

Study on Evaluation Indicators System of Crowd Management for Transfer Stations Based on Pedestrian Simulation

Guanghou Zhang*

Transportation Research Center, Beijing University of Technology, Beijing 100124, China

Yanyan Chen

Transportation Research Center, Beijing University of Technology, Beijing 100124, China

E-mail: cdyan@bjut.edu.cn

www.bjut.edu.cn

Pingpu Li

Transportation Research Center, Beijing University of Technology, Beijing 100124, China

E-mail: liping@emails.bjut.edu.cn

www.bjut.edu.cn

Simon Fibbe

Westplantsoen 6B, 2613 GL Delft, the Netherlands

E-mail: S.T.Fibbe@student.tudelft.nl

www.transport.citg.tudelft.nl

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Abstract

Improving safety and convenience of transfer is one of the most vital tasks in subway system planning, design and operation management. Because of complicated space layout and crowded pedestrian, crowd control is a big challenge for management of transfer stations. Thus, a quantitative evaluation should be done before improvement measures are carried out. Literature review showed that present evaluation indicators about crowd management in subway system were all based on fixed value or experience. Dynamic effect caused by pedestrian congestion and various facility combination cannot be represented based on these indicators. Thus, in this paper, based on the pedestrian simulation tool, dynamic evaluation indicators system of crowd management was established from the point of safety, cost-effectiveness and comfort. In order to aid decision makers to identify the most appropriate scenario to improve the effectiveness of crowd management, Matter-Element Analysis (MEA) was used to rate different scenarios. A pedestrian simulation model of a designing intermodal transfer station was built and four different scenarios were tested to demonstrate how to use this indicators system. Simulation results were evaluated based on the dynamic indicators system and MEA. The application results show that the dynamic evaluation indicators system is operational and can reflect level of the crowd management in transfer station comprehensively and precisely.

Keywords: crowd management, dynamic evaluation indicators, pedestrian simulation, Matter-Element Analysis

1. Background

With the continuous improvement of the subway network system in Beijing, passenger volume increased

dramatically. And with the subway system covering more and more areas, most of the passengers need to transfer between different lines. Based on the statistic data, the transfer ratio is 1.2-1.5. Many passengers need

*Transportation Research Center, Beijing University of Technology, 100 Pingleyuan, Chaoyang District, Beijing, 100124, China
Emails: guanghouzhang@emails.bjut.edu.cn

to transfer between lines. As convergences node of multi-lines, transfer stations need to assume more passengers than other stations. During peak time, there will be a mass arrival in a very short time and the transfer facilities face great press. Consequently, transfer in subway station is an uncomfortable and time-consuming issue for passenger. And, for the management, it is a great challenge to keep the transfer stations safe. But, crowd management in transfer station is a systematic work, included facility plan, facility design, and pedestrian traffic flow organization. Usually, it is a combination of kinds of measures. So, a quantitative evaluation should be done before the countermeasure scenarios of crowd management are carried out.

In china, many researchers have pay attention to the operation evaluation of subway or multimodal transfer stations. From the view of planning coordination, passenger satisfaction and operation management effectiveness, Liu xiaoming [1] proposed operation evaluation indicators system for urban public transfer terminals. Though this system included several qualitative indicators, it was one of earliest research results in such field in china. Following the basic frame proposed by Liu xiaoming, many researchers [2-7] improved and expanded the evaluation indicators system for transfer stations or hubs gradually.

But, the previous research results of evaluation system for transfer stations still have two mainly imperfect points. Firstly, there are still some qualitative indicators in exiting evaluation system. Setting value of these indicators need to be finished by experts. Thus, qualitative indicators are limited to the experience of the experts or decision makers and the values might be not objective and convictive. Especially for the planning or unfinished transfer stations, future operation status can only be imaged by experts. It is quite difficult to figure out results of different scenarios because of complicated facility layout and passenger behaviors. Secondly, calculations of the exiting quantitative indicators are all based on static threshold values in related design standard, such as, the speed of passenger and the capacity of facilities. Actually, different characteristics and behaviors of passengers will affect the capacity of all kinds of facilities. And, the demand of passengers is also assumed static and smooth. Generally, in procedure of facility design, the minimum interval used to count passenger volume is fifteen minutes. Actually, the

headway for trains in subway system is much shorter than fifteen minutes. Thus, the wave of passenger flow, congestion and combination of kinds of facilities can dramatically affect the traffic behavior of passenger. Consequently, static evaluation can not reflect the real status of transfer stations.

