

The study of tilt effect on the preloaded oil pad of hydrostatic turntable

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Abstract: A new method is proposed to analyze the bearing properties of the preloaded oil pad in different compensation method when the hydrostatic turntable tilts. Energy equation and Reynolds equation are coupled and solved in this paper. Results show that the bearing properties of the preloaded oil pad will be significantly reduced when tilting. And load carrying capacity even decreases by 42% at maximum tilt angle. All the heat produced in the lubricant film by friction also has a significant impact on the bearing properties of the preloaded oil pad.

Introduction

Hydrostatic turntables are well known for their high load-carrying capacity, low friction and negligible wear, so they are widely used to carry machine and the large workpiece in the heavy-duty machine tool. Furthermore, numerous have paid attention to the various aspects of the characteristics of hydrostatic turntable or bearing^[1-13]. According to references review, we found the investigation of tilt effect is not sufficient.

The preloaded oil pad is an important part of the supporting system of hydrostatic turntable. In the design of the pad, it is generally assumed that the pad surface parallels to the guide surface. However, due to the impact of partial load, manufacturing errors and local deformation, it cannot be avoided that the turntable tilts during being used. Heat is an important factor that can affect the bearing properties of the hydrostatic turntable system. And the increase of the oil temperature not only makes the load carrying capacity lower, but also leads to the thermal deformation of the turntable. A new method is proposed to analyze the bearing properties of the preloaded oil pad in different compensation method when the hydrostatic turntable tilts. Energy equation and Reynolds equation are coupled and solved in this paper.

Theoretical derivation

Reynolds equation

In this study, it is assumed that thin film lubrication theory is applicable. So the Reynolds equations can be written as:

$$\frac{\partial}{\partial r} \left(\frac{r \rho h_r^3}{12\eta} \frac{\partial p}{\partial r} \right) + \frac{1}{r} \frac{\partial}{\partial \varphi} \left(\frac{\rho h_r^3}{12\eta} \frac{\partial p}{\partial \varphi} \right) = r \rho v_z \quad (1)$$

We have the simplified energy equations as follows:

$$\rho c \left(u_r \frac{\partial T}{\partial r} + \frac{u_\varphi}{r} \frac{\partial T}{\partial \varphi} \right) = K \frac{\partial^2 T}{\partial z^2} + \eta \left[\left(\frac{\partial u_r}{\partial z} \right)^2 + \left(\frac{\partial u_\varphi}{\partial z} \right)^2 \right] \quad (2)$$

$$\eta = \eta_0 e^{-\beta(T-T_0)} \quad (3)$$

$$\rho = \rho_0 (1 - \lambda(T - T_0)) \quad (4)$$

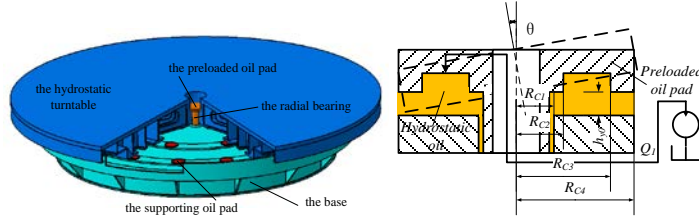


Fig.1.the main structure of the hydrostatic turntable. 2.the preloaded oil pad

Hydrostatic preloaded oil pad

The main structure of the hydrostatic turntable system is shown in Fig.1. The table and the base are its main structural parts. Meanwhile, the supporting oil pad, the preloaded oil pad and the radial bearing is the main component of the turntable support system. The form of the preloaded oil pad is generally annular oil pad, as shown in Fig.2. $R_{C1}, R_{C2}, R_{C3}, R_{C4}$ are the structural parameters of the pad. h_{y0} is the theoretical film thickness. Q_1 is flow rate of the pad. θ is the tilt angle.

