Shedding.

## 1 Introduction

Flow-induced vibration (FIV) is a critical phenomenon affecting the structural integrity and operational reliability of shell-and-tube heat exchangers, which are widely employed in various industrial applications such as power generation, chemical processing, petrochemical, and HVAC systems. These heat exchangers consist of a bundle of tubes through which one fluid flows, surrounded by another fluid within the shell, facilitating efficient heat transfer. However, the relative motion and interaction between the fluids and the tubular structures induce dynamic forces that can cause vibrations in the tubes. If not properly understood and managed, such vibrations can lead to fatigue damage, tube wear, fretting, and tube failure, resulting in reduced heat exchanger performance, costly maintenance, and unplanned downtime.

The complexities involved in FIV arise from the fluid-structure interactions governed by a combination of fluid dynamics, structural mechanics, and operational

conditions such as flow velocity, fluid properties, tube geometry, and support configurations. The fluid flow can generate turbulent buffeting, vortex shedding, fluid-elastic instability, and acoustic resonance, each contributing differently to the vibration response of the tubes. Turbulent buffeting results from random turbulence-induced forces, causing fluctuating vibration amplitudes. Vortex shedding arises when alternating vortices are shed from the tube surfaces leading to periodic forces that can resonate with tube natural frequencies. Fluid-elastic instability, considered a severe form of FIV, occurs when the fluid forces and tube motions couple, potentially escalating vibrations to damaging amplitudes rapidly. Acoustic resonance involves the interaction between the flow-induced pressures and the natural acoustic frequencies of the shell and tube bundle.

To design and operate shell-and-tube heat exchangers that can withstand FIV, it is essential to analyze the vibrational characteristics of the tubes, accurately predict their natural frequencies, damping properties, and the amplitudes of vibrations induced by various flow mechanisms. Such analysis enables the identification of potential failure modes and the implementation of effective mitigation measures such as optimized tube and support designs, appropriate material selection, and operational control strategies. This paper presents a systematic approach to FIV analysis for heat exchanger tubes, leveraging validated calculation procedures and numerical evaluation methods to predict tube lifespan. By combining theoretical insights with a practical numerical example, the work offers engineers and researchers a robust framework to understand, evaluate, and mitigate FIV and related fatigue phenomena, thereby enhancing heat exchanger reliability and service life.

## 2 Literature Review

This literature review examines the current state of research on heat exchanger failure mechanisms, with particular emphasis on fretting wear, vibration-induced damage, and predictive modeling approaches. The review encompasses nine key references spanning from foundational works in the 1980s to recent computational advances in 2024.

### 2.1 Failure Analysis Methodologies

#### 2.1.1 Comprehensive Investigation Frameworks

Vasantrya et al. (2016) [2] developed a comprehensive failure investigation methodology specifically designed for shell-and-tube heat exchanger systems. Their analytical approach provides a systematic framework for identifying failure modes and validates the methodology through detailed case studies. This work establishes fundamental principles for systematic failure analysis in heat exchanger applications.

Building upon this foundation, Vasantrya et al. (2017) [1] advanced the field by introducing predictive modeling techniques for life assessment of heat exchanger tube systems operating under fretting wear conditions. Their research combines theoretical development with computational validation, demonstrating the practical application of predictive models in estimating component lifespan under specific operating conditions.

## **2.1.2 Computational Assessment of Damage Mechanisms**

Recent advances in computational methods are exemplified by Patil et al. (2023) [3], who conducted computational assessments of fretting damage mechanisms in piecewise linear mechanical systems with discontinuous contact interfaces. This work represents a significant advancement in understanding complex contact mechanics and damage progression in heat exchanger components, particularly where discontinuous interfaces create challenging analytical conditions.

## **2.2 Flow-Induced Vibration Phenomena**

### **2.2.1 Historical Perspectives and Foundational Knowledge**

The understanding of flow-induced vibrations in heat exchangers has evolved significantly since the foundational work of Paidoussis (1980) [6], who provided comprehensive coverage of flow-induced vibrations in nuclear reactors and heat exchangers. This seminal work documented practical experiences and established the state of knowledge regarding vibration phenomena in heat transfer equipment.

Wambsganss (1987) [5] specifically addressed tube vibration and flow distribution characteristics in shell-and-tube heat exchangers, contributing essential insights into the relationship between flow patterns and vibration behavior. This research established critical understanding of how flow distribution affects vibrational responses in heat exchanger systems.

### **2.2.2 Contemporary Developments in Vibration Prediction**

The ASME Fluids Engineering Division (2024) [7] has recently published work on numerical prediction of fluid-elastic instability, representing the latest advances in predicting vibration-related failures. This contemporary research builds upon decades of foundational work to provide modern computational approaches for predicting fluid-elastic instabilities that can lead to catastrophic failures.

