

## Study on Dynamic Response Characteristics of Cu-Zeolite SCR Catalyst based on Kinetic Model

Jiao Tang<sup>1, a</sup>, Guoxiang Li<sup>1, b</sup>, Jun Zhang<sup>2, c</sup>, Xiaohua Wang<sup>2, d</sup> and Jianzhong Tao<sup>2, e</sup>

<sup>1</sup>School of Energy and Power Engineering, Shandong University, Jinan 250061, China

<sup>2</sup>Center of Research and Department, WEICHAI Power Co. Ltd., Weifang 261205, China

<sup>a</sup>tangjiao.cool@163.com, <sup>b</sup>liguox@sdu.edu.cn, <sup>c</sup>zhangjunzj@weichai.com, <sup>d</sup>wangxiaoh@weichai.com, <sup>e</sup>taojz@weichai.com

**Keywords:** diesel particulate filter; soot oxidation; soot loading model; WHTC test cycle; passive regeneration.

**Abstract.** Traditional SCR control methods can't fit the high efficiency SCR and keep the coherence of production. Model-based SCR control methods is developed to compensate the defect. A simulation model for a Cu-zeolite SCR catalyst has been developed. The model is capable of predicting the conversion of NO<sub>x</sub>, NH<sub>3</sub> slip and calculate the amount of urea on real time. It also can be used to study the impact of temperature, space velocity on NO<sub>x</sub> conversion and NH<sub>3</sub> storage. Testing validations were taken based on WHTC test cycle. The results show that the average error between calculated and measured NO<sub>x</sub> conversion efficiency is about 3.4% during the test cycle. In general, good agreement between model prediction and the experimental data was achieved.

### Introduction

Diesel Particulate Filters (DPFs) and Selective Catalytic Reduction (SCR) which is widely used to remove harmful particulate matter (PM) and NO<sub>x</sub> have become an indispensable feature of the modern diesel engines due to strict emissions [1-3]. SCR systems work by chemically reducing NO<sub>x</sub> to N<sub>2</sub>. In a lean gas stream, it is necessary to add a reductant, which is typically ammonia- NH<sub>3</sub>, to the system to enable this reaction to take place. The PM, however, can clog the DPF after long-term use and affect the operation of the engine. As too much PM accumulates in the DPF, the back pressure increases resulting in low fuel economy or other problems. This has necessitated a technology for removing the PM to ensure the efficiency during long term operation of the engine. The trapped PM can be removed by regeneration either periodically or continuously. DPF regeneration is divided into active regeneration and passive regeneration. Typically, active regeneration depends on oxidation of the soot by O<sub>2</sub> at higher exhaust temperature, which operates by injecting fuel into exhaust pipe and using Diesel Oxidation Catalysts (DOC) to oxidize it to raise the temperature to approximately 600 °C [4], and passive regeneration depends on continuous oxidation of the soot by NO<sub>2</sub> in the temperature range 200-500 °C, which operates by DOC to oxidize NO from exhaust to NO<sub>2</sub> and engine exhaust NO<sub>x</sub>/PM ratio. Numerous studies have been conducted which discuss both active and passive regeneration characteristics [5-10]. Active regeneration need much fuel and is likely to lead to DPF damage. Prolonging the interval of it or realizing pure passive regeneration is requisite for modern after treatment systems. Therefore, we need lower PM and higher NO<sub>x</sub> emission.

Urea-based SCR catalysts use aqueous urea that is injected into the exhaust stream to produce NH<sub>3</sub> as the active NO<sub>x</sub> reducing agent. The NO<sub>x</sub> contained in the engine exhaust gas then reacts with the stored NH<sub>3</sub>, which produces nitrogen and water. The amount of urea injected is controlled to provide a high NO<sub>x</sub> conversion whilst keeping the emissions of excess NH<sub>3</sub> (slip) to low values. Both demands are conflicting targets, because higher concentrations of NH<sub>3</sub> lead to better conversion, but also increased slip. It presents an interesting control challenge, especially at high conversion, because both reagents (NO<sub>x</sub> and ammonia) are toxic, and therefore an excess of either is highly undesirable.

