

# Study on Algorithm of Multidimensional Sets Sequential Patterns Mining Based on Identification of Position

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**Keywords:** multidimensional sets; support; sequential patterns mining

**Abstract.** Introduce the concepts related to multidimensional set sequence database, and in order to mine a special multidimensional set sequence database, in which all the sequences have the same length, items inside each dimension are ordered, and dimensions are unordered, we propose an algorithm of multidimensional sets sequential patterns mining. This algorithm is on the basis of the multidimensional sets sequential patterns mining based on bitmap, first uses the representation of multidimensional sets sequential database based on identification of position to mine the single frequent itemsets, and then uses the bitmap representation to mine the multidimensional frequent sequences. In each mining, the algorithm only records frequent itemsets of single dimensional element and corresponding frequent sequences, which can reduce memory overhead, improve the counting efficiency of support and mining speed.

## Introduction

Data mining has been widely used in various fields, and the mined data patterns have been extended from single data sets inside dimensions to multiple data sets among dimensions, it is so called multidimensional mining<sup>[1][2]</sup>. The system construction of college students' innovation ability training and the research on related factor indicate that<sup>[3]</sup> the cultivation of creativity is related with many factors, such as education system, education process, family environment, personal hobbies, enterprise culture, government advocacy and social environment. Each element contains several attributes, such as education process includes the accumulation of knowledge, the cultivation of creative thinking, innovation practice, innovation achievement display etc. Each attribute contains some different items, such as innovation practice includes experimental innovation activities, innovation activities of science and technology, social practice, innovation practice base etc. Each item also has different values. These elements compose a multidimensional transaction database. How to mine the elements closely related to college students' innovation ability development from this database, and to use in the education process of students' innovation ability in order to improve the students' innovation ability, is not only related to personal development of students, but also give an important scientific support to the cultivation of application and creative ability of students. Based on this requirement, we have studied on multidimensional sets of sequential patterns mining.

## Concepts Related to Multidimensional Sets<sup>[4][5]</sup>

Single dimensional set: The set of items denoted by  $I = \{ i_1, i_2, \dots, i_m \} (m \geq 0)$ , in which  $i_j (1 \leq j \leq m)$  is called item,  $I$  represents single dimensional set on attribute set  $E$  whose value domain is  $V$ , and  $i_j \in V$ . When  $m = 0$ ,  $I$  is empty set; When  $m = 1$ ,  $I$  is called the single dimensional set with single item; When  $m \geq 1$ ,  $I$  is called real single dimensional set.

The length of single dimensional set: The number of items included in single dimensional set.

Multidimensional set: Suppose  $A = \{ E_1, \dots, E_{dim} \} (dim \geq 1)$  is any attribute set, is the single dimensional set on any attribute set,  $dim$  is the number of dimension, the value domain of each attribute is  $V_1, \dots, V_{dim}$  respectively, the multidimensional set  $t = \{ s_1, \dots, s_{dim} \} (dim \geq 1)$ , in which  $s_i (1 \leq i \leq dim)$  is the single dimensional set on attribute  $E_{dim}$ , i.e.  $s_i \subseteq V_i$ , then  $t$  is called

multidimensional set or  $dim$ -dimensional set on attribute set  $A$ . If  $s_i$  is composed of the single dimensional set with single item, then we call it multidimensional set with single item, else we call it real multidimensional set. The number of single dimensional sets contained in multidimensional set is called the length of multidimensional set.

Contain: Suppose  $t$  and  $s$  are two multidimensional sets on attribute set  $A$ , for any attribute  $E_{dim} \in A$  ( $dim \geq 1$ ),  $t_i$  is the multidimensional set of  $t$  on attribute  $E_{dim}$ ,  $s_i$  is the multidimensional set of  $s$  on attribute  $E_{dim}$ , the inclusion relation  $s_i \subseteq t_i$  are both true. So we call multidimensional set  $t$  contains multidimensional  $s$  denoted by  $t \geq s$ .