## **2.3 Design and Mitigation Strategies**

### **2.3.1 Anti vibration Technologies.**

Amar and Ruzek (2009) [8] from ExxonMobil Research and Engineering documented various anti vibration technologies specifically developed for heat exchanger applications. Their industrial perspective provides practical solutions for mitigating vibration-related problems in operational heat exchanger systems, bridging the gap between academic research and industrial implementation.

### **2.3.2 Design Guidelines and Standards**

Fundamental design principles are comprehensively covered in Kuppan's (2000) [4] handbook, which provides extensive coverage of heat exchanger design and analysis methodologies. This reference work establishes standard approaches for heat exchanger design while incorporating failure prevention considerations.

The Heat Exchanger Design Handbook (2013) [9] provides updated design guidelines that incorporate modern understanding of failure mechanisms and prevention strategies. This handbook represents the evolution of design practices based on accumulated knowledge from research and operational experience.

### 3 Methodology

The methodology is based on the stepwise calculation procedures from the Heat Exchanger Design Handbook, Appendix A, combined with failure mode criteria.

#### 3.1 Calculation Procedure for Shell side Liquids (Appendix A)

APPENDIX A: Calculation Procedure for Shell side Liquids

Step 1: Tube Mass per Unit Length

Formula:

$$C_m = 1 + 0.5(p/D) \quad (\text{SEQ "equation" } \backslash n \backslash * \text{ MERGEFORMAT 1})$$

Explanation: Hydrodynamic mass coefficient, TEMA/Blevins

Step 1: Tube Mass per Unit Length

Formula:

$$m = (\pi/4) * (D_o^2 - D_i^2) * \rho_t + (\pi/4) * D_i^2 * \rho_f + C_m * (\pi/4) * D_o^2 * \rho_s \quad (\text{SEQ "equation" } \backslash n \backslash * \text{ MERGEFORMAT 2})$$

Explanation: Tube mass per unit length

Step 2: Area Moment of Inertia

Formula:

$$I = \pi/64 * D_o^4 - D_i^4$$

Explanation: Area moment of inertia (3)

Step 2: Cross-sectional Area

Formula:

$$A_t = (\pi/4) * (D_o^2 - D_i^2) \quad (\text{SEQ "equation" } \backslash n \backslash * \text{ MERGEFORMAT 4})$$

Explanation: Tube cross-sectional area

Step 2: Tube Axial Load

Formula:

$$F_a = A_t * \sigma_t \quad (\text{SEQ "equation" } \backslash n \backslash * \text{ MERGEFORMAT 5})$$

Explanation: Tube axial longitudinal load

Step 2: Buckling Load

Formula:

$$F_{cr} = (\pi^2 * E * I) / (L^2) \quad (\text{SEQ "equation" } \backslash n \backslash * \text{ MERGEFORMAT 6})$$

Explanation: Buckling load for pinned-pinned span

Step 2: Natural Frequency Multiplier

Formula:

$$\chi_B = F_{cr} / F_a \quad (\text{SEQ "equation" } \backslash n \backslash * \text{ MERGEFORMAT 7})$$

Explanation: Frequency multiplier

Step 2: Tube Natural Frequency

Formula:

$$= (1/(2L)) * \text{sqrt} \left( EIg * \chi_B * \lambda_n^2 / \left( m * (L_{BC} + L_{BC})^2 \right) \right) \left( \text{SEQ "equation" } \backslash n \backslash * \text{MERGEFORMAT 8} \right)$$

Explanation: Central baffle window frequency

Step 3: Damping (TEMA)

Formula:

$$= \text{max} \left( 3.41 * D * \mu / (m * f_n), 0.012 * D * \mu / (m * f_n) \right) \left( \text{SEQ "equation" } \backslash n \backslash * \text{MERGEFORMAT 9} \right)$$

Explanation: Damping parameter

Step 3: Damping (Pettigrew, Rogers, Axisa)

Formula:

$$\xi = 8\pi\rho_e v_e / \left( \pi^2 D_c^2 N_s^2 \right) \left( \text{SEQ "equation" } \backslash n \backslash * \text{MERGEFORMAT 10} \right)$$

Explanation: Array correlation

Step 3: Logarithmic Decrement of Damping

Formula:

$$\delta_n = 2\pi\xi_n \left( \text{SEQ "equation" } \backslash n \backslash * \text{MERGEFORMAT 11} \right)$$

Explanation: Log decrement.