Pedestrian simulation tools have been applied widely in crowd management. Especially in subway system, simulation tool can be used to evaluate the pros and cons of different scenarios such as facility design, passenger traffic organization and operation management [8-10]. With reasonable calibration of parameters and validation of output, pedestrian simulation tools can not only intuitively show the operational status of pedestrian traffic, but also record the accurate data about speed, acceleration, deceleration and track of all pedestrian. So, dynamic and quantitative evaluation can be done with pedestrian simulation tools. But, recently, qualitative description or basic comparison of simulation results is still the main application method of pedestrian simulation tools. The simulation evaluation method is not versatile because of lacking of standard dynamic evaluation indicators system and procedure.

Therefore, the goal of this paper was to propose a dynamic evaluation indicators system of crowd management in transfer stations based on Legion pedestrian simulation tool. The dynamic evaluation system selected indicators from the view of security, cost-effectiveness and comfort to evaluate different scenarios about crowd management in transfer stations.

2. Evaluation Procedure Based on Pedestrian Simulation

2.1. Introduction of Legion Pedestrian Simulation Tool

The multi-agent pedestrian model at the heart of the Legion simulation tool has been developed at the Maia Institute since 2000. Each pedestrian is modeled as a two-dimensional “entity” with a circular body, which moves in 2D continuous space, in 0.6s time steps. The model can handle multiple floors, with special objects to enable the modeling of circulation elements such as stairs, escalators, ramps, moving walkways and lifts (elevators) [11].

Each entity moves towards its current target by selecting a step which seeks to minimize a perceived objective

cost function. This cost is a weighted sum of the following three components:

- Inconvenience: Work to move, in excess of the amount which is necessary to reach one's destination;
- Frustration: Energetic cost equivalent of violating the speed preference time expenditure;
- Discomfort: Energetic cost equivalent of violating the preference clearance from other pedestrian and obstacles (Sum of functions of distances to predicted positions of perceived closest other pedestrian and other functions of distances to local obstacles).

Legion can record detailed track of each individual pedestrian and can accurately calculate the individual traffic behavior parameters and macroscopic traffic flow characteristics of pedestrian. The status of pedestrian traffic system can be reflected by maps, charts, tables. Detailed output parameters can be found in Table 1.

Legion can be used to a lot of fields relevant with pedestrian. Such as pre-feasibility assessment, new station designs and station refurbishment projects. So, in this paper, evaluation indicators system was established based on the Legion studio 2006.

Table.1 Output parameters of Legion

Output format	Output parameters
Map Chart Table	Ingress and Egress
	Occupancy
	Flow
	Speed
	Entity and Space density
	Journey time
	Social cost
	Inconvenience, Frustration,
	Discomfort and Dissatisfaction

2.2. Evaluation procedure

Traffic simulations model the complex traffic phenomenon and reproduce the actual traffic conditions based on predicting. Analysis works such as evaluation and optimization can be done based on simulation results. Fig. 1 shows the framework of evaluation procedure for crowd management in transfer stations based on pedestrian simulation. Analysis of simulation model can intuitively reflect the possible problems of the pedestrian facilities or pedestrian traffic organization in subway station. Then quantitative evaluation can be done with dynamic evaluation indicators system. At last, certain algorithms could be used to figure out the best scenario.

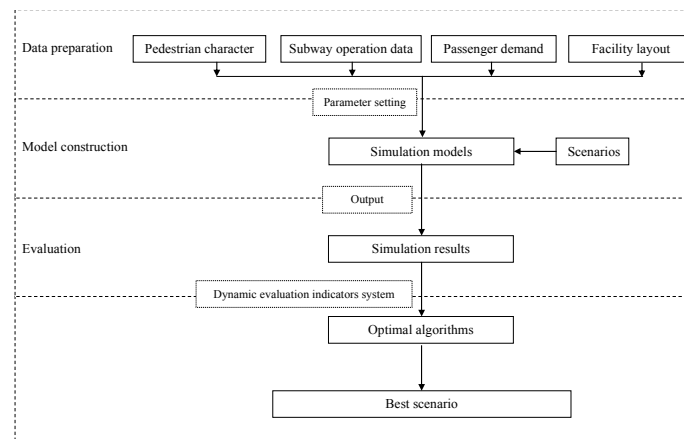


Fig. 1. Framework of evaluation procedure for crowd management in transfer stations based on pedestrian simulation

3. Dynamic Evaluation Indicators System

Making transfer more safe and efficient is the basic objective of crowd management in transfer stations. So, the main aim of dynamic evaluation of crowd management in transfer station is to evaluate the pros and cons of different scenarios in view of operation

safety, transfer time and comfort. Therefore, this paper built dynamic evaluation indicators system based on the output results of Legion simulation software from the view of security, cost-effectiveness and comfort. The frame of this dynamic evaluation indicators system can be found in Fig.2.