Multidimensional sets sequential patterns: Suppose  $D$  is a  $dim$ -dimensional set on  $A = \{E_1, \dots, E_{dim}\}$  ( $dim \geq 1$ ),  $B$  and  $C$  are attribute sets on  $A$ ,  $B \subset A$  and  $C \subset A$  and  $B \cap C = \emptyset$ . Suppose  $r$  is a real multidimensional set on attribute set  $B$ ,  $t$  is a real multidimensional set on attribute set  $C$ . Given a support threshold  $\zeta$ , if the number of multidimensional set  $s$  that contains both  $r$  and  $t$  in  $D$  is larger than  $\zeta$ , then call  $r \Rightarrow t$  is multidimensional sets association rules based on attribute relations  $B$  and  $C$ .

### Multidimensional Sets Database

According to the above definition of multidimensional sets, we give the multidimensional sets database to be mined as shown in Table 1. Each itemset represents a single dimensional set on each attribute, each sequence represents multidimensional set on attribute sets. To meet the need of the analysis of elements related to the innovation ability of college students, we call the attributes in this database elements  $E_{dim}$  that represent the elements related to the innovation ability of college students. Each sequence with the same dimension number  $dim$  is composed of single dimensional sets. Items are ordered inside each dimension, but not ordered among dimensions. Items in different dimensions represent different meaning, this is different from definition of traditional transaction database.

Transform the database in Table 1 into the form in Table 2, there are 3 sequences that represent 3 multidimensional sets, the length of each sequence is 3 that represents three itemsets, each itemset represents one single dimensional set on element  $E_{dim}$ . In each multidimensional set, the order of itemsets can not be changed, e.g.  $(bca)$  and  $(abc)$  are two different itemsets in this paper and represent different meaning. The item  $a$  of the single dimensional set on  $E_1$  is different from the item  $a$  in  $E_2$  and  $E_3$ , this is just to simplify the representation and no effect on mining result.

Table 1 Multidimensional sets database

<i>Sid</i>	Sequence
1	$\langle (bca)(ea)(bac) \rangle$
2	$\langle (abd)(eca)(ab) \rangle$
3	$\langle (bcd a)(deb)(acb) \rangle$

Table 2 Multidimensional sets sequence database

<i>Sid</i>	Itemsets of Sequence on $E_{dim}$		
	<i>dim=1</i>	<i>dim=2</i>	<i>dim=3</i>
1	$(bca)$	$(ea)$	$(bac)$
2	$(abd)$	$(eca)$	$(ab)$
3	$(bcd a)$	$(deb)$	$(acb)$

### The Algorithm of Multidimensional Sets Sequential Patterns Mining Based on Identification of Position

**The idea of the algorithm.** On the basis of existing sequential patterns mining algorithm<sup>[6]</sup>, to meet the need of new data model, we propose an algorithm of multidimensional sequential patterns mining based on positional identification. This algorithm uses database based on identification of position to mine frequent itemsets that can identify the order among items accurately, and uses bitmap representation to mine frequent sequences that improves counting efficiency. In each mining, the algorithm only records frequent itemsets of one dimensional element and corresponding association rules, which can reduce memory overhead. The idea of the algorithm is described as follows:

- (1) Generate the sequence database based on the identification of position  $Pos_D$ .
- (2) On element  $E_{dim}$ , mine the frequent itemsets  $FI_{k\_dim}$  first, and then mine the corresponding frequent sequence  $FS_{dim}$ .

(3) Mine frequent itemsets  $FI_{k\_dim}$ . Generate candidate itemsets  $CI_{k\_dim}$  through sequential patterns tree, and then count the support using database based on position identification to generate the frequent sequence  $FI_{k\_dim}$  on  $E_{dim}$ , and record the frequent itemsets in table  $Pos\_FI_{dim}$ .

(4) Mine frequent sequence  $FS_{dim}$ . Generate candidate sequences  $CS_{dim}$  through sequential patterns tree constructed by the frequent sequence  $FS_{dim-1}$  of the dimension before current dimension element and frequent itemsets  $FI_{k\_dim}$  of current dimension element, and count the support by bitmap representation to generate the multidimensional frequent sequence  $FS_{dim}$ , and then record the frequent sequences in table  $Bit\_FS_{dim}$ .

