

# Evaluation of Binarization Methods Using Global Threshold for Chinese Rubbing Images

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**Abstract**—There are a huge amount of historical Chinese rubbing images in different library that have not been exploited electronically. However, many invaluable collections of rubbing images are already digitized and indexed for consulting, exchange and distant access purposes which protect them from direct manipulation. In many applications of digital rubbing image, the use of binary images can decrease the computational cost of the succeeding steps compared to using gray-level images. Thresholding is a simple but effective tool to separate characters from the background for rubbing image. In this paper, five global thresholding algorithms such as Histogram Isodata method, Minimum Cross Entropy(MCE) method, Kittler's method, Maximum Entropy method, Otsu's method and Fuzzy C-Means(FCM) clustering thresholding method that had been used widely by scholars have been researched. Two quantitative measure of comparison is provided by the Peak Signal to Noise Ratio (PSNR) and Mean Square Error (MSE) of the rubbing image for segmentation results.

**Keywords**-Thresholding; Chinese rubbing image, Otsu's thresholding; image segmentation; FCM

## I. INTRODUCTION

With the computer technology and the rapid development of communication technology, modern society has gradually entered into the information age. The decreasing cost of digital image capture and processing hardware, especially CCD-scanned (Charge Coupled Device) photodiode arrays and memory chips, has made it possible to consider approaches to OCR (Optical Character Recognition) that have not been practical before. The traditional record information, storing the information carrier (such as papered) has been unable to meet those rapid require [1]. Much valuable information, such as Chinese calligraphy, art works and others, is usually scanned into digital document images to be stored, transmitted, displayed and printed. In order to ensure the effectively process of the document image, document image segmentation research is particularly important. At the same time, document image binarization is an essential preprocessing step in many document-related applications, such as cleanup, storage, transmission, and offline analysis and recognition. In many applications of image processing, the use of binary images can decrease the computational cost of the succeeding steps compared to using gray-level images. Thresholding is a simple but effective tool to separate characters from the background for rubbing image. Depending on the application, the foreground can be

represented by gray-level 0, that is, black as for text, and the background by the highest luminance for document paper that is 255 in 8-bit images or conversely the foreground by white and the background by black[2][3]. At the same time, the global thresholding approach is less sensitive to noise and does not require elaborate enhancement which is usually sensitive to the individual image characteristics and requires a lot of supervision. But, there is that the lack of objective measures to assess the performance of various thresholding algorithms for rubbing image segmentation. The main difficulty of image thresholding could be come from various factors, such as non-stationary and correlated noise, ambient illumination, busyness of gray levels within the object and its background, inadequate contrast, and object size not commensurate with the scene, complicate the thresholding operation [4].

In this study, we compared five global thresholding algorithms, such as histogram shape information thresholding (Iterative Isodata method) [5], clustering of gray-level information thresholding (Otsu's image thresholding [6], Kittler and Illingworth's minimum cross entropy thresholding), entropy-based thresholding methods (Maximum entropy thresholding)[7] and Fuzzy C-Means clustering thresholding method[8]. A quantitative measure of comparison is provided by the PSNR (Peak Signal to Noise Ratio) of the image. The remainder of the paper is broken down into 4 sections. In Sections 2, we reviewed the five thresholding method. Some results of experiments have been shown in section 3. The conclusion and future works have been introduced in section 4.

## II. THE THEORY OF RELATED METHODS

In here, we may consider Chinese rubbing image segmentation as a specific binarization procedure which tries to keep only text and other objects which in this paper. Improper thresholding causes blotches, streaks, and erasures on the document, confounding segmentation and recognition tasks. Since digital image segmentation using thresholding technique is a well-researched field, there exist many algorithms for determining an optimal threshold of the image. The detail of those methods could be found in [10].

### A. Histogram shape information thresholding

The basic and easiest way to determine the global threshold of image in the case of binary image is based on finding two peaks of normal distribution from image

histogram separated by a valley corresponding to the intermediate gray levels, which is used to divide the object and background into bi-level. Pixels with a gray scale level under the threshold level are labeled as print; pixels with a gray scale level above the threshold level are labeled as background. The process can be described as follows:

$$I(x, y) = \begin{cases} 1 & \text{if } f(x, y) \leq T \\ 0 & \text{otherwise} \end{cases} \quad (1)$$

Concrete steps of this algorithm could be described as follow:

1) Select an initial estimate for  $T$ .