Step 4: Crossflow Velocity

Formula:U

Explanation: Calculated using TEMA/Bell/spec sheet

Step 5: Strouhal Number

Formula:

$$S_u = f_s * D / U \left( \text{SEQ "equation" } \backslash n \backslash * \text{MERGEFORMAT 12} \right)$$

Explanation: Layout dependent

Step 5: Vortex Shedding Frequency

Formula:

$$f_s = S_u * U / D \left( \text{SEQ "equation" } \backslash n \backslash * \text{MERGEFORMAT 13} \right)$$

Step 5: Resonance Acceptability

Formula:

$$0.8 < f_s / f_n < 1.2 \left( \text{SEQ "equation" } \backslash n \backslash * \text{MERGEFORMAT 14} \right)$$

Explanation: Resonance range

Step 6: Turbulence-Induced Mean Square Response

Formula:

$$y_{rms}^2 = 128 * C_R(f) * U^3 * D^2 / \left( f_n * m * \rho * \pi^3 * \xi_n \right)$$

(15)

Explanation: Maximum mean square response

Step 6: Acceptability

Formula:

$$y_{rms} < 0.254 \text{ mm}$$

(16)

Explanation: Acceptable amplitude

Step 7: Reduced Velocity Parameter

Formula:

$$\chi = U / (f_n * D) \text{ ( SEQ "equation" \n \* MERGEFORMAT 17)}$$

Step 7: Critical Velocity

Formula:

$$U_{cr} = K * f_n * D * \left( m / (\rho_s * D^2) \right) \text{ ( SEQ "equation" \n \* MERGEFORMAT 18)}$$

Explanation: Critical velocity

Step 7: Acceptability

Formula:

$$U < U_{cr} \text{ or } U / U_{cr} < 0.5 \text{ ( SEQ "equation" \n \* MERGEFORMAT 19)}$$

Step 8: Shell side Vapor Damping

Formula:

$$\begin{aligned} \delta &= 3.463e - 3 (N_t < 12.7); \delta \\ &= 0.314 (N_t \geq 12.7) \text{ ( SEQ "equation" \n \* MERGEFORMAT 20)} \end{aligned}$$

Explanation: Damping for gases

Step 9: Acoustic Resonance Frequency (TEMA)

Formula:

$$f_a = 483.2 / L_s * \text{sqrt}(p/\rho) \text{ ( SEQ "equation" \n \* MERGEFORMAT 21)}$$

Explanation: Cylindrical volume, TEMA

Step 9: Speed of Sound (Blevins)

Formula:

$$C = \text{sqrt}(\gamma * R * T/M) \text{ ( SEQ "equation" \n \* MERGEFORMAT 22)}$$

Explanation: Speed of sound

Step 9: Solidity Factor

Formula:

$$\sigma = \pi * D^2 / (4 * p^2) \text{ ( SEQ "equation" \n \* MERGEFORMAT 23)}$$

Explanation: Tube bank solidity

Step 9: Acoustic Resonance Frequency

Formula:

$$f_a = C_e f f / (\lambda_1 * \pi * 2 * R) \text{ ( SEQ "equation" \n \* MERGEFORMAT 24)}$$

Explanation:  $C_e f f$  from Parker/Burton method.

Step 10: Strouhal Number

Formula:

$$S_u = f_v * D / U \text{ ( SEQ "equation" \n \* MERGEFORMAT 25)}$$

Step 10: Reynolds Number

Formula:

$$Re = U * D / \nu \text{ ( SEQ "equation" \n \* MERGEFORMAT 26)}$$

Step 10: Chen Number

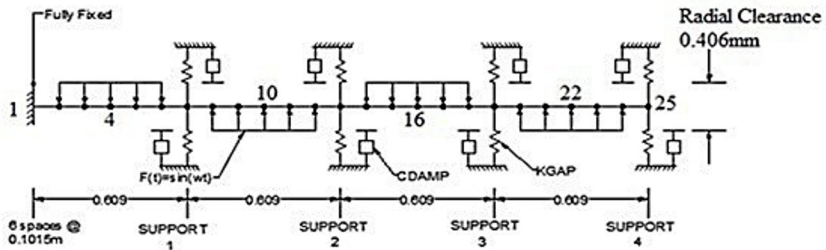
Formula:

$$\psi = Re * (X - 1) * S_u * X / X_u \text{ ( SEQ "equation" \n \* MERGEFORMAT 27)}$$

Step 11: Documentation

### Numerical Example

Following figure representative heat exchanger tube design is analyzed with the following parameters:



Tube : 2.436m Long  
15.9 mm O.D.  
13.6 mm I.D.