**Description of algorithm.** Input: Multidimensional sets sequence database based on identification of position  $Pos\_D$ ,  $min\_support$

Output: Multidimensional sets frequent sequential pattern  $FS_{dim}$

- ① for each dimension element  $E_{dim}$
- ②  $FI_{1\_dim} = generate(Pos\_D)$ ; //  $FI_{1\_dim}$  is frequent 1-itemsets on the  $dim$ th dimension element  $E_{dim}$
- ③ for ( $k = 2$ ;  $FI_{k-1\_dim} \neq \emptyset$ ;  $k++$ ) // generate frequent  $k$ -itemsets  $FI_{k\_dim}$  on  $E_{dim}$
- ④  $CI_{k\_dim} = generate\_CI(FI_{k-1\_dim})$ ; //  $CI_{k\_dim}$  is candidate  $k$ -itemsets on  $E_{dim}$
- ⑤  $FI_{k\_dim} = generate\_frequent\_kitemsets(CI_{k\_dim}, Pos\_FI_{dim})$ ; //  $Pos\_FI_{dim}$  is frequent table on  $E_{dim}$
- ⑥ if ( $dim == 1$ ) // generate frequent 1-sequences  $FS_1$
- ⑦  $FS_1 = FI_{k\_dim}$ ; //  $FS_1$  is composed of frequent  $k$ -itemsets on the 1st dimension element  $E_1$
- ⑧ else if ( $FS_{dim-1} \neq \emptyset \ \&\& \ FI_{k\_dim} \neq \emptyset$ ) // generate multidimensional frequent sequential patterns  $FS_{dim}$
- ⑨  $CS_{dim} = generate\_CS(FS_{dim-1}, FI_{k\_dim})$ ; //  $CS_{dim}$  is the candidate  $dim$ -sequences
- ⑩  $FS_{dim} = generate\_frequent\_sequences(CS_{dim}, Pos\_FI_{dim}, Bit\_FS_{dim})$ ;
- ⑪ return  $FS_{dim}$ ; //  $FS_{dim}$  is frequent  $dim$ -sequences

## The Description of Algorithm Flow

This paper takes multidimensional sets sequence database in Table 2 as example to describe the algorithm flow, and supposes the minimum support count is  $min\_support = 2$ .

**Generate multidimensional sequence database based on identification of position  $Pos\_D$ .** Save the sequence database of Table 2 into  $Pos\_D$  shown in Table 3. Record the occurrence position of each item on each dimension element in  $Pos\_D$ . For example, the 1st element  $E_1$  of sequence 1 is the itemset  $(bca)$ , in which the occurrence position of item  $a$  is 3, so noted as  $Pos(a) = 3$ , the occurrence position of item  $b$  is 1, so noted as  $Pos(b) = 1$ , the occurrence position of item  $c$  is 2, so noted as  $Pos(c) = 2$ , while item  $d$  doesn't occur, so noted as  $Pos(d) = 0$ .

**Generate frequent  $k$ -itemsets  $FI_{k\_dim}$  on each dimension element  $E_{dim}$ .**

**Generate frequent  $k$ -itemsets  $FI_{k-1}$  on the 1st dimension element  $E_1$ .**

**Generate frequent 1-itemsets  $FI_{1-1}$  on  $E_1$ .** (1) Take  $dim = 1$ ,  $Sid = 1$ , scan the item  $a$  in database  $Pos\_D$  longitudinally. If the value of  $Pos(a)$  is not 0, add 1 to support( $a$ ). (2) Add 1 to  $Sid$ , continue to perform the above operation until  $Sid = 3$ . If support( $a$ )  $\geq min\_support$ , then  $(a) \in FI_{1-1}$ , and record in  $Pos\_FI_{dim}$  as shown in Table 4; else  $(a) \notin FI_{1-1}$ . (3) Continue to scan next item  $b$  until to  $d$ , all of the frequent 1-itemsets  $FI_{1-1}$  on 1st dimension element  $E_1$  are generated, which are  $(a)$ ,  $(b)$ ,  $(c)$ ,  $(d)$  as shown in Table 4.