When the preloaded oil pad tilts, the film thickness distribution can be calculated as:

$$h = h_y + r \tan(\theta) \cos(\varphi) \quad (5)$$

So the recess pressure of the preloaded oil pad can be calculated as:

$$P_{y0} = \frac{Q_1}{\frac{h_{y0}^3}{\eta_0} \left(\int_0^{2\pi} \left(\frac{-RH^3}{12\eta_a} \frac{\partial p}{\partial R} \right)_{\bar{R}=1} d\varphi - \int_0^{2\pi} \left(\frac{-RH^3}{12\eta_a} \frac{\partial p}{\partial R} \right)_{\bar{R}=\frac{R_{C1}}{R_{C4}}} d\varphi \right)} \quad (6)$$

When the pad uses a constant-pressure oil pump for supply and the capillary restrictor for compensation, the recess pressure of hydrostatic oil pad can be calculated as:

$$P_{y0} = P_s - \frac{128\eta_a l_c Q_1}{\pi d_c^4} \quad (7)$$

As for the hydrostatic oil pad using the orifice restrictor, the recess pressure of hydrostatic oil pad can be calculated as:

$$P_{y0} = P_s - \frac{\rho}{2} \left(\frac{4Q_1}{\pi a d_o^2} \right)^2 \quad (8)$$

By integrating oil film pressure distribution, we can obtain the load carrying capacity of the oil pad.

$$wf_y = R_{C4}^2 P_{y0} \int_0^{2\pi} \int_{R_{C1}/R_{C4}}^1 \bar{p} \bar{R} d\bar{R} d\varphi \quad (9)$$

The load carrying capacity respectively derivation of the film thickness \bar{H} and the axial velocity of guide rail surface v_z , and we can get the stiffness coefficients and the damping coefficients of the oil pad.

$$K_z = \frac{\partial wf}{h_0 \partial H} \quad (10)$$

$$C = \frac{\partial wf}{h_0 \partial v_z} \quad (11)$$

The main design parameters of the oil pad and the restrictor are shown in Tab.1.

Tab.1

Parameter	Value	Parameter	Value
R_{C1} (mm)	175	R_{C2} (mm)	220
R_{C3} (mm)	235	R_{C4} (mm)	290
h_0 (mm)	0.1	Q_1 (m ³ /s)	1.73e-4
p_s (Mpa)	6	l_c (mm)	80
dc (mm)	2	a	0.65
do (mm)	2	η_0 (pa.s)	0.091
ρ (kg/m ³)	872		

Result and discussion

In this paper, when the flow supply means is respectively constant flow supply, capillary restrictor and orifice restrictor, various bearing properties of hydrostatic annular preloaded oil pads with tilt and thermal effects have been calculated. In order to analyze the results, some parameters like: load carrying capacity, recess pressure, stiffness and damping coefficients have been normalized by divide these parameters with no tilting respectively or other parameters.

Recess pressure

Fig.3 shows the recess pressure curves at different tilt angles. As shown in the figure, the recess pressure decreases with increasing tilt angle, and initially recess pressure will be slightly decreased when the dimensionless tilt angle $\theta^* < 0.3$, then recess pressure of the pad will be almost linearly decreased. At the same time, we found that the variation law of recess pressure with tilt angles will be changed when the flow supply means is different. First of all, using constant flow supply, the recess pressure is reduced by 44% at maximum tilt angle. Then, using orifice restrictor, it is reduced by 36% at maximum tilt angle. At last, using capillary restrictor, it is reduced by 29% at maximum tilt angle.

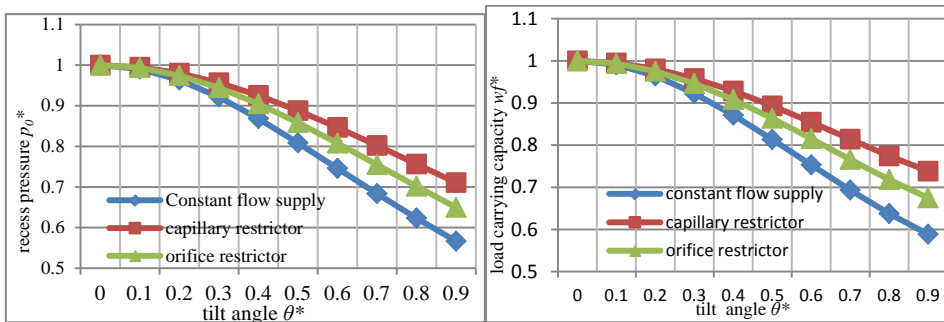


Fig.3 the recess pressure curves Fig.4 the load carrying capacity curves

Load carrying capacity

The load carrying capacity curves at different tilt angles are shown in Fig.4. As shown in the figure, the load carrying capacity decreases with increasing tilt angle, similar to the variation law of the recess pressure. When constant flow supply is used, the load carrying capacity is reduced by 42% at maximum tilt angle. Using orifice restrictor, it is reduced by 33%. There is no doubt that the best way to compensate is capillary restrictor, and it is reduced by 27% at maximum tilt angle.

