

Experimental Investigation and Finite Element Analysis for Mechanical Behavior of Steel-concrete Composite Beams under Negative Bending

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Abstract. Experiments on four steel-concrete composite beams under negative bending were carried out in this paper. The effects of three factors such as bending moment ratio between two ends of a beam, height-to-thickness ratio of web, lateral slenderness ratio of compressive flanges on the bending bearing capacity M_u of composite beams were investigated. The experimental results indicate that M_u and M_u/M_p decrease as bending moment ratio between two ends of a beam increases, and M_p is cross-section plastic moment of composite beam. M_u is less affected by height-to-thickness ratio of web. However, M_u/M_p decreases as height-to-thickness ratio of web increases. If lateral slenderness ratio of compressive flanges is large, M_u and M_u/M_p are less affected by lateral slenderness ratio of compressive flanges. Finally, the finite element models of four composite beams under negative bending were established. The calculated results agree well with the experimental results.

Introduction

Steel - concrete composite beam is a kind of reasonable and economical construction member of high strength and low cost. At the same time, composite beam by the negative bending can encounter distortional buckling failure mode which is different from buckling of the steel beams. so it's now attracting considerable attention on mechanical behavior of steel-concrete composite beams under negative bending.

Daniels et al.[1] studied on bending bearing capacity M_u of composite beams with the compact section in negative moment regions by applying concentrated load at mid-span for two-span continuous composite beam. The results showed that M_u of composite beams with the compact section can reach cross-section plastic moment of composite beam when the lateral slenderness ratio of steel beam is small. Johnson[2] and Bradford[3] studied on distortional lateral buckling of composite beam under negative moment regions by applying uniform load to the two-span continuous beam and proposed that height-to-thickness ratio of web is the major influence on M_u . Experiment study on simply supported composite beams by applying concentrated load at mid-span to form negative moment regions by Kemp et al.[4]. It was found from experiment results that height-to-thickness ratio of web, lateral slenderness ratio of compressive flange are the major influence on M_u . Zhu P.R. et al.[5] and Fan J.S. et al.[6] conducted experiment of continuous composite beams to analyze internal force redistribution and ductility of the continuous composite beams and presented that the larger force ratio of composite beam, the smaller the ductility of composite beam. Liu Y. et al.[7] studied on the mechanical performance of composite beams under negative moments by finite element analysis and considered that bending moment ratio between two ends of a beam has effect on M_u and ductility of the composite beam. In above experiments, bending moment ratio between two ends of a beam was not investigated.

This paper will present experiments on four steel-concrete composite beams under negative bending were carried out in this paper. The effects of three factors such as bending moment ratio between two ends of a beam, height-to-thickness ratio of web, lateral slenderness ratio of

compressive flanges on the bending bearing capacity M_u of composite beams were investigated. At the same time, this paper will introduce the finite element models of four composite beams under negative bending and verification of the model.

Experimental Program

Test Specimens

A total of four composite beam specimens in Figure 1 were tested under negative bending. As shown in Figure 1, the concrete slab was 800mm wide and 100mm thick. Two layers of C8 (8mm in diameter) rebars with 200mm spacing in the concrete slab longitudinally were provided 15mm away from the top and bottom surface of the concrete slab. Two layers of C8 (8mm in diameter) rebars in the concrete slab along the width direction were provided at 250mm spacing. Two rows of studs with 16mm diameter and 80mm long were welded to the top flange with a transverse spacing of 70mm and longitudinal spacing of 220 mm and 300 mm for the beams with a span of 3 m and 4.2 m.

