



designed for monitor AGC;  $K_f(1 + \frac{1}{Ts})$  is the transfer function of monitor AGC;  $\Delta S$ ,  $\Delta P$  and  $\Delta h$  is increment of gauge, press and thickness, respectively;  $\Delta S^*$  is gauge increment for  $\Delta h$ ;  $M$  and  $Q$  is stiffness coefficient of rolling mill and plasticity coefficient of steel;  $e^{-Ts}$  is time delay part.

From fig. 1, we can see that it is a cascade control system and we can design controller for DAGC system and monitor AGC system, respectively. As shown in fig. 2 a data driven controller is designed for the monitor AGC main loop control system, and controller can be designed directly based on input and output data, and the process of model identification is avoided. The PID control strategy is applied to the secondary loop control system. With the secondary loop control system, disturbances added in the secondary loop are rejected in advance, and the influence of disturbances on the main control loop is weakened.

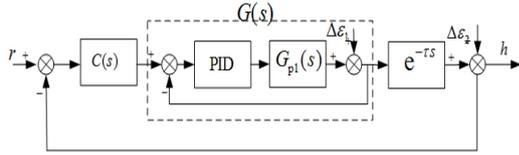


Fig.2 Block diagram of AGC cascade control system

Where  $G(s)$  is press AGC control system;  $r$  is reference input;  $\Delta\epsilon_1$ ,  $\Delta\epsilon_2$  is external disturbance;  $C(s)$  is controller for monitor AGC system.

### III. DATA DRIVEN CONTROLLER DESIGNING

#### A. Subspace Identification

A linear time invariant state space system can be described as<sup>[8]</sup>:

$$\mathbf{x}(k+1) = \mathbf{A}\mathbf{x}(k) + \mathbf{B}\mathbf{u}(k) + \mathbf{K}\mathbf{v}(k) \quad (1)$$

$$\mathbf{y}(k) = \mathbf{C}\mathbf{x}(k) + \mathbf{D}\mathbf{u}(k) + \mathbf{v}(k) \quad (2)$$

Where  $\mathbf{u}(k)$ ,  $\mathbf{y}(k)$  and  $\mathbf{x}(k)$  are the process inputs, outputs and states, respectively;  $\mathbf{A}$ ,  $\mathbf{B}$ ,  $\mathbf{C}$ ,  $\mathbf{D}$  and  $\mathbf{K}$  are appropriate dimension matrices;  $\mathbf{v}(k)$  is white noise sequence. We assumed that  $(\mathbf{A}, \mathbf{B})$  is controllable and  $(\mathbf{A}, \mathbf{C})$  is observable, it can be obtained by recursive substitution of (1) into (2)

$$\mathbf{Y}_f = \mathbf{\Gamma}\mathbf{X}_f + \mathbf{H}_f\mathbf{U}_f \text{ or } \mathbf{Y}_p = \mathbf{\Gamma}\mathbf{X}_p + \mathbf{H}_p\mathbf{U}_p \quad (3)$$

Where the subscript p and f denote “past” and “future”.

The measurements of the inputs and outputs  $\mathbf{u}(k)$  and  $\mathbf{y}(k)$  for  $k \in \{0, 1, \dots, 2N+j-2\}$  are available. The data block Hankel matrices for  $\mathbf{u}(k)$  represented as  $\mathbf{U}_p$  and  $\mathbf{U}_f$  with i-block rows and j-blocks columns are defined as

$$\mathbf{U}_p = \begin{pmatrix} \mathbf{u}(1) & \mathbf{u}(2) & \cdots & \mathbf{u}(j) \\ \mathbf{u}(2) & \mathbf{u}(3) & & \mathbf{u}(j+1) \\ \vdots & \vdots & \ddots & \vdots \\ \mathbf{u}(N-1) & \mathbf{u}(N) & \cdots & \mathbf{u}(N+j-1) \end{pmatrix}$$

$$\mathbf{U}_f = \begin{pmatrix} \mathbf{u}(N) & \mathbf{u}(N+1) & \cdots & \mathbf{u}(N+j) \\ \mathbf{u}(N+1) & \mathbf{u}(N+2) & & \mathbf{u}(N+j+1) \\ \vdots & \vdots & \ddots & \vdots \\ \mathbf{u}(2N-1) & \mathbf{u}(2N) & \cdots & \mathbf{u}(2N+j-1) \end{pmatrix}$$

Where the outputs block Hankel matrices  $\mathbf{Y}_f$  and  $\mathbf{Y}_p$  are defined in the same way.