In this study, a one-dimensional numerical model for a Cu-zeolite SCR catalyst has been developed. The model is based on kinetics developed from laboratory micro reactor data for the various NH<sub>3</sub>-NO<sub>x</sub> reactions, as well as for NH<sub>3</sub> oxidation. The kinetic scheme used is discussed and evidence for it presented. The model is capable of predicting the conversion of NO and NO<sub>2</sub>, NH<sub>3</sub> slip and the formation of N<sub>2</sub>O, as well as effects associated with NH<sub>3</sub> storage and desorption. It can improve SCR management on minimum calibrated labels, real time feedback, potential to minimize sensors and adaptable controls.

## Experimental setup

The engine used in these experiments is equipped with common rail system of BOSCH. Table 1 and Fig. 1 show relating specification and detailed information about test bench, respectively. The experiments were carried out by using AVL INDYS66JD, AVL 483, HORIBA MEXA-7100D, METTLER TOLEDO KA32s to focus on torque and speed, soot emission, concentration of NO<sub>x</sub> and O<sub>2</sub>, soot weight in DPF, respectively.

Tab.1 Test engine specifications

project	specification
Engine type	6 cylinder in-line/intercooling
Bore stroke[ mm ×mm]	108×130
Swept volume[L]	7.14
Compression ratio	18
Rated power[kW]	200
Rated speed[r/min]	2100
Max torque[N·m]	1100

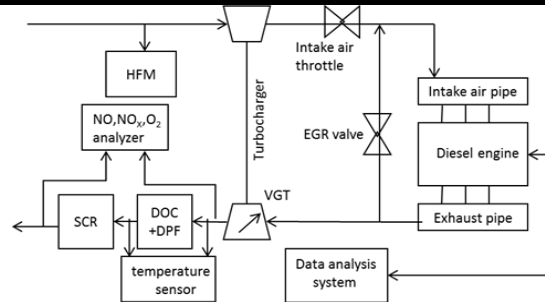


Fig.1 Schematic of experimental setup

Exhaust after-treatment system consists of DOC, DPF and SCR. Table 2 shows the detailed specification.

Tab.2 DOC and DPF specification

parameter/unit	DOC	DPF	SCR
PGM[g/L]	1.06	0.18	0
material	cordierite	cordierite	cordierite
Pore[cell/cm <sup>2</sup> ]	62	31	62
Wall thick[mm]	0.10	0.32	0.10
Diameter[mm]	267	267	267
Length[mm]	102	305	305
Volume[L]	5.7	17.0	17.0

## Model

**Reaction Kinetics.** Following the Eley-Rideal mechanism and other studies [11-15], there are 7 main chemical reactions representing the relevant dynamics in the catalytic converter as shown:





Where S is an unoccupied active catalytic site.  $(\text{NH}_3)_S$  is  $\text{NH}_3$  molecule adsorbed at S.

In these reactions, the reaction Eq.1 and Eq.2 is adsorption and desorption of  $\text{NH}_3$  on the catalyst.  $\text{NH}_3$  must be adsorbed on the active catalyst site can react with other reactants ( $\text{NO}_x$ ,  $\text{O}_2$ ) [16-20]. Eq. (3-5) is the reaction of removing  $\text{NO}_x$  and is the fast-reaction, standard-reaction and slow-reaction, respectively. Other reactions, despite of Eq. (6-7), can be neglected.