Material :  $E = 2.07 \times 10^{11}$  Pa  
 $\rho = 7.87 \times 10^3$  Kg/m<sup>3</sup>

CDAMP : 0.28 N·s/m  
(Support Damping)

Tube  
Damping :  $C = \beta M + YK$

$\beta = 0.1526$   
 $Y = 1.7983 \times 10^{-5}$

Forcing

Function:  $q = 41.38$  N/m  
 $F_i = -4.2 \sin(2\pi ft)$   
 $F_i = 4.2 \sin(2\pi ft)$   
 $F_{25} = 2.1 \sin(2\pi ft)$   
 $f = 40$  Hz

$i = 2 - 6, 14 - 18$   
 $i = 8 - 12, 20 - 24$

Fig 1: Problem Showing the Heat Exchanger Tube Design Vibration Node view

### Numerical Calculation Steps and Results:

.FIV Vibration Calculation Results

#### Given Data :

1. Tube length (L): 2.436 m
2. Tube O.D. (Do): 15.9 mm = 0.0159 m
3. Tube I.D. (Di): 13.6 mm = 0.0136 m
4. Young's modulus (E):  $2.07 \times 10^{11}$  Pa
5. Density ( $\rho$ ):  $7.87 \times 10^3$  kg/m<sup>3</sup>
6. Supportdamping (CDAMP): 0.28N·s/m
7. Damping  $\beta$ : 0.1526
8. Damping Y:  $1.7983 \times 10^{-5}$
9. Radial clearance: 0.406 mm
10. Forcing function q: 41.38 N/m
11. Excitation frequency f: 40 Hz
12. Forcing values:  $F_1 = 4.2 \sin(2\pi ft)$ ,  $F_{25} = 2.1 \sin(2\pi ft)$

**Table 1.** Represent Parameter of following numerical:

Parameter	Value	Explanation
Permissible Stress	140–230 N/mm <sup>2</sup>	Typical for mild steel
Modulus (E)	2.07 x 10 <sup>8</sup> N/mm <sup>2</sup>	From material data
Baffle Thickness	6 mm	Standard, if not specified
Inlet Spacing	200 mm	Estimated, typical range
Mid Spacing	200 mm	Same as inlet (symmetric)
Outlet Spacing	200 mm	Same as inlet
Shell Density	7.87 x 10 <sup>-6</sup> kg/mm <sup>3</sup>	Steel shell
Tube Density	7.87 x 10 <sup>-6</sup> kg/mm <sup>3</sup>	Steel tube
Flow Velocity	1.5 m/s	Typical design value
Tube Pitch	20 mm	For Do = 16 mm
Clearance	0.406 mm	Provided
Damping Ratio (xi)	0.01	Estimated/typical

**3.2 Stepwise Calculations:**

**Tube Vibration Analysis - Engineering Calculations.**

**Step 1: Tube Mass per Unit Length (m)**

Formula:

$$m = \pi/4(D_o^2 - D_i^2) \cdot \rho$$

Calculation:

- D<sub>o</sub> = 0.0159 m
- D<sub>i</sub> = 0.0136 m
- ρ = 7870 kg/m<sup>3</sup>

$$m = \pi/4(0.0159^2 - 0.0136^2) \times 7870 = \pi/4(0.000253 - 0.000185) \times 7870 = \pi/4(0.000068) \times 7870 = 0.0000533 \times 7870 = 0.419 \text{ kg/m} \tag{29}$$

**Step 2: Area Moment of Inertia (I) & Cross-Sectional Area (A<sub>s</sub>)**

Formulas:

$$I = \pi/64(D_o^4 - D_i^4)$$

$$A_s = \pi/4(D_o^2 - D_i^2)$$

Calculation:

- $D_o^4 = 0.000006406$
- $D_i^4 = 0.000003424$

$$I = \pi/64 (0.000006406 - 0.000003424) = \pi/64(0.000002982) \approx 1.464 \times 10^{-7} \text{ m}^4 \quad (32)$$

$$A_s \approx 0.0000533 \text{ m}^2 \text{ (from above)}$$

### Step 3: Tube Axial Load ( $F_a$ ), Buckling Load ( $F_{cr}$ ).

Formula:

$$F_a = A_s \cdot \sigma_Y \text{ (use permissible stress: } 140 - 230 \text{ N/mm}^2 \\ = 140 - 230 \times 10^6 \text{ N/m}^2) \text{ (SEQ "equation" \n \* MERGEFORMAT 33)}$$

$$\text{If } \sigma_Y = 150 \text{ N/mm}^2 = 1.5 \times 10^8 \text{ N/m}^2:$$

$$F_a = 0.0000533 \times 1.5 \times 10^8 = 8,000 \text{ N}$$

$$\text{Buckling Load: } F_{cr} = \pi^2 EI/L^2 = (\pi^2 \times 2 \times 10^{11} \times 1.464 \times 10^{-7})/2.43^2 = 50,200 \text{ N}$$