2) Segment the image using  $T$ . This will produce two groups of pixels.  $G1$  consisting of all pixels with gray level values  $>T$  and  $G2$  consisting of pixels with values  $\leq T$ .

3) Compute the average gray level values  $\mu_1$  and  $\mu_2$  for the pixels in regions  $G1$  and  $G2$ .

4) Compute a new threshold value,  $T = \frac{1}{2}(\mu_1 + \mu_2)$ .

5) Repeat steps 2 through 4 until difference in  $T$  in successive iterations is smaller than a predefined parameter  $T_0$ .

#### B. OTSU's thresholding method

Otsu has developed a thresholding method based on a discriminate criterion, which is the ratio of between-class variance and total variance of gray levels. Let the pixels of a given image. Let the pixels of a given image be represented in  $L$  gray levels  $[1, 2^L]$ . The number of pixels at level  $i$  is denoted by  $n_i$ , and the total number of pixels by

$$N = n_1 + n_2 + \dots + n_i. \quad (2)$$

So, a probability of gray level  $i$  in an image is

$$p_i = n_i / N. \quad \text{Then suppose that the pixels were}$$

dichotomized into two classes  $C_1$  and  $C_2$ , which denote pixels with levels  $[1, k]$  and  $[k+1, L]$ , respectively.

Then, the gray level probability distributions for the two classes are

$$\begin{aligned} C_1: & p_1 / \omega_1(t), \dots, p_k / \omega_1(t) \\ C_2: & p_{k+1} / \omega_2(t), \dots, p_L / \omega_2(t) \end{aligned} \quad (3)$$

$$\text{where } \omega_1(t) = \sum_{i=1}^k P_i \text{ and } \omega_2(t) = \sum_{i=k+1}^L P_i.$$

Also, the means for classes  $C_1$  and  $C_2$  are

$$\mu_1 = \sum_{i=1}^k ip_i / \omega_1(t) \text{ and } \mu_2 = \sum_{i=1}^k ip_i / \omega_2(t).$$

Let  $\mu_T$  be the mean intensity for the whole image. It is easy to show that

$$\begin{aligned} \omega_1 \mu_1 + \omega_2 \mu_2 &= \mu_T \\ \omega_1 + \omega_2 &= 1 \end{aligned} \quad (4)$$

Based on discriminate analysis, Ostu's method of threshold selection is ranked as the best and fastest global

thresholding method [16], [17]. This method uses a combination of a variety of segmentation methods, while ensuring the speed greatly improved the accuracy of image segmentation; the resulting document image binarization results are very satisfactory.

#### C. Minimum error thresholding

Minimum error thresholding method finds the optimum threshold by optimizing the average pixel classification error rate directly, using either exhaustive search or an iterative algorithm. This method assumes that an image is characterized by a mixture distribution with the population of object and background classes are normally distributed. The probability density function of the mixture distribution is estimated based on the histogram of the image.

In this method assumes that the image can be characterized by a mixture distribution of foreground and background

$$\text{pixels: } p(g) = P(T) \cdot p_f(g) + [1 - P(T)] \cdot p_b(g)$$

considers equal variance Gaussian density functions, and minimizes the total misclassification error via an iterative search. The total misclassification error expression can be interpreted also as a fitting error expression to be minimized such that:

$$\begin{aligned} T_{opt} &= \arg \min [P(T) \log \sigma_f(T) + \\ &(1 - P(T)) \log \sigma_b(T) - P(T) \log P(T) - \\ &-(1 - P(T)) \log (1 - P(T))] \end{aligned} \quad (5)$$

where  $\sigma_f(T)$  and  $\sigma_b(T)$  are, respectively, the foreground and background variances for each choice of  $T$ .

Besides assuming a normal distribution, the approach also assumes that the overlap between the two underlying distributions is small and the truncation error in the derivation of the algorithm can thus be ignored.

#### D. Fuzzy C means thresholding

Among all image segmentation methods, clustering methods get more attention in image segmentation field. Clustering is considered as the process of classifying patterns such that the patterns in the same cluster are more similar than ones in other clusters. In the clustering method, fuzzy C-means (FCM) algorithm is one of the most widely used methods due to its flexibility advantage in classifying pixels of segmented image [14]. The FCM algorithm assigns pixels to each category by using fuzzy memberships.