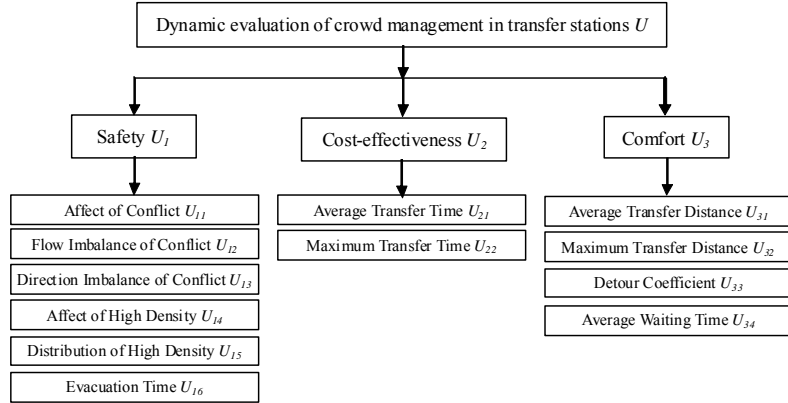


Fig. 2. Dynamic evaluation indicators system of crowd management for transfer stations

3.1. Indicators of Safety

3.1.1. Affect of conflict u_{11}

In transfer stations, crossing area with passengers from two or more directions is defined as conflict point. Affect of conflict points is represented by proportion of passengers who cross the conflict points. It is assumed as in Eq. (1):

$$u_{11} = \sum_{i=1}^n q_i / q_t \quad (1)$$

Where q_i is passenger flow of conflict point i , q_t is the total flow in the transfer station during simulation time, n is the number of conflict points.

3.1.2. Flow imbalance of conflict u_{12}

This indicator reflects the flow distribution among different conflict points. Equilibrium distribution of passenger flow is helpful for safety of transfer stations. The more evenly the flow is distributed among different conflict points, the safer the transfer stations will be. Gini-Concentration index was used to calculate flow imbalance of conflict. Based on the definition, 0 means the distribution is most even; 1 means the distribution is dramatic concentration [12], as shown in Eq. (2):

$$u_{12} = \sum_{i=1}^{n-1} |f_i - p_i| / \sum_{i=1}^{n-1} f_i \quad (2)$$

Where n is the number of conflict points, f_i is accumulative distribution assumed that each conflict point has the same number of passengers, $f_i = i/n$; p_i is the actually accumulative distribution,

$p_i = \sum_{j=1}^i q_j / \sum_{j=1}^n q_j$, q_i is the real passenger flow of conflict point j .

3.1.3. Direction Imbalance of Conflict u_{13}

For a conflict point, evenly flow distributions of different directions means higher lose of capacity. This indicator reflects the flow distribution among different directions in one conflict point, as shown in Eq. (3):

$$u_{13} = \sum_{i=1}^n w_i \cdot d_i \quad (3)$$

Where n is the number of conflict points, w_i is weight of conflict point i , d_i is the direction imbalance of conflict point i . d_i can be also calculated based on Gini-Concentration index, as follows:

$$d_i = \sum_{j=1}^{dn_i-1} |f_{ij} - p_{ij}| / \sum_{j=1}^{dn_i-1} f_{ij} \quad (4)$$

Where dn_i is number of directions of passenger flow in conflict point i , f_{ij} is accumulative distribution assumed that the distribution among all directions is even in conflict point i , $f_{ij} = j/dn_i$; p_{ij} is actually accumulative distribution among all directions in conflict point i , $p_{ij} = \sum_{m=1}^j qd_{im} / q_i$, qd_{im} is passenger flow of direction m in conflict i , q_i is the real passenger flow of conflict point.