Rates of the above reactions are listed respectively as followed:

$$r_1 = k_1 e^{\frac{-E_1}{RT}} C_{\text{NH}_3} (1 - \theta) \quad (8)$$

$$r_2 = k_2 e^{\frac{-E_2(1-\alpha\theta)}{RT}} \theta \quad (9)$$

$$r_3 = k_3 e^{\frac{-E_3}{RT}} C_{\text{NO}} C_{\text{NO}_2} \theta \quad (10)$$

$$r_4 = k_4 e^{\frac{-E_4}{RT}} C_{\text{NO}} C_{\text{O}_2} \theta \quad (11)$$

$$r_5 = k_5 e^{\frac{-E_5}{RT}} C_{\text{NO}_2} \theta \quad (12)$$

$$r_6 = k_6 e^{\frac{-E_6}{RT}} C_{\text{NO}_2} \theta \quad (13)$$

$$r_7 = k_7 e^{\frac{-E_7}{RT}} C_{\text{O}_2} \theta \quad (14)$$

Where  $k$  and  $E$  are the preexponential factor and the apparent activation energy, respectively.  $R$  is the molar gas constant, 8.314 J/ (mol·K).  $T$  is the temperature in DPF, K.  $C$  is the concentration of reactant.  $\theta$  is the ratio of the existing amount of  $\text{NH}_3$  storage and max amount of  $\text{NH}_3$  ( $Q_{\text{max}}$ ) storage on the catalyst.

The key to calculate reaction rate is  $\theta$ . Summarized from above:

$$d\theta/dt = Q_{\text{max}}(r_1 - r_2 - 2 * r_3 - 4 * r_4 - 2 * r_5 - 2 * r_6 - 2 * r_7) \quad (15)$$

Generally, NO and  $\text{NO}_2$  is about 95% and 5% ratio of  $\text{NO}_x$  from exhaust gas. In order to improve the reaction rate of Eq.3, SCR catalysts are typically used downstream of DOC. It can converts NO to  $\text{NO}_2$  and approximately optimize the  $\text{NO}_2$ : NO ratio to 1:1. On this condition, the  $\text{NO}_x$  reduction activity can be improve.

Fig. 2 shows the NO conversion efficiency of DOC under the space velocity of 50000  $\text{h}^{-1}$ . As can be observed in the figure, at low temperature, NO conversion efficiency is lower and at high temperature, chemical balance limits the production of  $\text{NO}_2$ . Hence, the optimal efficiency can be obtained at temperature about 300 °C.

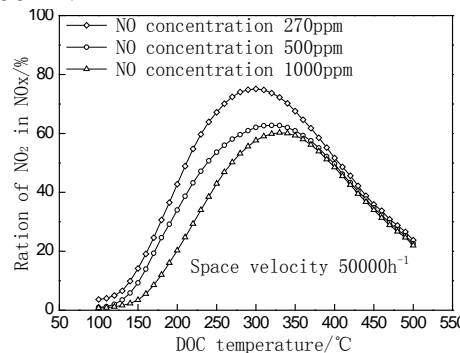


Fig.2 The conversion efficiency of NO by DOC oxidation

$\text{NO}_2$  concentration upstream DPF can be calculated:

$$C_{\text{NO}_2} = C_{\text{NO}_x} \times \eta \quad (16)$$

Where  $C_{\text{NO}_x}$  is the NO concentration upstream DOC, ppm.  $\eta$  Is the NO conversion efficiency by DOC?

**Simulation model.** SCR simulation model is established with Simulink based on the reaction kinetics equations. The  $\text{NO}_x$  sensor is upstream of the DOC. The valve of  $\text{NO}_2$ : NO ratio will change after passing through DPF. Because  $\text{NO}_2$  will react with soot in the DPF. Therefore, calculating the  $\text{NO}_2$  and NO concentration is required. The paper [21] shows the details. The sampling period is 100

ms, which is the test interval of the test-bench. Fig. 3 shows the main structure of the model and it's used to calculate the NO<sub>x</sub> conversion efficiency, NH<sub>3</sub> storage and slip.