Table 3 Multidimensional sets sequence database based on identification of position  $Pos\_D$

Sid	Pos ( $E_{dim}$ )											
	dim = 1				dim = 2				dim = 3			
	a	b	c	d	a	b	c	d	e	a	b	c
1	3	1	2	0	2	0	0	0	1	2	1	3
2	1	2	0	3	3	0	2	0	1	1	2	0
3	4	1	2	3	0	3	0	1	2	1	3	2

**Generate candidate 2-itemsets  $CI_{2-1}$  on  $E_1$ .** Construct the sequential patterns tree<sup>[8]</sup>, *root* is the root node. Its subnodes formed the first layer nodes are the first items of  $CI_{2-1}$  composed of all the frequent 1-itemsets on 1st dimension element. The subnodes of first layer nodes composed of their sibling nodes, formed the second layer nodes, and are the second items of  $CI_{2-1}$ . For example, in Fig. 1, the father node of (*a*) is *root*, the subnodes of *root* are (*a*), (*b*), (*c*), (*d*), so the subnodes of (*a*) are its sibling nodes (*b*), (*c*), (*d*). And the candidate 2-itemsets  $CI_{2-1}$  are (*ab*), (*ac*), (*ad*), (*ba*), (*bc*), (*bd*), (*ca*), (*cb*), (*cd*), (*da*), (*db*), (*dc*).

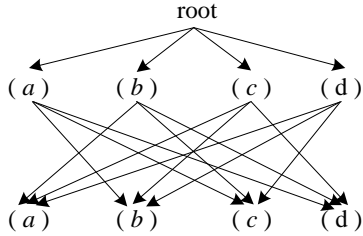


Fig.1 Candidate 2-itemsets  $CI_{2-1}$  on  $E_1$

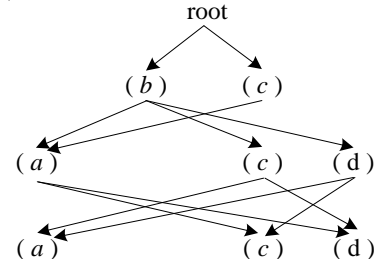


Fig.2 Candidate 3-itemsets  $CI_{3-1}$  on  $E_1$

**Generate frequent 2-itemsets  $FI_{2-1}$  on  $E_1$ .** (1) Take one candidate 2-itemset  $CI_{2-1}$ , such as (*ba*). Take  $dim = 1$ ,  $Sid = 1$ , scan (*b*) and (*a*) of  $FI_{1-1}$  in Table 4. If  $Pos(a) \neq 0$ ,  $Pos(b) \neq 0$ ,  $Pos(a) > Pos(b)$  are all true, which indicate that (*a*) and (*b*) both occur, and (*a*) is located behind (*b*), so add 1 to support(*ab*), and record  $Pos(ba) = Pos(a)$ ; else record  $Pos(ba) = 0$ . (2) Increase  $Sid$  until  $Sid = 3$ . If support(*ab*)  $\geq min\_support$ , then (*ba*)  $\in FI_{2-1}$ , record (*ab*) in table  $Pos\_FI_{dim}$ , as shown in Table 4; else (*ba*)  $\notin FI_{2-1}$ . (3) Continue to take next candidate 2-itemset  $CI_{2-1}$  until to the end, and then generate all the frequent 2-itemsets  $FI_{2-1}$  on  $E_1$ , which are (*ba*), (*bc*), (*bd*) and (*ca*).

Table 4 Frequent itemsets table on the  $dim$ th element  $E_{dim} - Pos\_FI_{dim}$

Sid	$FI_{k-dim} (dim = 1)$								
	$FI_{1-1} (k = 1)$				$FI_{2-1} (k = 2)$				$FI_{3-1} (k = 3)$
	(a)	(b)	(c)	(d)	(ba)	(bc)	(bd)	(ca)	(bca)
1	3	1	2	0	3	2	0	3	3
2	1	2	0	3	0	0	3	0	0
3	4	1	2	3	4	2	3	4	4
Sid	$FI_{k-dim} (dim = 2)$			$FI_{k-dim} (dim = 3)$					
	$FI_{1-2} (k = 1)$		$FI_{2-2} (k = 2)$	$FI_{1-3} (k = 1)$			$FI_{2-3} (k = 2)$		
	(a)	(e)	(ea)	(a)	(b)	(c)	(ab)	(ac)	
1	2	1	2	2	1	3	0	3	
2	3	1	3	1	2	0	2	0	
3	0	2	0	1	3	2	3	2	

Note:  $Pos\_FI_{dim}$  only records frequent  $k$ -itemsets on one dimension element at one time, here lists records for three times.