In the case when no noise is present, the actual future outputs  $\mathbf{Y}_f$  lies in the combined row space and the linear predictor equation can be written as

$$\hat{\mathbf{Y}}_f = \mathbf{L}_w\mathbf{W}_p + \mathbf{L}_u\mathbf{U}_f \quad (4)$$

Where  $\mathbf{W}_p = [\mathbf{U}_p^T \quad \mathbf{Y}_p^T]^T$  and  $\mathbf{U}_f$  are the past inputs and outputs and future inputs, respectively,  $\mathbf{L}_w$  and  $\mathbf{L}_u$  are subspace matrices corresponding to the states and inputs. By solving the following least-square problem, the outputs prediction  $\hat{\mathbf{Y}}_f$  can be extracted

$$\min \left\| \mathbf{Y}_f - (\mathbf{L}_w, \mathbf{L}_u) \begin{pmatrix} \mathbf{W}_p \\ \mathbf{U}_f \end{pmatrix} \right\|_F^2 \quad (5)$$

The orthogonal projection of the row space of  $\mathbf{Y}_f$  into the row  $\mathbf{W}_p$  and  $\mathbf{U}_f$ , and  $\mathbf{L}_w$ ,  $\mathbf{L}_u$  can be obtained via QR decomposition.

$$\begin{bmatrix} \mathbf{W}_p \\ \mathbf{U}_f \\ \mathbf{Y}_f \end{bmatrix} = \mathbf{R}\mathbf{Q} = \begin{bmatrix} \mathbf{R}_{11} & 0 & 0 \\ \mathbf{R}_{21} & \mathbf{R}_{22} & 0 \\ \mathbf{R}_{31} & \mathbf{R}_{32} & \mathbf{R}_{33} \end{bmatrix} \begin{bmatrix} \mathbf{Q}_1^T \\ \mathbf{Q}_2^T \\ \mathbf{Q}_3^T \end{bmatrix} \quad (6)$$

$$\mathbf{L} = [\mathbf{L}_w \quad \mathbf{L}_u] = [\mathbf{R}_{31} \quad \mathbf{R}_{32}] \begin{bmatrix} \mathbf{R}_{11} & 0 \\ \mathbf{R}_{21} & \mathbf{R}_{22} \end{bmatrix}^\dagger \quad (7)$$

where “ $\dagger$ ” denote the Moore-Penrose pseudo-inverse.

#### B. Controller Designing

For the time instant  $k$ , using the future inputs  $\mathbf{u}_f = [\mathbf{u}_k, \dots, \mathbf{u}_{k+N-1}]$ ,  $\mathbf{u}_p = [\mathbf{u}_{k-N}, \dots, \mathbf{u}_{k-1}]$  and past outputs  $\mathbf{y}_p = [\mathbf{y}_{k-N}, \dots, \mathbf{y}_{k-1}]$ , we can get the future

outputs  $\hat{\mathbf{y}}_f = [\hat{\mathbf{y}}_k, \dots, \hat{\mathbf{y}}_{k+N-1}]$ , and the prediction expressions of the outputs can be written as

$$\hat{\mathbf{y}}_f = \mathbf{L}_w \mathbf{w}_p + \mathbf{L}_u \mathbf{u}_f \quad (8)$$

That is

$$\begin{bmatrix} \hat{\mathbf{y}}(k) \\ \hat{\mathbf{y}}(k+1) \\ \vdots \\ \hat{\mathbf{y}}(k+N-1) \end{bmatrix} = \mathbf{L}_w \begin{bmatrix} \mathbf{u}(k-N) \\ \mathbf{u}(k-N+1) \\ \vdots \\ \mathbf{u}(k-1) \\ \mathbf{y}(k-N) \\ \mathbf{y}(k-N+1) \\ \vdots \\ \mathbf{y}(k-1) \end{bmatrix} + \mathbf{L}_u \begin{bmatrix} \mathbf{u}(k) \\ \mathbf{u}(k+1) \\ \vdots \\ \mathbf{u}(k+N-1) \end{bmatrix} \quad (9)$$

The cost function to be minimized becomes

$$\begin{aligned} J &= \sum_{i=1}^{H_p} (\mathbf{r}(k+i) - \hat{\mathbf{y}}(k+i))^T \mathbf{Q}_i (\mathbf{r}(k+i) - \hat{\mathbf{y}}(k+i)) \\ &\quad + \sum_{i=0}^{H_c-1} \mathbf{u}(k+i)^T \mathbf{R} \mathbf{u}(k+i) \\ &= (\mathbf{r}_f - \hat{\mathbf{y}}_f)^T \mathbf{Q} (\mathbf{r}_f - \hat{\mathbf{y}}_f) + \mathbf{u}_f^T \mathbf{R} \mathbf{u}_f \end{aligned} \quad (10)$$