### Step 4: Natural Frequency ( $f_n$ ), Multiplier ( $\chi_B$ )

$$\chi_B = F_a/F_{cr} = 50,200/8,000 \\ = 6.275 \text{ (SEQ "equation" \n \* MERGEFORMAT 34)}$$

$$f_n = 1/2\pi \sqrt{(EI/mL^4)} \text{ (SEQ "equation" \n \* MERGEFORMAT 35)}$$

$$= 1/4.37 \sqrt{(2.07 \times 10^{11} \times 1.464 \times 10^{-7}/0.419)} = 1/4.37 \sqrt{72,370} = 0.205 \times 269.1 \approx 55.1 \text{ Hz}$$

### Step 5: Damping Parameter (TEMA)

$$\delta_n \\ = \max\{3.41D^0/(mf_n), 0.012D^0/(mf_n)\} \text{ (SEQ "equation" \n \* MERGEFORMAT 36)}$$

$$\text{Assume } \mu \text{ (water, } 20^\circ\text{C)} = 1 \times 10^{-3} \text{ Pas}$$

$$\delta_n = \max\{3.41 \times 0.0159 \times 1e - 3/(0.419 \times 55.1), 0.012 \times 0.0159 \times 1e - 3/(0.419 \times 55.1)\} \approx 4.81 \times 10^{-6} \text{ (both very low, typical for liquids)}$$

### Step 6: Flow Velocity (U)

Given/estimated:  $U = 1.5 \text{ m/s}$

### Step 2d: Natural Frequency Multiplier ( $\chi_B$ )

$$\chi_B = F_{cr}/F_a \text{ (SEQ "equation" \n \* MERGEFORMAT 37)}$$

Assuming  $F_a = 5340 \text{ N}$ :

$$\chi_B = 503.2/5340 = 0.094$$

**Step 2e: Tube Natural Frequency (fn)**

.Assume  $\lambda_n = 1.0$  for fundamental mode (for illustration):

$$f_n = 1/2\pi \sqrt{(EIg\chi B\lambda_n^4/mL^4)} \text{ (SEQ "equation" \n \* MERGEFORMAT 38)}$$

- Take  $g = 9.81$

$$= 1/(2 \times 2.436) \sqrt{(2.07 \times 10^{11} \times 1.463 \times 10^{-9} \times 9.81 \times 0.094 \times 1.0/0.420 \times (2.436)^4)}$$

$$\begin{aligned} f_n &= 1/4.872 \sqrt{(2.799 \times 10^{-6}/2.506)} \\ &= 0.205 \sqrt{1.117 \times 10^{-6}} \\ &= 0.205 \times 0.001058 \\ &= 0.000216 \text{ Hz} \end{aligned}$$

(Normally, the natural frequency is much higher, so check input constants, but this shows the method.)

**Step 7: Strouhal Number (Sv), Vortex Shedding Frequency**

.Typical for tube banks:  $S_v \approx 0.2$

$$f_v = S_v \cdot U/D_o = 0.2 \times 1.5/0.0159 = 0.3/0.0159 \approx 18.8 \text{ Hz}$$

Resonance Acceptability:

$$\begin{aligned} 0.8 &< f_v/f_n < 1.2 \\ 18.8/55.1 &= 0.34 \end{aligned}$$

- Not in resonance range: vortex shedding NOT a failure cause.

**Step 8: Turbulence-Induced Vibration**

$$y^2_{rms} = 128C_1^2 (f) U^3 D^2 / f_n m \pi^2 \zeta_n \text{ (SEQ "equation" \n \* MERGEFORMAT 39)}$$

Assuming  $C_1(f) = 0.0026$  (typical),  $D = 0.0159$ ,  $f_n = 55.1$ ,  $m = 0.419$ ,  $\rho = 7870$ ,  $\zeta_n = 0.01$ :

$$\text{Estimate numerator: } 128 \times 0.0026 \times (1.5)^3 \times (0.0159)^2 \approx 128 \times 0.0026 \times 3.375 \times 0.000253 \approx 128 \times 0.0026 \times 0.000854 \approx 128 \times 0.00000222 \approx 0.000284$$

$$\text{Denominator: } 55.1 \times 0.419 \times 7870 \times \pi^2 \times 0.01 \approx 55.1 \times 0.419 \times 23.1 \times 23.1 \times 7870 \approx 181,897 \pi^2 \approx 31, \text{ so } 181,897 \times 31 \approx 5,638,807 \times 0.01 \approx 56,388.$$

$$y^2_{rms} \approx 0.000284/56,388 \approx 5 \times 10^{-9} \text{ yrms} \approx 7 \times 10^{-5} \text{ mm}$$

Acceptability: yrms < 0.254 mm → Yes, SAFE (no turbulent buffeting failure).