**Generate candidate 3-itemsets  $CI_{3-1}$  on  $E_1$ .** In sequential patterns tree, the first layer nodes are the first items of frequent 2-itemsets  $FI_{2-1}$ , the second layer nodes are the second items of frequent 2-itemsets  $FI_{2-1}$ , the third layer nodes are composed of the sibling nodes of the second layer nodes. For example, in Fig. 2, the father node of (*a*) is (*b*) whose subnodes are (*a*), (*c*) and (*d*), so the subnodes of (*a*) are its sibling nodes (*c*) and (*d*). And the candidate 3-itemsets  $CI_{3-1}$  are (*bac*), (*bda*), (*bca*), (*bcd*), (*bda*), (*bdc*), (*cad*).

**Generate frequent 3-itemsets  $FI_{3-1}$  on  $E_1$ .** (1) Take one candidate 3-itemset  $CI_{3-1}$ , e.g. (*bca*). Take  $dim = 1$ ,  $Sid = 1$ , scan (*bc*) and (*a*) in Table 4. If  $Pos(bc) \neq 0$ ,  $Pos(a) \neq 0$ ,  $Pos(a) > Pos(bc)$  are all true, which indicate (*a*) and (*bc*) both occur, and (*a*) is located behind (*bc*), then add 1 to support(*bca*), and record  $Pos(bca) = Pos(a)$ ; else record  $Pos(bca) = 0$ . (2) Increase  $Sid$  until  $Sid = 3$ . If support(*bca*)  $\geq min\_support$ , then (*bca*)  $\in FI_{3-1}$ , record (*bca*) in table  $Pos\_FI_{dim}$  as shown in Table 4; else (*bca*)  $\notin FI_{3-1}$ . (3) Continue to take next candidate 3-itemset  $CI_{3-1}$  until to the end, then generate all the frequent 3-itemsets  $CI_{3-1}$  on  $E_1$ , which is (*bca*).

**Generate candidate  $k$ -itemsets  $CI_{k-1}$  on  $E_1$ .** Construct sequential patterns tree, the  $(k-1)$ th items of frequent  $(k-1)$ -itemsets  $FI_{k-1-1}$  compose the  $(k-1)$ th layer nodes, whose sibling nodes compose the subnodes of it. Use generate\_C ( $FI_{k-1-dim}$ ) to generate candidate  $k$ -itemsets  $CI_{k-1}$ .

**Generate frequent k-itemsets  $FI_{k-1}$  on  $E_1$ .** (1) Take one candidate  $k$ -itemset  $CI_{k-1}$ , take  $dim = 1$ ,  $Sid = 1$ , scan the top  $k-1$  item and  $k$ th item of  $CI_{k-1}$  in Table 4. If both values are not 0, and the value of  $k$ th item is greater than top  $k-1$  item, then add 1 to  $support(CI_{k-1})$ , and record the value of  $Pos(CI_{k-1})$  the same as the value of  $k$ th item; else record the value of  $Pos(CI_{k-1})$  as 0. (2) Increase  $Sid$  until  $Sid = 3$ . If  $support(CI_{k-1}) \geq min\_support$ , then  $CI_{k-1} \in FI_{k-1}$ , record  $CI_{k-1}$  in table  $Pos\_FI_{dim}$ , as shown in table 4; else  $CI_{k-1} \notin FI_{k-1}$ . (3) Continue to take next candidate  $k$ -itemset  $CI_{k-1}$ , until to the end, then generate all the frequent  $k$ -itemsets  $FI_{k-1}$  on  $E_1$ .

