

# Transient Characteristics Analysis of DFIG during Power Grid Fault and Crowbar Resistance Adaptive Tuning

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**Abstract**—The purpose of this paper is to improve low voltage ride through (LVRT) capability of doubly fed induction generator (DFIG). First, this paper gives expressions of the stator flux and rotor current during the grid fault occurrence and clearing by solving the mathematical model of DFIG. The results of simulation conducted on a 1.5MW DFIG in the PSCAD/EMTDC verified the correctness of the derivation. Through qualitative analysis of stator flux expression, different fault durations will lead to the difference of transient during fault clearing and ignoring the process of fault clearing will lead to excessive crowbar resistance. Therefore, this paper optimizes the Crowbar resistance by considering both the process of grid fault and fault clearing, and then presents a Crowbar resistance adaptive setting principle based on Crowbar structure with parallel resistor. Simulation confirms this method can improve LVRT of wind farms.

**Keywords**—doubly fed induction generator (DFIG); transient characteristics; low voltage ride through (LVRT); Crowbar circuit; adaptive tuning

## I. INTRODUCTION

DFIG has two converters with small capacity and its active and reactive power can be adjusted independently, so it is widely used in the world [1-2]. But the DFIG stator is directly connected to the grid, so it's vulnerable to the impact of system faults. The transient characteristics of DFIG are complex, and control ability of the small capacity converters is limited, making it more difficult to realize LVRT [3-4]. When a serious fault occurs, it's needed to add hardware device for low voltage ride through, among which Crowbar protection is most widely used. Accurate analysis and calculation of DFIG transient process is the premise and key to the design of Crowbar protection scheme.

A lot of papers analyze and calculates the transient process of DFIG. When grid voltage sags, the impact of transient flux on rotor open circuit voltage was analyzed in [5]; [6] derived DFIG rotor current expression under grid faults, but only under the converter controlled conditions; [7] analyzed the impact of crowbar protection action time on DFIG short circuit current, and acquired the short circuit current expressions; [8] made use of mathematical analytical method to analyze the electromagnetic transient process of DFIG, and gave the expressions of rotor flux and current; [9] precisely deduced the expressions of stator, rotor flux and voltage, on the basis of which putting forward a new design method to optimize the

parameters of new Crowbar circuit structure. [10-13] calculated the maximum estimated value of DFIG short-circuit current, and then gave the constraints optimization of Crowbar resistance.

The references above mostly studied the DFIG transient process during the period of the fault, with the result that LVRT strategy (such as the Crowbar resistance selection) was not reasonable. Aiming at solving the problem, this paper studies the whole transient process of fault occurrence and clearing of DFIG, derives the expressions of the stator and rotor current, simulation verifies the correctness of deduction. At last, a Crowbar resistance adaptive tuning principle is proposed to improve the LVRT ability of DFIG.

## II. ANALYSIS OF DFIG TRANSIENT CHARACTERISTICS

### A. Analysis and Calculation of the Stator Flux Linkage

According to the motor convention, in the two-phase stationary coordinate system, the DFIG voltage and flux linkage equations are [5]:

$$\mathbf{u}_s = R_s + p\boldsymbol{\Psi}_s \quad (1)$$

$$\mathbf{u}_r = R_r \mathbf{i}_r + p\boldsymbol{\Psi}_r - j\omega\boldsymbol{\Psi}_r \quad (2)$$

$$\boldsymbol{\Psi}_s = L_s \mathbf{i}_s + L_m \mathbf{i}_r \quad (3)$$

$$\boldsymbol{\Psi}_r = L_r \mathbf{i}_r + L_m \mathbf{i}_s \quad (4)$$

Where  $\mathbf{u}$ ,  $\mathbf{i}$  and  $\boldsymbol{\Psi}$  are voltage, current and flux vector,  $R$  and  $L$  are resistances and inductance, subscripts  $s$ ,  $r$  represent the stator and the rotor respectively,  $p$  is differential operator.

The grid three-phase symmetrical short circuit in  $0s$ , voltage sag depth is  $k$ ,  $t_1$  is grid voltage recovering time. Stator voltage can be expressed as:

$$\mathbf{u}_s = \begin{cases} U_{sm} e^{j\omega t} & t < 0, t > t_1 \\ kU_{sm} e^{j\omega t} & 0 \leq t \leq t_1 \end{cases} \quad (5)$$

The voltage amplitude is synchronous electric angular velocity. Ignoring the stator resistance, equation 5 into equation 1, stator flux can be solved as:

$$\Psi_s = \begin{cases} \frac{kU_{sm}}{j\omega_s} e^{j\omega_s t} + \frac{(1-k)U_{sm}}{j\omega_s} e^{-T_s t} & 0 \leq t \leq t_1 \\ \frac{U_{sm}}{i\omega_e} e^{j\omega_s t} - \frac{(1-k)U_{sm}}{i\omega_e} (e^{j\omega_s t_1} - e^{-T_s t_1}) e^{-T_s(t-t_1)} & t > t_1 \end{cases} \quad (6)$$