Let  $X = (x_1, x_2, \dots, x_N)$  denotes an image with  $N$  pixels to be partitioned into  $c$  clusters, where  $x_i$  represents features data [11]. However, the spatial Fuzzy c-means (FCM) is a method of clustering which allows one piece of data to belong to two or more clusters. This method (developed by Dunn in 1973 and improved by Bezdek in 1981) is frequently used in pattern recognition [8] [9]. The algorithm is an iterative optimization that minimizes the of the objective function  $J_q(U, V)$  as follows:

$$J_q(U, V) = \sum_{k=1}^n \sum_{i=1}^c (u_{ik})^q d^2(x_k, v_i) \quad (6)$$

where  $X = \{x_1, x_2, \dots, x_n\} \subseteq R^p$ ,  $n$  is the number of data items,  $c$  is the number of clusters with  $2 \leq c < n$ ,  $u_{ik}$  is the degree of membership of  $x_k$  in the  $i^{\text{th}}$  cluster,  $q$  is a weighting exponent on each fuzzy membership,  $v_i$  is the prototype of the centre of cluster  $i$ ,  $d^2(x_k, v_i)$  is a distance measure between  $x_k$  object and cluster centre  $v_i$ . A solution of the object function can be obtained via an iterative process, which is carried as follows:

- 1) Set value for  $c$ ,  $q$  and  $\varepsilon$ .
- 2) Initialize the fuzzy partition matrix  $U$ .
- 3) Set the loop counter  $b = 0$ .
- 4) Calculate the  $c$  cluster centers  $\{v_i^{(b)}\}$  with  $U^{(b)}$ :

$$v_i^{(b)} = \frac{\sum_{k=1}^n (u_{ik}^{(b)})^q x_k}{\sum_{k=1}^n (u_{ik}^{(b)})^q}$$

5) Calculate the membership  $U^{(b+1)}$ . For  $k = 1$  to  $n$ , calculate the following:

$$I_k = \{i | 1 \leq i \leq c, d_{ik} = \|x_k - v_i\| = 0\}$$

$$\tilde{I}_k = \{1, 2, \dots, c\} - I_k$$

for the  $k^{\text{th}}$  column of the matrix, compute new membership values:

$$\text{a) if } I_k = \phi, \text{ then } u_{ik}^{(b-1)} = \frac{1}{\sum_{j=1}^c \left(\frac{d_{jk}}{d_{ik}}\right)^{2/(q-1)}},$$

$$\text{else } u_{ik}^{(b-1)} = 0 \text{ for all } i \in \tilde{I}_k \text{ and } \sum_{i \in I_k} u_{ik}^{(b-1)} = 1;$$

next  $k$ .

6) If  $\|U^{(b)} - U^{(b-1)}\| < \varepsilon$ , stop; otherwise, set

$b = b + 1$  and go to step 4.

#### E. Max entropy method

In this method the foreground and background classes are considered as two different sources. When the sum of the two class entropies is a maximum the image is said to be optimally thresholded. Thus using the definitions of the foreground and background entropies,

$$H_f(T) = - \sum_{g=0}^T \frac{p(g)}{P(T)} \log \frac{p(g)}{P(T)} \quad \text{and}$$

$$H_b(T) = - \sum_{g=T+1}^G \frac{p(g)}{P(T)} \log \frac{p(g)}{P(T)} \quad \text{one has:}$$

$$T_{opt} = \arg \max [H_f(T) + H_b(T)] \quad (7)$$

### III. EXPERIMENTAL RESULTS PERFORMANCE EVALUATION

To investigate the performance of the different threshold method, the images which come from library of Harvard are chosen as input images with resolution of  $2112 \times 1781$  (another rubbing image size is  $1688 \times 2400$ ) pixels and 256 intensity levels, respectively. For the

purpose of comparison, we adopt the same approach that was taken by Kittler and Illingworth, Ostu's method, the minimum error method, and fuzzy C-means thresholding method are implemented on the Chinese rubbing image as stored in Harvard library, could be found in reference [12].

The rubbing image histograms are shown in Fig .2 and 4. The exact thresholds that have been obtained by the five algorithms are summarized in Table 1, respectively. The results of Peak Signal to Noise Ratio (PSNR) and Mean Square Error (MSE) for different algorithm have been shown in Table 1 also.