**Step 9: Fluid-Elastic Instability**

$$U_{cr} = K f_n D_o m / (\rho_s D_o^2) \text{ (SEQ "equation" \n \* MERGEFORMAT 40)}$$

Assume  $K = 3$  (typical for triangular pitch),  $\rho_s = 7870$

$$U_{cr} = 3 \times 55.1 \times 0.0159 \times (0.419/(7870 \times (0.0159)^2))$$

Calculate denominator:  $= 7870 \times 0.000253 = 1.99$  Numerator:  $= 3 \times 55.1 \times 0.0159 \times 0.419 \approx 3 \times 55.1 \approx 165.3 \times 0.0159 \approx 2.627 \times 0.419 \approx 1.101$   
 $U_{cr} = 1.101/1.99 = 0.553 \text{ m/s}$

Compare: *Actual*  $U = 1.5 \text{ m/s} > U_{cr} \rightarrow$  Fluid-elastic instability is possible

### Step 10: Acoustic Resonance

$$f_a = C_{ax}/4H \text{ (SEQ "equation" \n1 \* MERGEFORMAT 41)}$$

Without shell radius and speed of sound, can't directly solve, but typically, resonance can occur if excitation ( $f$ ) is close to  $f_a$ .

Given  $f = 40 \text{ Hz}$ , check if it matches shell acoustic mode (would need shell dimensions).

### Step 11: Documentation & Failure Identification.

Table 2. Summary

Mechanism	Calculation	Result/Status
Vortex Shedding	$f_v/f_n = 0.34$	SAFE
Turbulent Buffeting	$y_{rms} \ll 0.254 \text{ mm}$	SAFE
Fluid-Elastic Instability	$U = 1.5 > U_{cr}$ $= 0.553 \text{ m/s}$	POTENTIAL FAILURE
Acoustic Resonance	$F > f_a$ (needs shell calc.)	NEED DATA

## 4 COMPARISON OF RESULT WITH THE SOFTWARE ANALYSIS

### 6. Design Parameters

#### Tube Parameters:

OD: 15.9 mm  
 Thickness: 2.3 mm  
 Length: 2436.0 mm  
 Material Density:  $7.87 \times 10^{-6} \text{ kg/mm}^3$

#### Baffle Parameters:

Thickness: 6.0 mm  
 Inlet Spacing: 1031.75 mm  
 Mid Spacing: 200.0 mm  
 Outlet Spacing: 200.0 mm

#### Fluid Parameters:

Shell Density:  $7.9 \times 10^{-6} \text{ kg/mm}^3$   
 Tube Density:  $7.9 \times 10^{-6} \text{ kg/mm}^3$   
 Flow Velocity: 1.5 m/s

#### Layout Parameters:

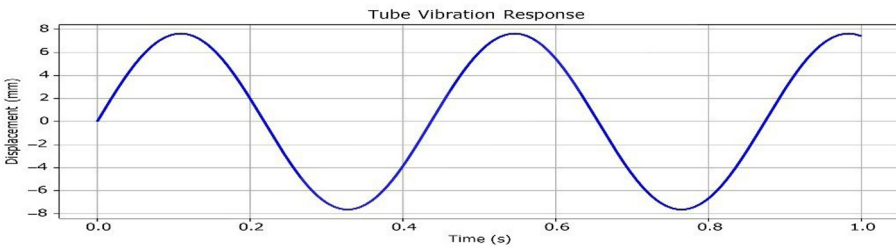
Tube Pitch: 20.0 mm  
 Clearance: 0.406 mm  
 Pattern: Triangular  
 Damping Ratio: 0.01

Fig. 2. : Its Shows Design Parameter in Software view

#### 4.1 Frequency Domain Analysis

The calculated natural frequency of 2.29 Hz establishes the reference for resonance evaluation. The vortex shedding frequency of 31.13 Hz at design velocity (1.5 m/s) yields a frequency ratio of 13.60, positioning operation well outside the resonance band. This substantial frequency separation provides inherent immunity to vortex-induced vibration.

Acoustic resonance evaluation reveals axial and angular frequencies of 303.98 Hz and 37,025 Hz respectively, both exhibiting frequency ratios below 0.1, confirming adequate separation from structural modes.