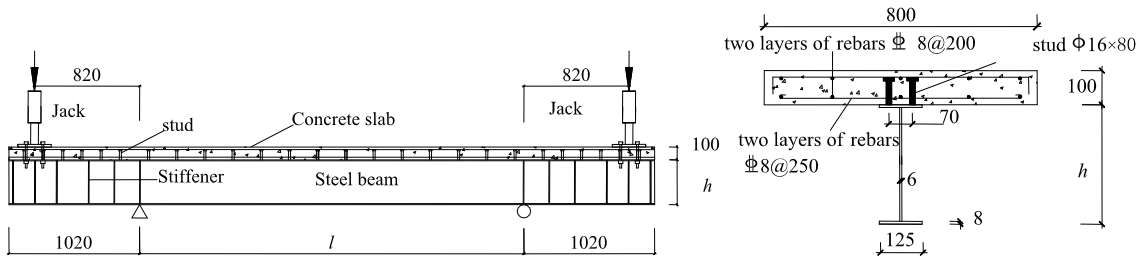


Fig. 1 Geometry of composite beam specimens

As shown in the Table 1, the test specimens were labelled as $-B\Box-\bigcirc-\triangle$ so that the specimen information could be identified from the labels: the B indicated composite beam; The $-\Box$ indicated the span of the beam. 4.2 and 3.0 meant 4200mm and 3000mm respectively; The $-\bigcirc$ indicated the height of the H-shaped cross section. 350 and 400 meant 350mm and 400mm respectively; The $-\triangle$ indicated the load case. 1 and 0 meant bending moment ratio $M_2/M_1=1$ and bending moment ratio $M_2/M_1=0$, respectively.

Tab. 1 Parameters of Test Specimens

Specimens	Span l (mm)	Cross section dimension(mm)	Spacing in studs(mm)	Bending moment ratio M_2/M_1
B3.0-350-1	3000	350×125×6×8	220	1
B3.0-350-0	3000	350×125×6×8	220	0
B4.2-350-1	4200	350×125×6×8	300	1
B4.2-400-1	4200	400×125×6×8	300	1

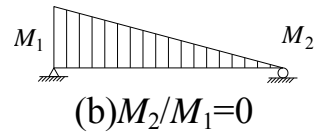
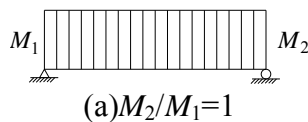


Fig. 2 Bending Moment Cases

The primary parameters were the bending moment ratio between two ends of a beam, height-to-thickness ratio of web, lateral slenderness ratio of compressive flanges. The value of primary parameters is setting as the follows:(1)There are two types of bending moment ratio between two ends of a beam in Figure 2.(2)Two kinds of H-shaped section are 350mm × 125mm × 6mm×8 mm and 400mm ×125mm × 6mm ×8 mm. The main difference between the two kinds of H section lies in height-thickness ratio of web h_w/t_w . The h_w/t_w of former and latter section are 55.7 and 64.0,

respectively. (3) There are two kinds of lateral slenderness ratio of compressive flange. The spans l of all the specimens are 3000mm and 4200mm so that the value of lateral slenderness ratio l/r_y of compressive flanges is 83.1 and 116.4 respectively. r_y is the radius of gyration of compressive flange along y direction.

Material

Mechanical properties of steel, rebar and concrete are given in Table 2.

Tab. 2 Mechanical Properties of Steel, Rebar and Concrete

Element	f_y (MPa)	f_u (MPa)	f_{cu} (MPa)
Steel web	362	489	—
Steel flange	403	522	—
Rebar	530	657	—
Concrete slab	—	—	25.1

Notes: f_y is yield strength of steel; f_u is tensile strength of steel; f_{cu} is compressive strength of concrete

Instrumentation and Test Rigs

Stress of the rebar in the concrete slab, flange and web of the steel beam were recorded by means of strain gauges for revelation of any possible local buckling of the I-beam at the middle span and the support. Besides, vertical and lateral displacement of the beam was recorded through displacement transducers at the end support, one-half and one-quarter points of the beam for investigation of any possible distortional buckling of the whole beam. Besides, the end rotation angle of the beam was recorded by rotation angle indicator, and then the rotation capacity of the beam can be defined through the end moment-rotation curve.

Experimental Results

Moment-rotation Curves and Characteristic Values of Moments

Moment-rotation curves of composite beam specimens are drawn in Figure 3. In the curve M_{cr} is concrete -cracked moment; M_y is the moment that bottom flange of steel beam reaches the yield point; M_u is the bending bearing capacity of composite beam; M_p is cross-section plastic moment of composite beam. Fig.3 illustrates applied moment M increases until the M reaches M_u where distortional buckling or local buckling of specimens occur; M decreases after the M reaches M_u .