Where  $H_p$  and  $H_c$  denote the predictive horizon and control horizon, respectively.  $\mathbf{r}$  are reference inputs. The output and input weighting matrices  $\mathbf{Q} = \text{diag}(\mathbf{Q}_1 \dots \mathbf{Q}_{H_p}) > 0$  and  $\mathbf{R} = \text{diag}(\mathbf{R}_1 \dots \mathbf{R}_{H_c}) \geq 0$ . To find the minimum of  $J$ , its derivative is set to zero

$$\frac{\partial J}{\partial \mathbf{u}_f} = 0 \quad (11)$$

The control law are therefore defined as

$$\mathbf{u}(k) = (\mathbf{R} + \mathbf{L}_u^T \mathbf{Q} \mathbf{L}_u)^{-1} \mathbf{L}_u^T \mathbf{Q} (\mathbf{r} - \mathbf{L}_w \mathbf{W}_p) \quad (12)$$

and only the first control law is used to the system at time  $k$ .

$$\begin{aligned} \mathbf{u}(k) &= (\mathbf{I} \ 0 \ \dots \ 0) \cdot \\ &(\mathbf{R} + \mathbf{L}_u^T \mathbf{Q} \mathbf{L}_u)^{-1} \mathbf{L}_u^T \mathbf{Q} (\mathbf{r} - \mathbf{L}_w \mathbf{W}_p) \end{aligned} \quad (13)$$

#### IV. SIMULATION RESULTS

In this section, we will use the simplified second order transfer function from the engineering practice to illustrate the performance of the proposed control strategy.

$$G(s) = \frac{2110.7}{s^2 + 1983.7s + 39.7}$$

We set control horizon  $H_c = 2$ ; predictive horizon  $H_p = 4$ ; sampling time is 5ms; and input disturbance  $\Delta \varepsilon_1 = 0.08 \sin(12t + 90) + 0.04 \cos(24t) + 0.008$  as shown in fig. 3.

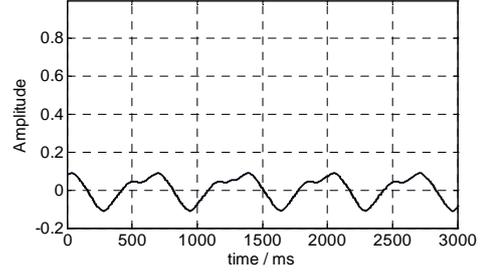


Fig. 3 Input of disturbance

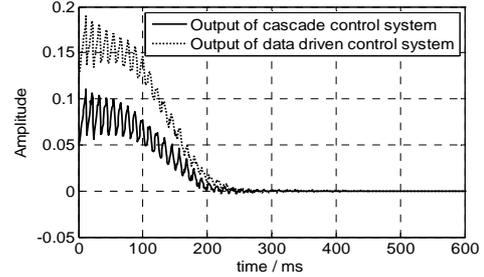


Fig. 4 Output of the system

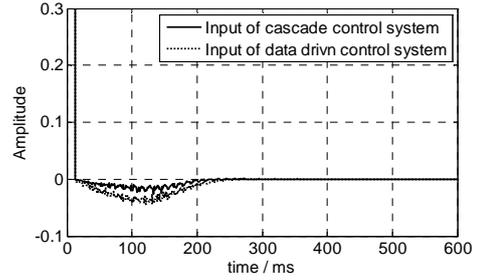


Fig. 5 Output of the system with disturbance

Fig. 4 compares the outputs of the control system of two control strategy. it can be seen that, we can get better control effects using cascade control strategy compared with data driven control strategy alone, where second looper PID control, we set parameter values  $P=80$ ,  $I=0.4$ . In addition, we can improve performance by setting different value of PID parameter. Fig.5 compares inputs of control system of two control strategy. In summary, the disturbance rejection and control precision can be improved using cascade control strategy.

#### V. CONCLUSIONS

In the paper, we design cascade control strategy for automatic gauge control system, where we design data driven controller for main loop monitor AGC system as well as PID controller for secondary loop DAGC system. The PID second loop control system can reject disturbance in advance, and reacts quickly and able to compensate the disturbance faster compared to the data driven control system. Furthermore, based on data driven control theory, the model identification process is avoided and control precision and performance is improved. Simulation results

show the efficiency and feasibility of the proposed control strategy.

#### ACKNOWLEDGMENT

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