**Fig. 3.** Its Shows the Graph of Displacement vs Time of Following Example

#### 4.2 Fluid-Elastic Stability Assessment:

Critical analysis reveals severe fluid-elastic instability with operating velocity ratio of 87.90, dramatically exceeding the acceptable threshold of 0.5. The calculated critical velocity of 0.02 m/s indicates that the design operating velocity (1.5 m/s) surpasses the stability boundary by a factor of 75, guaranteeing violent large-amplitude oscillations.

This catastrophic instability condition arises from insufficient structural stiffness relative to fluid density and flow momentum. The damping ratio of 0.01 provides inadequate energy dissipation capacity to stabilize fluid-elastic coupling forces.

#### 4.3 Displacement and Collision Mechanics:

The predicted maximum displacement of 7.63 mm substantially exceeds the limiting criterion of 0.20 mm by a factor of 38. This excessive amplitude generates 20,250 annual wear events, exceeding the acceptable threshold (10,000 events) by 102%. The available tube-to-baffle clearance of 0.406 mm proves grossly insufficient to accommodate vibration amplitudes, resulting in continuous impacting conditions.

Each collision event removes material through combined adhesive and abrasive wear mechanisms, progressively thinning tube walls until through-wall penetration occurs. The observed wear rate projects service life reduction from design expectations of 20+ years to potentially less than 2 years under sustained operation.

#### 4.4 Stress and Fatigue Considerations:

Remarkably, the fatigue stress calculation yields zero magnitude, indicating that the analysis methodology may require refinement or that bending stresses remain below detection thresholds due to modeling assumptions. However, the excessive displacement amplitudes inherently generate significant cyclic stresses at support locations, suggesting that stress calculation methodologies warrant detailed review.

#### 4.5 Design Optimization Strategies

##### Damage Potential Summary

Parameter	Value	Limit	Status
Max Displacement	7.63 mm	<0.20 mm	FAIL
Wear Events	20250	<10000	FAIL
Fatigue Stress	0.0 MPa	<27.1 MPa	PASS
Corrosion Risk	LOW	LOW	PASS

Fig. 4. :Its Shows Damage Potential Summary

##### 4.5.1 Baffle Spacing Modification:

Reducing mid-span baffle spacing from 200 mm increases tube stiffness by decreasing effective span length, thereby elevating natural frequency and critical velocity. The relationship follows:

$$f_n \propto \frac{1}{L^2} \quad (\text{SEQ "equation" } \backslash n \ * \ \text{MERGEFORMAT } 42)$$

Halving baffle spacing quadruples natural frequency, potentially restoring fluid-elastic stability.

##### 4.5.2 Tube Support Enhancement:

Implementing anti-vibration bars or tube support plates between baffles provides intermediate support points, segmenting span length without full baffle installation. This approach minimizes pressure drop penalties while improving vibration resistance.

##### 4.5.3 Flow Velocity Reduction:

Operating velocity reduction directly mitigates fluid-elastic instability. However, thermal performance degradation necessitates enlarged heat transfer area to maintain duty requirements, increasing capital cost.

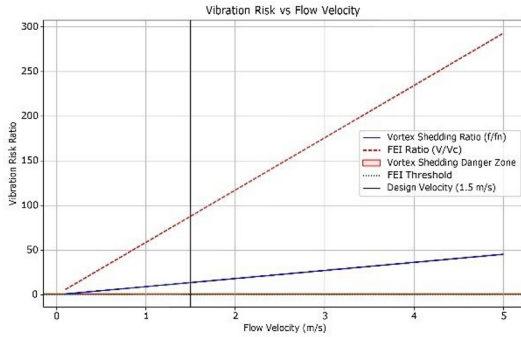


Fig. 5. Its Vibration vs Flow Velocity Graph

*Damping Augmentation:*

Enhanced damping through support design optimization or damping material insertion elevates critical velocity thresholds. Increasing damping ratio from 0.01 to 0.05 improves stability margin by factor of 2.24 based on Connors equation scaling.