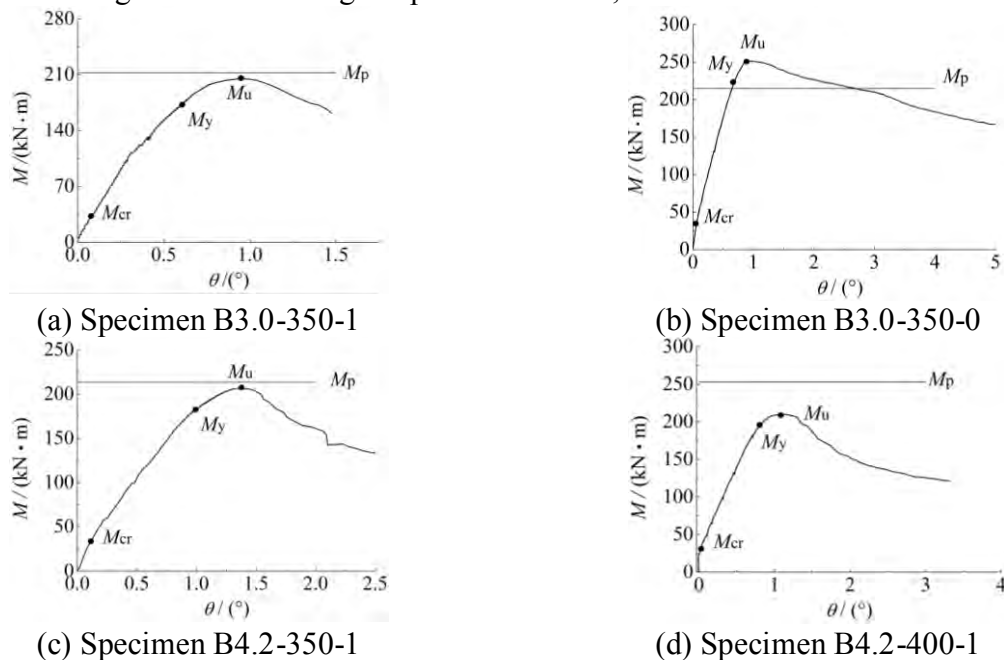


Fig. 3 Moment-rotation Curves of Composite Beam Specimens

Characteristic values of moments are given in Table 3. It can be seen that M_{cr} of all the specimens have similar value; M_{cr}/M_u of all the specimens are roughly 0.15; M_y/M_u of all the specimens are roughly 0.85.

Tab.3 Characteristic Values of Moments of Composite Beam Specimens

specimen	M_{cr} (kN · m)	M_y (kN · m)	M_u (kN · m)	M_p (kN · m)	M_{cr}/M_u	M_y/M_u	M_u/M_p
B3.0-350-1	32.9	173.0	205.1	212.2	0.16	0.84	0.97
B3.0-350-0	32.9	226.2	251.5	214.7	0.13	0.90	1.17
B4.2-350-1	32.9	180.5	206.9	213.9	0.16	0.87	0.97
B4.2-400-1	32.9	196.9	210.5	253.3	0.16	0.94	0.83

Influence of Parameters on M_u and M_u/M_p

Table 3 also illustrates the Influence of parameters on M_u and M_u/M_p :

(1) It is found from the comparison between specimen B3.0-350-0 with bending moment ratio $M_2/M_1=0$ and specimen B3.0-350-1 with $M_2/M_1=1$ that M_u decreases from 251.5 kN · m to 205.1 kN · m, and M_u/M_p also decreases from 1.17 to 0.97 when bending moment ratio between two ends of a beam increases from 0 to 1. Therefore, It is conclude that M_u and M_u/M_p decrease as bending moment ratio between two ends of a beam increases.

(2) It shows from the comparison between specimen B4.2-350-1 with height-to-thickness ratio of web $h_w/t_w=55.7$ and specimen B4.2-400-1 with $h_w/t_w=64.0$ that M_u is less affected from 206.9 kN · m to 210.5 kN · m by h_w/t_w . However, M_u/M_p decreases from 0.97 to 0.83 as h_w/t_w increases from 55.7 to 64.0.