Considering number of directions and flow of different conflict points, w_i can be calculated based on entropy weight coefficient method. Based on information theory [13], the entropy of conflict i is:

$$H_i = -\frac{1}{\ln dn_i} \sum_{j=1}^{dn_i} h_{ij} \ln h_{ij} \quad (5)$$

Where, $h_{ij} = qd_{ij} / \sum_{k=1}^{dn_i} qd_{ik}$, the weight of conflict i is:

$$w_i = 1 - H_i / n - \sum_{i=1}^n H_i \quad (6)$$

3.1.4. Affect of high density u_{14}

Concentration of high-density crowd is a serious risk of safe for transfer stations. This indicator reflects the affect of high density. It is assumed that the value of high density is under D Level of service [14]. Considering duration and flow of affected passenger, the affect of high density is:

$$u_{14} = \sum_{i=1}^e \sum_{j=1}^{m_i} l_{ij} \cdot v_{ij} / T_i \cdot q_i \quad (7)$$

Where e is the number of high density areas, m_i is the number of high density duration in high density area i , l_{ij} is length of high density duration j in high density area i , v_{ij} is passenger flow of high density duration j in density area i , T_i is total length of simulation time, q_i is the total flow of the transfers station during simulation time.

3.1.5. Distribution of high density u_{15}

This indicator reflects distribution of passenger who suffered high density [14]. And the value of this indicator can be calculated by Legion directly.

3.1.6. Evacuation time u_{16}

Evacuation time is direct evaluation of evacuation ability in emergency. Because Legion can record the track of each pedestrian, the value of this indicator can be calculated by Legion software directly too.

3.2. Indicators of Cost-effectiveness

3.2.1. Average transfer time u_{21}

From the view of passenger, transfer time can intuitively reflect cost-effectiveness of transfer, as shown in Eq. (8):

$$u_{21} = \sum_{i=1}^{q_i} t_i / q_i \quad (8)$$

Where t_i is transfer time of passenger i , q_i is the total flow in the transfer station during simulation time.

3.2.2. Maximum average transfer time u_{22}

Transfer stations service kinds of transportation mode. It is necessary to make sure that transfer time of any OD pair cannot exceed a threshold value. This indicator reflects the maximum average transfer time of different transportation mode or OD pair, as shown in Eq. (9):

$$u_{22} = \max_{1 \leq i \leq r} \max_{1 \leq j \leq s} \left\{ \sum_{k=1}^{o_{ij}} t_{ijk} / o_{ij} \right\} \quad (9)$$

Where r is number of origin in simulation model, s is number of destination in simulation model, o_{ij} is passenger flow from origin i to destination j , t_{ijk} walking time of passenger k from origin i to destination j .

3.3. Indicators of Comfort

3.3.1. Average transfer distance u_{31}

Shorter transfer distance means passengers can easily arrive at their destinations. In other words, passenger will feel comfort if they could easily transfer. This indicator reflects the average transfer distance of all passengers, as shown in Eq. (10):

$$u_{31} = \sum_{i=1}^{q_i} l_i / q_i \quad (10)$$

Where l_i is transfer distance of passenger i , q_i is the total flow of the transfers station during simulation time.

3.3.2. Maximum average transfer distance u_{32}

As mentioned above, transfer stations cover kinds of transportation mode. It is also necessary to make sure that transfer distance of any OD pair cannot exceed a threshold value. This indicator reflects the maximum average transfer distance of different transportation mode or OD pair, as shown in Eq. (11):

$$u_{32} = \max_{1 \leq i \leq r} \max_{1 \leq j \leq s} \left\{ \sum_{k=1}^{o_{ij}} l_{ijk} / o_{ij} \right\} \quad (11)$$

Where r is number of origins in simulation model, s is number of destinations in simulation model, o_{ij} is passenger flow from origin i and destination j , l_{ijk} is the transfer distance of passenger k from origin i to destination j .

3.3.3. Detour coefficient u_{33}

This indicator reflects the transfer convenience of all passengers, as shown in Eq. (12):

$$u_{33} = \sum_{i=1}^r \sum_{j=1}^s w_{ij} \sum_{k=1}^{o_{ij}} l_{ijk} / o_{ij} \cdot s_{ij} \quad (12)$$

Where r is number of origin in simulation model, s is number of destination in simulation model, o_{ij} is passenger flow from origin i and destination j , l_{ijk} is the transfer distance of passenger k from origin i to destination j , s_{ij} is the shortest transfer distance from origin i to destination j .

w_{ij} is weight of original i and destination j , considering shortest distance and passenger flow of each OD pair, w_{ij} can also be calculated based on entropy weight coefficient method which can be found from Eq. (5) and Eq. (6).