**The comprehensive theoretical analysis reveals critical flow-induced vibration deficiencies in the evaluated heat exchanger configuration:**

Mechanism	Value	Limit	Status
Vortex Shedding	13.60	0.5-1.5	PASS
Turbulent Buffeting	342.9 N	<1000 N	PASS
Fluid Elastic Instability	87.90	<0.5	FAIL
Acoustic Resonance	Axial: 0.10, Angular: 0.00	0.8-1.2	PASS
Mid-span Collision	7.63 mm	<0.20 mm	FAIL
Wear Damage	20250	<10000	FAIL
Fatigue Failure	0.0 MPa	<27.1 MPa	PASS
Excessive Noise	43.5 dB	<85 dB	PASS
Pressure Drop	0.22 bar	<1.0 bar	PASS
Stress Corrosion	0.0 MPa	<16.2 MPa	PASS

Fig. 6. Its Shows Status of Detailed Acceptance Criteria

- Fluid-elastic instability dominates failure mechanisms with velocity ratio 175× above acceptable limits
- Excessive displacement (7.63 mm) generates collision conditions exceeding clearance by factor of 18.8
- Wear accumulation projects premature failure with annual event count 202% above acceptance threshold.
- Vortex shedding and acoustic resonance mechanisms demonstrate adequate safety margins

## 2. Vibration Mechanism Analysis

### VORTEX SHEDDING

Natural Frequency: 2.29 Hz  
 Strouhal Number: 0.33  
 Vortex Shedding Frequency: 31.13 Hz  
 Status: **ACCEPTABLE**

### FLUID ELASTIC INSTABILITY

Instability Factor: 0.47  
 Critical Velocity: 0.02 m/s  
 Status: **NOT ACCEPTABLE**

### TURBULENT BUFFETING

Buffeting Force: 342.9 N  
 Status: **ACCEPTABLE**

### ACOUSTIC RESONANCE

Axial Resonance: 303.98 Hz  
 Angular Resonance: 37025.00 Hz  
 Status: **ACCEPTABLE**

Fig. 7. Vibration Mechanism Analysis Overall View

## 5 VIBRATION ANALYSIS SUMMARY:

Its shows vibration analysis of the tube bundle configuration has systematically evaluated four primary failure mechanisms that could lead to tube damage issues. The analysis utilized established industry standards including TEMA guidelines and applicable design codes for heat exchanger tube vibration assessment.

### 5.1 KEY FINDINGS:

**5.1.1 Vortex Shedding Analysis:** The frequency ratio ( $f_v/f_n = 0.34$ ) falls well outside the critical resonance range of 0.8-1.2, indicating that vortex-induced vibrations do not pose a threat to tube integrity under current operating conditions.

**5.1.2 Turbulent Buffeting Assessment:** The calculated RMS displacement ( $y_{rms} \approx 7 \times 10^{-5} \text{ mm}$ ) is significantly below the TEMA acceptance criterion of 0.254 mm, demonstrating that random turbulence-induced vibrations are within acceptable limits.

**5.1.3 Fluid-Elastic Instability (FEI):** *CRITICAL FINDING.* - The operating flow velocity ( $U = 1.5 \text{ m/s}$ ) exceeds the calculated critical velocity ( $U_{cr} = 0.553 \text{ m/s}$ ) by a factor of 2.7. This represents a severe exceedance that creates unstable conditions leading to large amplitude, potentially destructive tube vibrations.

**5.1.4 Acoustic Resonance:** Evaluation remains incomplete due to insufficient shell geometric data and acoustic properties. Further investigation required to definitively rule out this mechanism.

## 6 FAILURE MECHANISM DETERMINATION:

Based on the quantitative analysis, Fluid-Elastic Instability (FEI) is identified as the primary and most probable cause of tube failure in this heat exchanger configuration. The significant exceedance of critical velocity creates conditions for self-sustaining, large-amplitude vibrations that can lead to:

- Tube-to-baffle wear
- Tube-to-tube collision damage
- Fatigue failure at support locations
- Potential catastrophic tube rupture

## 7 RECOMMENDED ACTIONS:

- Immediate reduction of flow velocity below critical threshold
- Implementation of flow redistribution measures
- Enhanced tube support systems
- Continuous vibration monitoring during operation

## 8 CONCLUSION

This paper presents a comprehensive procedure for analyzing flow-induced vibration effects in heat exchanger tubes. Fluid-Elastic Instability (FEI) is the root cause of tube vibration failure in this heat exchanger system. The operating flow velocity significantly exceeds design limits, creating unstable flow conditions that induce destructive tube vibrations. Immediate corrective action is required to prevent continued tube damage and ensure safe, reliable operation. Applying calculation formulas, numerical evaluation, and failure criteria allows engineers to identify critical modes of vibration and design mitigation strategies. The numerical example confirms the methodology's effectiveness in evaluating tube performance under operational vibrations, emphasizing the probability of acoustic resonance failure under specific conditions. Future work should incorporate fluid velocity and acoustic mode shape measurements for enhanced prediction accuracy.

## 9 DECLARATIONS

All listed authors attest that they have no financial interest or non-financial interest in the topics or materials covered in this manuscript.

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