(3) It is found from the comparison between specimen B3.0-350-1 with lateral slenderness ratio of compressive flanges $l/r_y=83.1$ and specimen B4.2-350-1 with $l/r_y=116.4$ that M_u is less affected from 205.1 kN · m to 206.9 kN · m by h_w/t_w , and M_u/M_p also is less affected by h_w/t_w . So, l/r_y has little influence on M_u and M_u/M_p when l/r_y is large.

Failure Mode

As shown in Figure 4, two types of failure mode namely distortional buckling and local buckling occurred. All the specimens in the moment case $M_2/M_1=1$ (specimen B3.0-350-1, B4.2-350-1 and B4.2-400-1) encounter distortional buckling. Because of moment gradient, specimen B3.0-350-0 in the moment case $M_2/M_1=0$ encounters local buckling.



(a) Distortional buckling (specimen B3.0-350-1)



(b) Local buckling (B3.0-350-0)

Fig. 4 Failure Mode

Finite Element Model and Verification of the Model

Finite Element Model

The FE software package Abaqus v6.10 was used in the present study. Finite element model is single beam with rigid plate at two ends of a beam to apply the bending moments M_1 and M_2 . As shown in Figure 5, the webs and flanges were modelled by four-node thin shell thin S4R with reduced integration points using six degrees of freedom per node. Eight-node solid elements

C3D8R were employed to model concrete slab. Strut elements T3D2 were employed to model the steel reinforcement bars which were embedded in the concrete slab. A group of connection elements CONN3D2 were employed to model the studs between the concrete slab and steel top flange. Rigid elements R3D4 were employed to model rigid plate at two ends of a beam.

A tri-linear curve was used to describe the stress-strain relationship for the H-shaped steel beam. A bi-linear curve was employed to describe the stress-strain relationship for the rebars. The stress-strain relation for the concrete in compression and tension was the model proposed by Chinese code for design of concrete structures (GB50010-20010). The model properties were directly adopted from the measured values of experimental specimens.

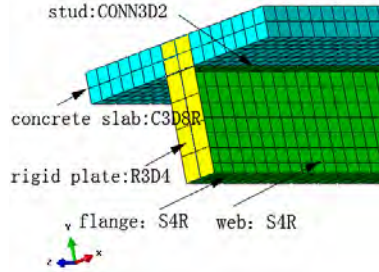


Fig. 5 Finite Element Model

Initial geometric imperfection was adopted from the first mode of elastic buckling. The maximum amplitude of geometric imperfections in the steel bottom flange used in the finite element analysis is limited to 1/1000 of span. Residual stress pattern for the welded plated steel sections was considered in the nonlinear buckling analysis.

Newton's iterative technique was used to analyze the nonlinear response of the composite beam under displacement.

Verification of the Model

Figure 6 illustrates the comparison of moment-rotation curves between FE analysis and experiment of four composite beam specimens. It can be seen that the curves derived from the nonlinear finite element analysis agree well with the experimental curves.

The bending bearing capacity M_u measured in the experiments and FE analysis are also given in Table 4. The maximum relative error between the results of test and theory is less than 10%.