**Generate frequent k-itemsets  $FI_{k-dim}$  on  $E_{dim}$ .** Add 1 to  $dim$ , the process of algorithm is the same as section 2.1, until to the last dimension element. Record the frequent  $k$ -itemsets  $FI_{k-dim}$  on the  $dim$ th dimension element in table  $FI_{k-dim}$ .

**Generate multidimensional frequent sequences  $FS_{dim}$ .**

**Generate frequent 1-sequences  $FS_1$ .** If  $dim = 1$ , frequent 1-sequences  $FS_1$  is composed of the frequent  $k$ -itemsets  $FI_{k-1}$  on  $E_1$ , then save  $FI_{k-1}$  of Table 4 into frequent sequence table  $Bit\_FS_{dim}$  in the form of bitmap, as shown in Table 5. The value is not 0 in Table 4 will be recorded as 1 in Table 5 which represents occurrence, and the value is 0 will be still recorded as 0 which represents not occurrence. For example, in Table 4, if  $Sid = 1$ ,  $Pos(a) = 3$ , then record  $Bit(a) = 1$  in Table 5. And then, clear table  $Pos\_FI_{dim}$  in order to record the frequent  $k$ -itemsets on next dimension element.

**Generate candidate 2-sequences  $CS_2$ .** If  $dim = 2$ , construct sequential patterns tree, the root node is *root*. Its subnodes formed the first layer nodes are the first itemsets of  $CS_2$  composed of all the frequent 1-sequences  $FS_1$ . The subnodes of first layer nodes formed the second layer nodes are the second itemsets of  $CS_2$ , which are composed of all the frequent  $k$ -itemsets  $FI_{k-2}$  on the 2nd dimension element  $E_2$  in Table 4. As shown in Fig. 3.

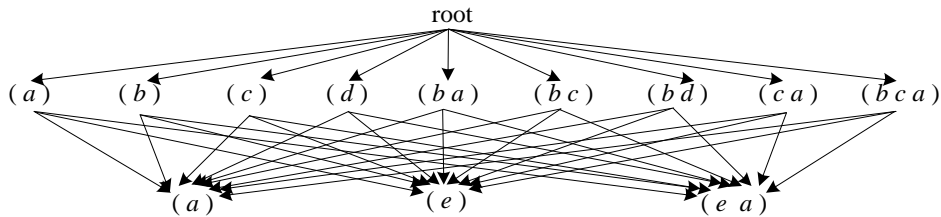


Fig.3 Candidate 2\_sequence  $CS_2$

**Generate frequent 2-sequence  $FS_2$ .** (1) Record  $FS_1$  of table  $Bit\_FS_{dim}$  into table  $Temp\_FS_{dim}$ , as shown in Table 6. (2) Take one candidate 2-sequence  $CS_2$ , e.g.  $(ca)(e)$ . Take  $Sid = 1$ , scan  $(ca)$  in Table 6, and scan  $(e)$  with  $dim = 2$  in Table 4. If both  $Bit(ca)$  and  $Pos(a)$  are not 0, which indicates  $(ca)$  and  $(e)$  all occur, then add 1 to  $support((ca)(e))$ , and record  $Bit((ca)(e)) = 1$ ; else record  $Bit((ca)(e)) = 0$ . (3) Increase  $Sid$  until  $Sid = 3$ . If  $support((ca)(e)) \geq min\_support$ , then  $(ca)(e) \in FS_2$ , record  $(ca)(e)$  in table  $Bit\_FS_{dim}$ , as shown in Table 5; else  $(ca)(e) \notin FS_2$ . (4) Continue to take next candidate 2-sequence  $CS_2$ , until to the end, and generate all the frequent 2-sequences  $FS_2$ , they are  $(a)(a)$ ,  $(a)(e)$ ,  $(a)(ae)$ ,  $(b)(a)$ ,  $(b)(e)$ ,  $(b)(ae)$ ,  $(c)(e)$ ,  $(d)(e)$ ,  $(ba)(e)$ ,  $(bc)(e)$ ,  $(bd)(e)$ ,  $(ca)(e)$ ,  $(bca)(e)$ . As shown in Table 5.

And then, clear table  $Pos\_FI_{dim}$  to record the frequent  $k$ -itemsets on next dimension element.