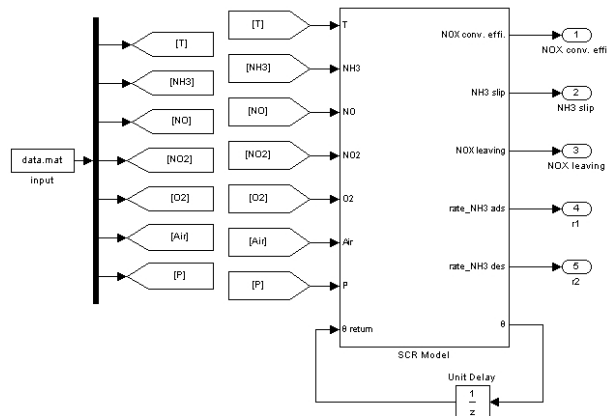


Fig.3 Simulation model of SCR

**Results and Discussion.** WHTC is applied to validate the transient accuracy of the model. During the experiment, NO<sub>x</sub> concentration at downstream SCR is obtained from test-bench while NH<sub>3</sub> concentration is obtained from sensor. Fig.4 shows NO<sub>x</sub> concentration at downstream SCR, which illustrates that the model gives a good prediction of the NO<sub>x</sub> conversion efficiency during the whole WHTC cycle. Error between calculated and measured results is controlled at 3.4%. Boundary conditions of the inputs are vital to the model, including the vaporization, hydrogenation and distribution equality of ammonia during the design of after-treatment system. Temperature inside SCR is different from the sensor value sometimes because the thermal capacity of the catalyst. While temperature means a lot to the chemical reaction rate, some researchers adopt model to simulate the temperature inside SCR, which produces a more accurate result.

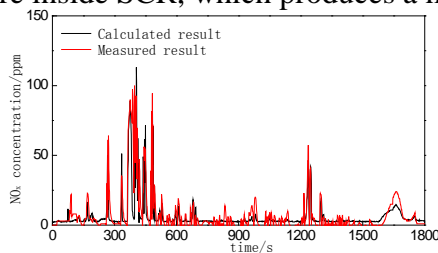


Fig.4 Comparison of calculated and measured NO<sub>x</sub> concentration

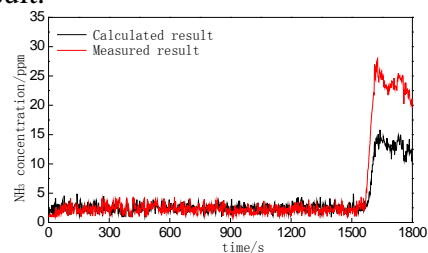


Fig.5 Comparison of calculated and measured NH<sub>3</sub> slip

Amount of NH<sub>3</sub> slip is illustrated in Fig.5. Some study[13] shows that the NH<sub>3</sub> slip prediction is much more sensitive to the inlet NH<sub>3</sub> supplied to the model than the NO<sub>x</sub> prediction. Thus a small error in the inlet NH<sub>3</sub> concentration could lead to a relatively large error in the NH<sub>3</sub> slip prediction but still give an acceptable NO<sub>x</sub> prediction. Temperature error between measured and actual value can affect the accuracy of model results. But as we can see from Fig.5, calculated and measured results show the same trend. Concerning about the high load of the latter part of WHTC cycle, which results in larger error of the temperature, makes a greater difference between the calculated result and measured result.

## Conclusion

This article describes a model-based approach for the control of urea injection amount based on reaction kinetics. Below is a summary of our study and the findings:

The NO<sub>x</sub> conversion efficiency in the SCR can be predicted by the proposed model. During the WHTC test cycle, the average error between calculated and measured results is about 3.4%.

The model not only enables after treatment systems to be designed quickly with the minimal of testing, but also aids in the detailed understanding of the chemistry characteristics of the system. This model can be further used to explore a wide range of catalyst and system scenarios, which allow us to efficiently optimize systems for varied applications and rapidly investigate many parameters with the

after treatment system (e.g. catalyst position, size, aspect ratio, urea injection strategy, etc.) and the effect on the systems of varying engine calibration (e.g. inlet temperature, inlet NO<sub>x</sub> levels, etc.).

## Acknowledgements

This work was financially supported by the Nation Natural Science Foundation (51306105) and Nation "863" project (2014AA041501).

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