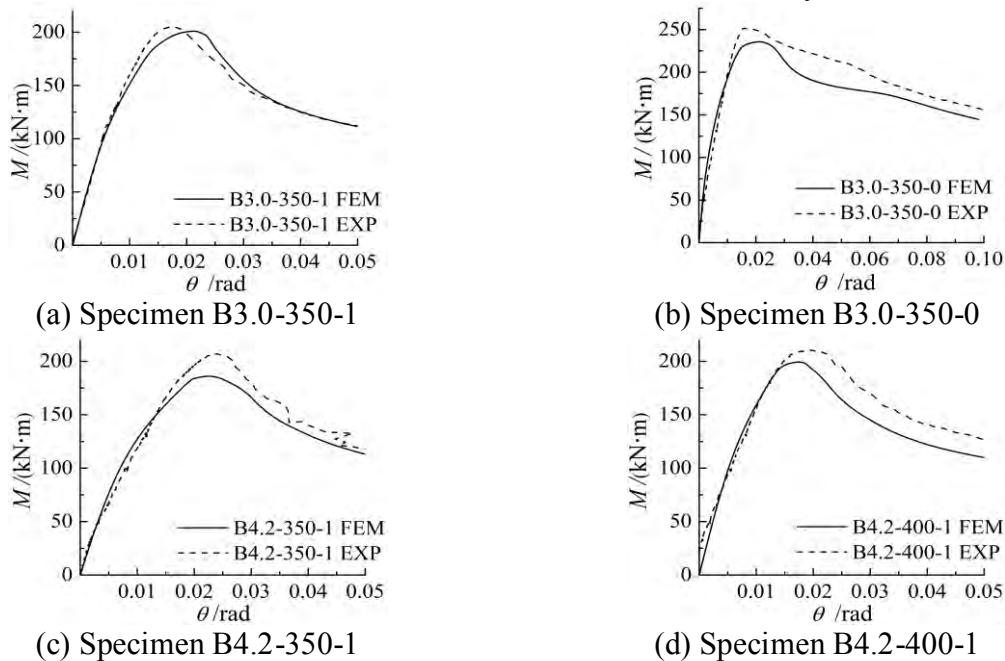


Fig. 6 Comparison of Moment-rotation Curves between FE Analysis and Experiment

Tab. 4 Comparison of Bending Bearing Capacity between FE Analysis and Experiment

Specimen	M_p (kN·m)	$M_{u,EXP}$ (kN·m)	$M_{u, FEM}$ (kN·m)	$\frac{M_{u,FEM}}{M_{u,EXP}}$
B3.0-350-1	212.2	205.1	201.3	0.98
B3.0-350-0	214.7	251.5	235.7	0.94
B4.2-350-1	213.9	206.9	186.0	0.90
B4.2-400-1	253.3	210.5	199.4	0.95

It can be seen from the above comparison that the FE model is reliable in analyzing mechanical behaviour of composite beams under negative bending.

Summary

From experimental Investigation and FEM analysis for mechanical behaviour of composite beams under negative bending, it was found as the follows:

- (1) Bending bearing capacity M_u decrease as bending moment ratio M_2/M_1 between two ends of a beam increases. Distortional buckling occurred for the case that $M_2/M_1=1$. M_u was less than cross-section plastic moment of composite beam M_p . However, local buckling took place for the case that $M_2/M_1=0$. The M_u was greater than M_p .
- (2) As the height-thickness ratio of web decreased, M_u / M_p decreases significantly.
- (3) If lateral slenderness ratio of compressive flanges is large, M_u is less affected by lateral slenderness ratio of compressive flanges.
- (4) The finite element models of four composite beams under negative bending were established. Its validity is verified by the experimental findings. It shows that finite element method is versatile and efficient in analyzing mechanical behaviour of composite beams under negative bending.

References

- [1] Daniels J. H., Fisher J. W. Static behavior of continuous composite beams. Bethlehem, PA: Lehigh University. Fritz engineering Laboratory Report No.324.2, 1967:1-85.
- [2] Johnson R.P. Distortional lateral buckling of continuous composite beams. Proceedings of the institution of civil engineers, London:Thomas Telford Services ltd, 1991:131-161.
- [3] Bradford M.A., Johnson R.P. Inelastic buckling of composite bridge girders near internal supports. Proceedings of the institution of civil engineers, London:Thomas Telford Services ltd, 1987:143-159.
- [4] Kemp A. R. Inelastic local and lateral buckling in design codes. Journal of structural engineering, 1996, 122(4): 374-382.
- [5] ZHU Pinru, GAO Xiangdu, WU Zhengsheng. Research on plastic hinge behaviour and internal moment redistribution in steel concrete continuous composite beam. Journal of Building Structures, 1990, 11(6): 26-37. (in Chinese)
- [6] FAN Jiansheng, NIE Jianguo, YE Qinghua, WANG Ting. Experimental Study on Moment Redistribution of Continuous Composite Steel—Concrete Beams with Profiled Sheeting. Journal of Building Structures, 2001, 22(2): 57-61. (in Chinese)
- [7] LIU Yang, TONG Lewei. Numerical analysis of rotation capacity of steel-concrete composite beam under negative moment. Proceeding of The 12th national symposium on advanced structure engineering. Beijing: Industrial Construction Magazine Agency, 2012: 976-981. (in Chinese)