Expression (6) shows that both the fault occurrence and clearance will cause transient changes of stator flux linkage. The stator flux linkage contains synchronous rotating AC component and the DC component which attenuates by time constant  $T_s$ . The amplitude of stator flux linkage oscillation is related to the voltage sag degree  $k$ ; stator flux linkage goes in the same rules of vibration attenuation in the fault clearance stage, but the amplitude of the oscillation is not only associated with  $k$ , but the fault clearing time  $t_1$ , so extracts feature component in (6):

$$\psi_{sn} = \left[ \frac{(1-k)U_{sm}}{j\omega_s} (e^{j\omega_s t_1} - e^{-T_s t_1}) \right] e^{-T_s(t-t_1)} \quad (7)$$

When  $t=t_1$ , obtain the maximum value:

$$e_r = \begin{cases} \frac{L_m}{L_s} skU_{sm} e^{j\omega_s t} - \frac{L_m}{L_s} (1-s)(1-k)U_{sm} e^{-T_s t} & 0 \leq t \leq t_1 \\ \frac{L_m}{L_s} sU_{sm} e^{j\omega_s t} + \frac{L_m}{L_s} (1-s)(1-k)U_{sm} (e^{j\omega_s t_1} - e^{-T_s t_1}) e^{-T_s(t-t_1)} & t \geq t_1 \end{cases} \quad (11)$$

Where:  $s$  is slip. When Crowbar is connected,  $\mathbf{u}_r = -\mathbf{R}_c \mathbf{i}_r$ , where is Crowbar.

Expression (11) can be transformed into:

$$\sigma L_r p i_r + (R_r + R_c - j\omega_r \sigma L_r) i_r = -e_r \quad (12)$$

$$A = \begin{cases} \frac{L_m}{L_s} skU_{sm} & 0 \leq t \leq t_1 \\ \frac{L_m}{L_s} sU_{sm} & t \geq t_1 \end{cases}, \quad B = \begin{cases} -\frac{L_m}{L_s} (1-s)(1-k)U_{sm} & 0 \leq t \leq t_1 \\ \frac{L_m}{L_s} (1-s)(1-k)U_{sm} (e^{j\omega_s t_1} - e^{-T_s t_1}) & t \geq t_1 \end{cases}$$

From expression (13), rotor current consists of three components: AC steady-state component, DC attenuation component and rotor speed frequency attenuation component, which attenuates by rotor time constant, which is related to DFIG parameters, rotor speed and Crowbar resistance.  $C_1$  can be obtained from rotor current initial values at each stage. In the steady state, DFIG adopts the stator flux oriented vector control, so rotor current in the steady state are [2]:

$$\begin{cases} i_{rq} = -\frac{2P_s}{3U_{s0}} \\ i_{rd} = \frac{U_{s0}}{\omega_s L_s} - \frac{2Q_s}{3U_{s0}} \end{cases} \quad (14)$$

Where:  $P_s$  and  $Q_s$  are DFIG active power, reactive power, the subscript d, q represent d, q components in d and q coordinates system. In the steady state, the DFIG active power, reactive power can be calculated according to the given value of rotor current. Switching expression (15) to the two-phase stationary coordinate system:

$$i_r = (i_{rd} + j i_{rq}) e^{j\omega_s t} \quad (15)$$

$$\psi_{sn} = \frac{(1-k)U_{sm}}{j\omega_s} (\cos\omega_s t_1 - e^{-T_s t_1} + j \sin\omega_s t_1) \quad (8)$$

As shown in (8): when  $t_1$  is equal to odd multiples of half power cycle, the flux oscillation amplitude is large; when  $t_1$  is equal to multiples of one power cycle, the flux oscillation amplitude is small.

### B. Analysis and Calculation of Rotor Current

The rotor voltage can be solved from (2),(3) and (4):

$$u_r = \frac{L_m}{L_s} (p\psi_s - j\omega_r \psi_s) + R_r i_r + \sigma L_r (p i_r - j\omega_r i_r) \quad (9)$$

Where:  $\sigma = 1 - L_m^2 / (L_s L_r)$ , and extracts feature component in (9):  $e_r = \frac{L_m}{L_s} (p\psi_s - j\omega_r \psi_s)$ .

$$u_r = e_r + R_r i_r + \sigma L_r (p i_r - j\omega_r i_r) \quad (10)$$

Expression (6) into expression (10):

Simplification of expression 12 is:

$$i_r = -\frac{A}{j\omega_s \sigma L_r + F} e^{j\omega_s t} + \frac{B}{\sigma L_r T_s - F} e^{-T_s t} + C_1 e^{-\frac{F}{\sigma L_r} t} \quad (13)$$

Where:  $F = R_r + R_c - j\omega_r \sigma L_r$ ,

When  $t=0$ ,  $i_r(0) = i_{rd} + j i_{rq}$ , so  $C_1 = i_r(0) + \frac{A}{j\omega_s \sigma L_r + F} - \frac{B}{\sigma L_r T_s - F}$ , then the rotor current expression can be obtained. Rotor current values can be obtained as DFIG parameters and fault data substitute into expression (14).

