Low Frequency Spherical Vector Hydrophone Based on the Geophone

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Abstract. In this paper, a new type of low frequency spherical vector hydrophone is designed. It can be directly installed on the underwater platform and sense the underwater acoustic particle velocity. The sensing element is a moving-coil geophone. The paper described the structure of the spherical vector hydrophone, analyzed the modal of spherical shell and calculated the influence of the size and material parameters on the stiffness of spherical sleeved rubber spring. In the test frequency range, the sensitivity of vector hydrophone is about - 205dB. The ration of the maximum and the minimum in the directivity pattern is greater than 20dB.

Introduction

With the development of underwater acoustic technology, researchers pay more attention to the low frequency underwater acoustic detection. Because the directivity of the vector hydrophone has no relation with the frequency and is cosine pattern, using the vector hydrophone to receive acoustic wave can reduce the size of underwater wet end in low frequency. Besides the directivity of the vector hydrophone, the sensitivity of the vector hydrophone is another important technical parameter. The sensitivity of hydrophone depends on the internal sensors and the acoustic quantity that the vector hydrophone measures. At present, the vector hydrophone usually senses the particle acceleration and particle velocity signals under the water[1]. They are all underwater inertial sensors. This kind of vector hydrophone is first built by Leslie[2]. The response of acoustic vector hydrophone based on acceleration sensor increases with increasing frequency at a rate of 6 dB/oct. But the sensitivity curve of acoustic vector hydrophone based on moving-coil geophone is a horizontal line. So the latter is more suitable for measuring low frequency signals.

A low frequency spherical vector hydrophone based on the moving-coil geophone is designed in this paper. A spherical vector hydrophone is placed in a rigid spherical shell and the acoustically transparent elastic rubber is filled in the space between the spherical shell and hydrophone to act as the suspension component of acoustic vector hydrophone.

Structure of Spherical Vector Hydrophone

The structure diagram of vector hydrophone can be known in Fig.1.



Fig.1 Structural diagram of acoustic vector hydrophone

In Fig.1, 1 is installing rod of acoustic vector hydrophone, 2 is the rigid spherical shell, 3 is the acoustically transparent elastic rubber, 4 is the spherical vector hydrophone and 5 is the moving-coil geophone inside the vector hydrophone.

The vibration system diagram Fig.2 can be obtained easily from Fig.1.



Fig.2 Vibration system diagram of acoustic vector hydrophone based on the geophone

The dynamics of the system were described by McConnell, when an inertial sensor such as a moving-coil geophone was imbedded in the sphere[3]

$$\frac{V_s}{V_o} = -\frac{m_o + m_i}{m_c + m_i} \left[(1 - 2j\xi_o \frac{\omega_o}{\omega} - \frac{\omega_o^2}{\omega^2}) \times (1 - 2j\xi_t \frac{\omega_t}{\omega} - \frac{\omega_t^2}{\omega^2}) - \frac{m_t}{m_c + m_i} \times (2j\xi_t \frac{\omega_t}{\omega} + \frac{\omega_t^2}{\omega^2}) \right]^{-1}$$
(1)

$$m_{i} = \frac{2}{3}\pi a^{3} \rho_{c} \frac{1 + 2(a/a_{c})^{3}}{1 - (a/a_{c})^{3}}$$
(2)

 V_s and V_o are the velocity of vector hydrophone and free-field particle velocity under the water respectively. The *R* and *k* are the damping and stiffness of acoustically transparent rubber. R_p and k_p are the damping and stiffness of the coil of the geophone. And m_t is the mechanical mass of geophone. So the resonance frequency and damping factor of geophone are ω_t and ζ_t . They are defined as $\omega_t = (k_p/m_t)^{1/2}$ and $\zeta_t = R_p/2m_t\omega_t$. m_i is the induce mass, *a* and a_c are the inner radius and outer radius of rubber. From Eq.1 and Eq.2, the dynamic characteristics of vector hydrophone can be known.