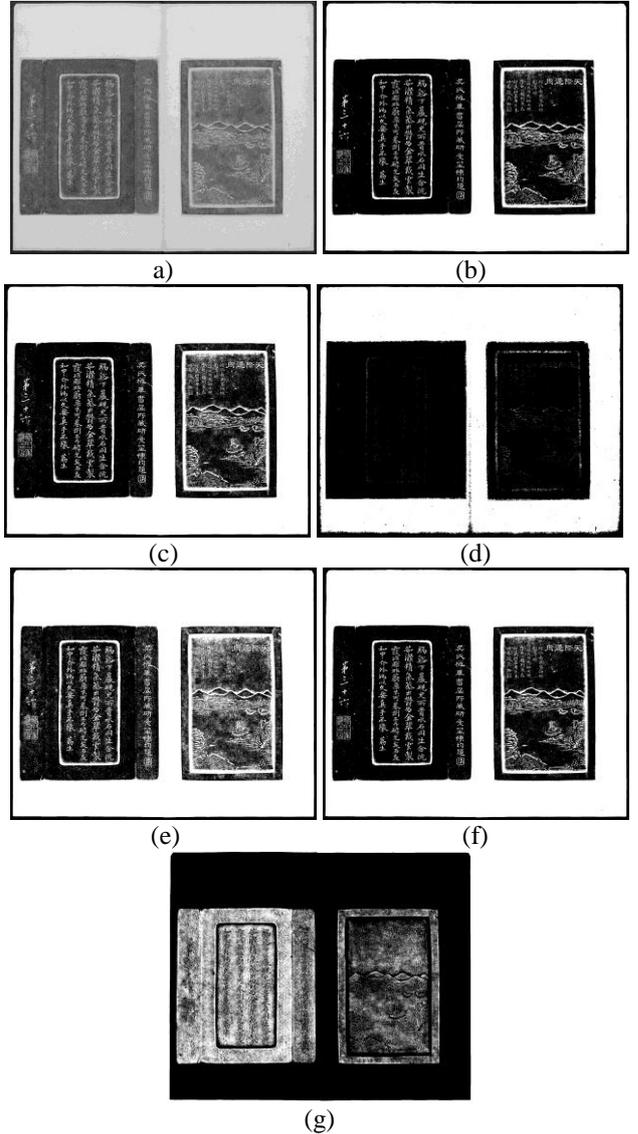


Figure 1. Thresholding results of rubbing image which number is 10402096 [12]. From left to right and from top to bottom: Original images, segmentation image using isodata thresholding, segmentation image using Minimum cross entropy thresholding image, segmentation image using Kittler's method thresholding, segmentation image using Max entropy method thresholding, segmentation image using Ostu's method thresholding, segmentation image using FCM's method thresholding.

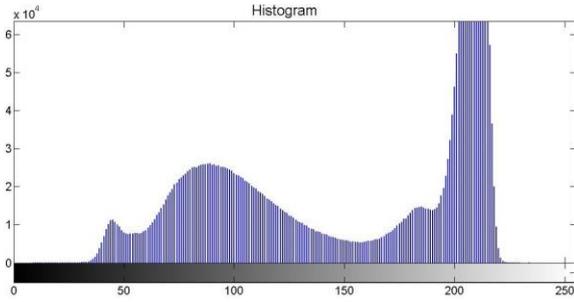
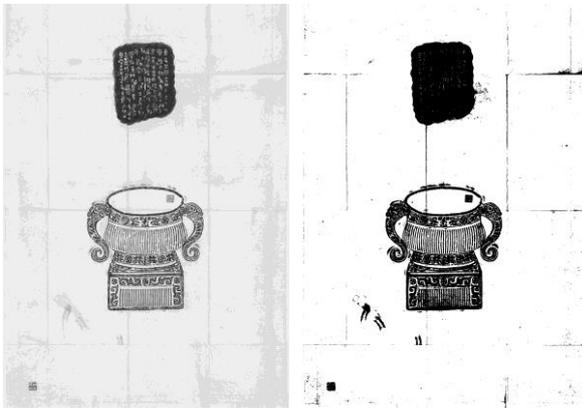
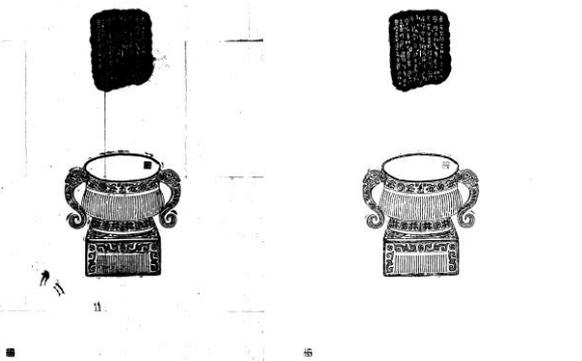