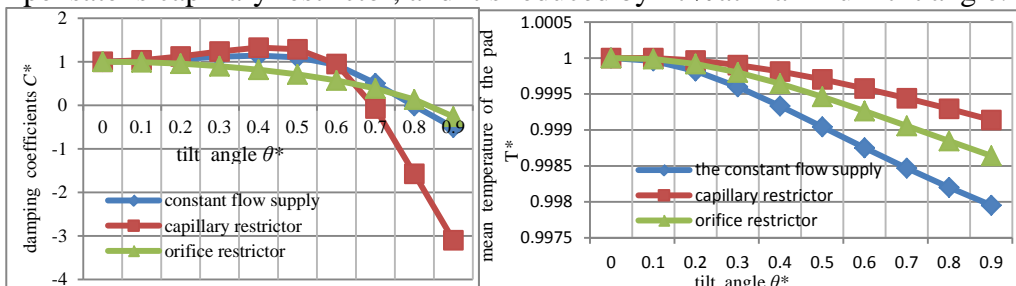


Fig.5 damping coefficients curves Fig.6 temperature of the pad curves

Damping coefficients

The variation law of damping coefficients curves is shown in Fig.5. There is huge impact on damping coefficients because of tilt, and the damping coefficient even is negative when the tilt angle is larger. For the constant flow supply and capillary restrictor, the damping coefficients are consistent on the overall trend, which are slightly increased first and then a sharp decline in, but their biggest drop is different. When using capillary restrictor, it is maximally reduced by 409.8%. While using the constant flow supply, it is maximally reduced by 151.2%. When using orifice restrictor, the damping coefficient is smoothly decreased with the increase of tilt angle and maximally by 126.1%.

Temperature of the pad

The mean temperature of the pad will be decreased with the increasing of tilt angle, as shown in Fig. 6. Here, we can find that reduction is less than 0.2%. And different restrictors also can influence it. While, when using the constant flow supply, the maximum amount of impact is about 0.2%, and when using capillary restrictor, the number is about 0.1%. There, temperature has a strong influence on performance of the pad, and the influence rate of thermal effects to load carrying capacity curves are shown in Fig. 7. It can be calculated as $P_{wf} = 100\% * (w_{f_n} - w_{f_t}) / w_{f_n}$. While, w_{f_n} is the load carrying capacity without considering the influence of the pad, and w_{f_t} is the load carrying capacity considering the influence of the pad. Seen from the figure, the influence of temperature on the load carrying capacity is around 0.4% and increases with the increase of the tilt angle. Meanwhile, when using the constant flow supply, the influence is the largest, and it is the smallest when using capillary restrictor.

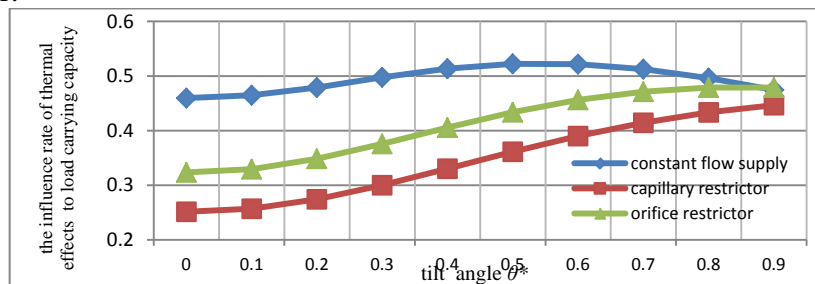


Fig.7 the influence rate of thermal effects load carrying capacity curves

Conclusion

In this paper, energy equation and Reynolds equation are established when the preloaded oil pad of the hydrostatic turntable tilts, and the influence of tilt on pad bearing properties is analyzed using different supply systems. The results show that the tilt has a greater impact on recess pressure, the load carrying capacity and damping. Thereinto, recess pressure and the load carrying capacity reduce by 10% to 50% at the maximum tilt angle, and the reduction in damping is even more than 100%. Different methods of supply systems may also affect the anti-tilt ability of the pad. In general, constant pressure supply system is better than constant flow supply system, and this is due to the constant pressure supply will increase the compensation effect when tilting to make its anti-tilt ability improved.

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