The Modal Analysis of Rigid Spherical Shell

Because the vector hydrophone is a kind of inertial sensor, the vibration of the shell will affect the acoustic signal received. To avoid the negative influence of spherical shell modal on the internal vector hydrophone, the modal analysis of the spherical shell was calculated by ANSYS software in order to make the modal frequency outside the operating frequency bandwidth of acoustic vector hydrophone. To make the acoustic vector hydrophone high operating reliability, the material of rigid spherical shell is steel, and the acoustically transparent elastic rubber is filled in the space between the spherical shell and the spherical vector hydrophone.



Fig.3 The deformation figure of steel spherical shell at 4112Hz

A three dimensional steel spherical shell model is established. Its radius is 150 mm, and the shell thickness is 5 mm.

Figure 3 is the deformation figure at 4112 Hz by calculating the modal of steel spherical shell. And it is the lowest modal frequency. As long as the work frequency is far less than the lowest modal frequency, that would not have big influence on the sensitivity of vector hydrophone.

The Stiffness of Spherical Acoustically Transparent Elastic Rubber

Because the acoustically transparent rubber is regarded as the spring that suspends the acoustic vector hydrophone. So it determines the lower limit operating frequency of acoustic vector hydrophone.

It can be known that when the acoustic vector hydrophone is vibrating in the spherical shell, the inner surface of spherical rubber moves with acoustic vector hydrophone together, and the outside surface of spherical rubber is in the stationary state as a result of the limitation of steel shell from Fig.1. So the spherical rubber can be seen the sleeved rubber spring. The finite element method can be used to calculate the stiffness.

Usually if the shore hardness is known, the shear modulus of rubber can be obtained[4]

 $G \approx 0.117 e^{0.034 HS}$

(3)

HS is the shore hardness. The unit of G is MPa. From the above content, if the dimensions of spherical rubber are determined, the stiffness can be worked out by ANSYS software from measuring the shore hardness of rubber.

A three dimensional finite element model of spherical sleeved rubber spring is constructed. The inner radius is 70mm, and the outer radius is 145mm. The analysis applies to using the Mooney Rivlin option with the element solid 186 and G=272000Pa.



Fig.4 Curve of stiffness

From Fig.4 it can be known that the stiffness is a constant when the displacement is small. But in fact, the stiffness is not a constant when the displacement changes. In order to present the change trend of spherical sleeved rubber spring's stiffness objectively, the stiffness of different dimensions of outer radius is calculated under the condition that inner radius is 70 mm. In the table.1, k_1 is the stiffness when the displacement is 1mm, and k_2 is the stiffness when the displacement is 0.1mm.

Table 1 The change of stiffness						
The outer radius[mm]	95	105	115	125	135	145
$k_1 [N/m]$	21096000	10303700	6436310	3979530	2959510	2354090
k_2 [N/m]	21168500	10909800	6592380	3981580	2959680	2354520

From table.1 it can be know that the stiffness decreases as the outer radius increases, but the trend of change gradually decreases. Under the different displacements, the stiffness presents a nonlinear

state. The greater the displacement is, the smaller the stiffness is. And the nonlinear decreases in the case of a large outer radius.

Measurement Results

Fig.5 is the material object of vector hydrophone. The spherical vector hydrophone is measured by comparing with standard hydrophone in water. Fig.6 are the measurement results. From 315Hz to 800Hz, the receiving sensitivity is about -205dB. It accords with the sensitivity characteristics of acoustic vector hydrophone based on geophone. The ration of the maximum and the minimum are more than 20dB in the directivity patterns.



Fig.5 Material object of vector hydrophone



Fig.6 Sensitivity and normalized directivity pattern

Summary

In this paper, a low frequency spherical acoustic vector hydrophone has been developed by calculating the modal of steel spherical shell and the stiffness of spherical sleeved rubber spring. From the measurement results, this design method is feasible. This kind of acoustic vector hydrophone can sense the low frequency acoustic signals.

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