Figure 2. Histogram of rubbing image that No. 12443747



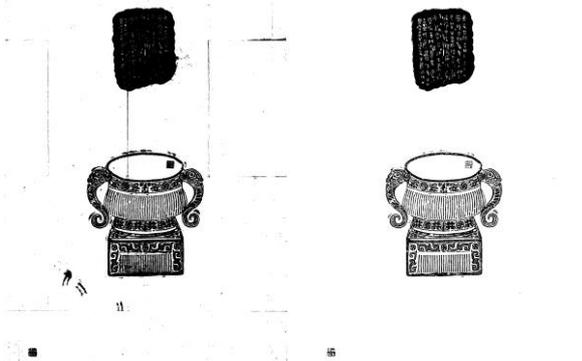
(a)

(b)



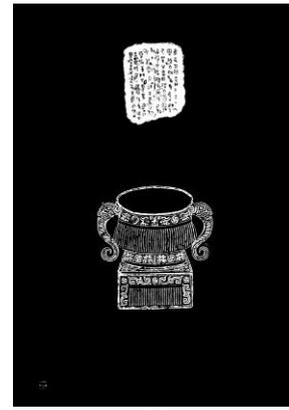
(c)

(d)



(e)

(f)



(g)

Figure 3. Thresholding results of rubbing image which number is 14940418 [13]. From left to right and from top to bottom: Original images, segmentation image using isodata thresholding, segmentation image using Minimum cross entropy thresholding image, segmentation image using Kittler's method thresholding, segmentation image using Max entropy method thresholding, segmentation image using Ostu's method thresholding, segmentation image using FCM's method thresholding.

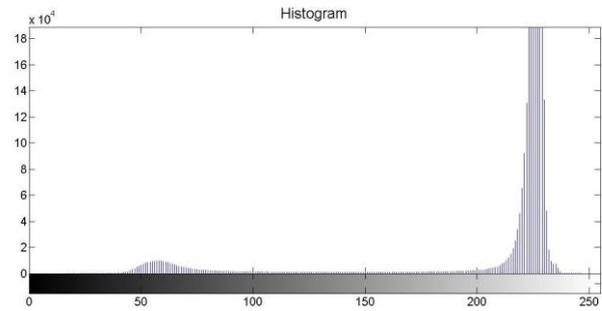


Figure 4. Histogram of rubbing image that No. 14940418

TABLE I. THRESHOLDING EVALUATION OF RUBBING IMAGES.

	Method	MSE	PSNR	Thresholding Level
Name. 12443747 Size of Image : 2112*1781	Histogram	116.46	27.46	147.8
	Isodata			
	Minimum cross entropy	109.54	27.73	137.0
	Kittler's method	138.76	26.71	189.0
	Max entropy	97.67	28.23	121.0
	Ostu's method	114.03	27.56	146.0
	Fuzzy C Means	189.06	25.36	97.5
Name. 14940418 Size of Image : 1688*2400	Histogram	27.41	33.75	168.18
	Isodata			
	Minimum cross entropy	18.08	35.56	133.0
	Kittler's method	28.17	33.63	215.0
	Max entropy	25.12	34.13	208.0
	Ostu's method	19.09	35.32	149.0
	Fuzzy C Means	238.9	24.35	104.5

The three methods that are Histogram Isodata, Minimum cross entropy and Ostu's method have obtained similar thresholding level in No.12443747. The Max entropy method does give minimum MSE. The FCM

method gives smaller thresholding level, and show more detail structures in segmentation rubbing image.

#### IV. CONCLUSIONS

Automatic extraction of characters from Chinese rubbing images is a difficult task due to their degradation because of different types of noise. Applying a global threshold or a chosen threshold based on visual intuition might miss the finer Chinese characters with low intensity values. In this study, we make a compared evaluation of image thresholding methods for Chinese rubbing image. Several other issues remain to be addressed. For example, the increasing number of color documents becomes a new challenge for binarization and segmentation. Other topic such as that after applying global threshold, left out background image consists of some mixed image background and characters intensities on which we apply mathematical morphology (opening and closing), which produces a smooth contour and gives an adaptive threshold.

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