## III. SIMULATION AND VERIFICATION

To verify the above theory is correct, in PSCAD/EMTDC, on the grid under grid connected three-phase symmetrical fault 1.5MW DFIG the simulation, parameters of unit reference [16]. Before fault the speed of generator rotor is 1.2pu, generator full load operation, we suppose wind speed constant during the period of fault.

In the simulation, power system fault at 0.2s, the terminal voltage symmetry fell to 0.2pu,  $R_c = 0.2\Omega$ , Crowbar protection act when failure occurs, fault durations 0.09s. The rotor current waveforms are compared in Figure 1 and Figure 2. The dotted line is the simulation results and the solid line is the calculated results.

From Figure 1 and Figure 2, the rotor current rotor current maximum value after fault clearance is far greater than the time of fault happening when fault duration is very short

(0.09s). Stator flux is not decayed to stable before the fault is cleared while fault is short, if the fault duration is odd times frequency half cycle, amplitude of stator flux oscillation will be greater than the time of fault at fault clearing time, the rotor current will be far greater than the moment of rotor current fault occurs.

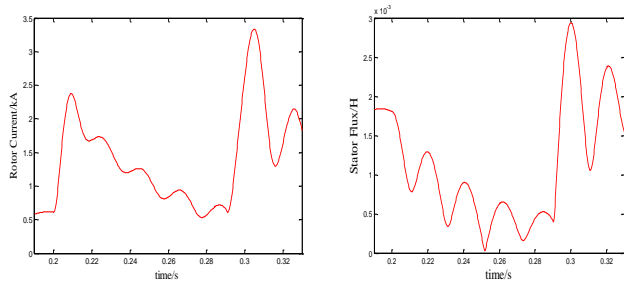


FIGURE I – II. COMPARISON WAVEFORMS OF ROTOR CURRENT AMPLITUDE WHEN FAULT DURATION ARE 0.09S.

#### IV. OPTIMIZATION OF CROWBAR RESISTANCE

The main purpose of Crowbar protection is protecting the generator and converter not affected by the rotor over voltage and over current during fault time, to achieve two effects, the Crowbar resistance selection constraint conditions is:

$$R_c \leq U_{dc\_lim} / I_{r\_max} \quad (17)$$

The analysis in this paper shows that at a certain time, the rotor current at the fault clearing stage is much larger than that at the fault occurrence stage. Therefore, this paper adopts a new Crowbar structure with parallel resistor (as shown in Figure 3), and then proposes corresponding Crowbar resistance adaptive tuning principle as follows.

$$\begin{cases} R_c \leq U_{dc\_lim} / I_{r\_max1} \\ R'_c \leq U_{dc\_lim} / I_{r\_max2} \end{cases} \quad (18)$$

Where:  $R_c, R'_c$  are the crowbar resistors settings at both fault occurrence and clearing stage,  $I_{r\_max1}, I_{r\_max2}$  are the maximum values of rotor current at both fault occurrence and clearing stage, which can be calculated by the 1.2 quarter of theoretical, the Crowbar resistance values obtained are simulated respectively. It can be seen from Figure 4 that according to traditional methods DC bus voltage exceeds the allowable range at the fault clearing stage, indicating that Crowbar resistance setting is improper; in contrast the use of adaptive tuning principle can keep DC bus voltage in the allowable range. Therefore scheme proposed in this paper is more reasonable.

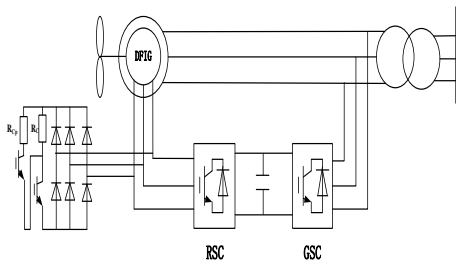


FIGURE III. CROWBAR WITH PARALLEL RESISTOR.

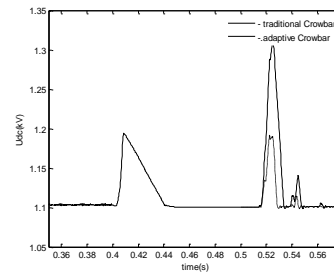


FIGURE IV. COMPARISONS OF DC VOLTAGE.

#### V. CONCLUSION

On the basis of DFIG mathematical model, the transient characteristics of DFIG are analyzed and derived during the whole fault period, the simulation analysis verifies the correctness of the theoretical analysis, accordingly a novel selection and control scheme of Crowbar resistance is proposed. Therefore, some useful conclusions are obtained as follows:

- 1) Rotor current derived in this paper has higher calculation accuracy.
- 2) When fault duration is odd times to half power cycle after fault, the stator flux oscillations, the rotor over voltage and over current is more serious; when fault duration is integer times to power cycle, DFIG quickly restore stability after fault is cleared, causing smaller transient impact, so the rotor converter can regain control unit quickly.
- 3) This paper comprehensively considers the whole stage of both in fault occurrence and clearing process, and Crowbar resistance adaptive tuning principle is proposed accordingly, which can effectively improve the ability of LVRT.

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