Table 5 Frequent sequences table  $Bit\_FS_{dim}$

Sid	Bit ( $FS_{dim}$ )											
	FS <sub>1</sub> (dim = 1)						FS <sub>2</sub> (dim = 2)					
	(a)	(b)	(c)	(d)	(ba)	(bc)	(bd)	(ca)	(bca)	(a)(a)	(a)(e)	(a)(ae)
1	1	1	1	0	1	1	0	1	1	1	1	1
2	1	1	0	1	0	0	1	0	0	1	1	1
3	1	1	1	1	1	1	1	1	1	0	0	0
Sid	Bit ( $FS_{dim}$ )											
	FS <sub>2</sub> (dim = 2)											
	(b)(a)	(b)(e)	(b)(ae)	(c)(e)	(d)(e)	(ba)(e)	(bc)(e)	(bd)(e)	(ca)(e)	(bca)(e)	(e)	
1	1	1	1	1	0	1	1	0	1	1	1	
2	1	1	1	0	1	0	0	1	0	0	0	
3	0	1	0	1	1	1	1	1	1	1	1	

Note: Table  $Bit\_FS_{dim}$  only record frequent  $dim$ -sequences corresponding to current dimension, here lists two records.

**Generate candidate sequence  $CS_{dim}$ .** Add 1 to  $dim$ , construct sequential patterns tree, the root node is  $root$ , the first layer nodes are composed of all frequent  $(dim-1)$ -sequences  $FS_{dim-1}$ , the second layer nodes are composed of all frequent  $k$ -itemsets on  $dim$ th dimension element, and use  $generate\_CS (FS_{k\_dim-1}, FI_{k\_dim})$  to generate candidate sequence  $CS_{dim}$ .

**Generate frequent sequence  $FS_{dim}$ .** (1) Record  $FS_{dim-1}$  of table  $Bit\_FS_{dim}$  into table  $Temp\_FS_{dim}$ . (2) Take one candidate sequence  $CS_{dim}$ . Let  $Sid = 1$ , scan the top  $dim-1$  itemset of  $CS_{dim}$  in table  $Temp\_FS_{dim}$ , and scan the  $dim$ th itemset of  $CS_{dim}$  in table  $Pos\_FI_{dim}$ , if both are not 0, indicates that both occur, then add 1 to  $support(CS_{dim})$ , and record  $Bit(CS_{dim}) = 1$ ; else record  $Bit(CS_{dim}) = 0$ . (3) Increase  $Bit(CS_{dim}) = 0$  until to the end. If  $support(CS_{dim}) \geq min\_support$ , then  $CS_{dim} \in FS_{dim}$ , and record  $CS_{dim}$  in table  $Bit\_FS_{dim}$ ; else  $CS_{dim} \notin FS_{dim}$ . (4) Continue to take next candidate sequence  $CS_{dim}$  until to the end, and then generate all the frequent sequences  $FS_{dim}$ .

Table 6 Temporary frequent sequences table  $Temp\_FS_{dim}$

$Sid$	$FS_1$									
	(a)	(b)	(c)	(d)	(ba)	(bc)	(bd)	(ca)	(cba)	
1	1	1	1	0	1	1	0	1	1	
2	1	1	0	1	0	0	1	0	0	
3	1	1	1	1	1	1	1	1	1	

## Conclusions

The algorithm of multidimensional set sequential patterns mining can mine the sequence database of teaching effect, in which the items are in order while itemsets are not. Through the mining, we can find the relationships among elements. And in the practical application, according to the learning habits of student, as well as the relationship between the grades of courses related to practice teaching and innovation achievements, we can mine the learning state in which they can get good effect of cultivation of innovation ability. This can help to adjust teaching method, fully develop the students' potential, and improve teaching quality. The algorithm can be further optimized in the candidate set and candidate sequence, i.e. effective pruning in the generation of  $CI_{k\_dim}$  and  $CS_{dim}$  to improve the efficiency, and should add different weights in items, which is a study emphasis in further research.

## Acknowledgements

Project supported by the Inner Mongolia Autonomous Region Natural Science Foundation (2011MS0914).

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