3.3.4. Average waiting time u_{34}

Waiting time reflects the level of service of pedestrian service facilities such as ticket window, ticket machine, and security check. This indicator reflects the average waiting time of all passengers in transfer station, as shown in Eq. (13):

$$u_{34} = \frac{\sum_{i=1}^n \sum_{j=1}^{p_i} w_{ij}}{\sum_{i=1}^n p_i} \quad (13)$$

Where n is the number of service facilities in transfer station, p_i is the passenger flow of service facility i , w_{ij} is waiting time of passenger j in service facility i .

4. Application

In order to test the practicability of the dynamic evaluation system, this paper built a pedestrian simulation model of an intermodal transfer station and modeled four different scenarios about crowd management.

4.1. Pedestrian Simulation Model

The selected transfer station is SONGJIAZHUANG (SJZ) station in Beijing subway network. SJZ is a multi-models transfer hub. Passenger come from subway, bus,

long-distance bus, taxi and private car will transfer here. It is expected that, by 2016, 792,000 passengers will be transfer here a day. And, in the peak hours, about 113,200 passengers will transfer. It is undoubted that SJZ transfer hub will be one of the busiest hubs in Asia when it is finished. So, it is very necessary to evaluate the scenarios of facility design, pedestrian traffic organization and headway schedule before construction. Data preparation is the basic work for pedestrian simulation modeling. Generally, for each subway station, surrounding land use and facilities layout are quite different. So, pedestrian traffic characteristics and pedestrian flow organization plans are also different for each station. Therefore, in order to build a simulation model more close to the real situation, exact data preparation work need to be done from the view of pedestrian traffic characteristics, facility layout, operational organization and other aspects, as shown in Table 2. Detail information about the data used in the simulation model can be found from the previous research work [8].

Based on the simulation results, the dynamic evaluation indicators were calculated, as shown in Table 3.

Table 2 Data preparation for pedestrian simulation modeling

Data	Contents
Pedestrian characteristics	Speed distribution, route choice model, reaction of congestion and shopping time
Capacity of facilities	Auto-fare gate, security check, ticket window, ticket machine and checkout counters
Demand	Pedestrian traffic composition, arrival pattern, and OD distribution
Operation data of subway	Schedule, alight and boarding time
Facilities layout	Layout of pedestrian facilities
Pedestrian organization	Temp or Permanent fence, operation of Auto-fare gate, stairs, elevators or escalators

4.2. Calculation for best scenario

Many algorithms can be used to sort the best scenario, such as cosine function, linear assignment, matter-element analysis [15] and fuzzy logic[16-17]. This paper used matter-element analysis to calculate the value of decision-making of four scenarios based on the dynamic evaluation indicators.

The Matter-Element Analysis (MEA) is proposed to handle problems with contradictions and incompatibility using a set of matter element based correlation transformations [18]. The main theories of this analysis are the definition of matter elements, extension mathematics, and the matter element transformation theory. A matter element is a representation of the characteristics of the object under study, which can be

defined using an ordered triad such as $ME = (N, C, V)$. Where N denotes the name of the matter, C is its characteristic (or representative parameter), and V is called the "Field" session to store the measure of the characteristic, which can be a number, an interval, or a verbal description, etc. For matter elements with multiple parameters, C and V are represented as vectors [19], as shown in Eq. (14):

$$ME = (N, C, V) = \begin{bmatrix} N & C_1 & V_1 \\ & C_2 & V_2 \\ & \cdots & \cdots \\ & C_n & V_n \end{bmatrix} \quad (14)$$

Thus the matter elements of the four scenarios can be represented as Eq. (15):

$$ME_{original} = \begin{bmatrix} & S_1 & S_2 & S_3 & S_4 \\ u_{11} & 1.75 & 1.82 & 1.89 & 1.67 \\ u_{12} & 0.462 & 0.523 & 0.477 & 0.49 \\ u_{13} & 0.325 & 0.467 & 0.254 & 0.355 \\ u_{14} & 0.845 & 0.883 & 0.965 & 0.674 \\ u_{15} & 0.24 & 0.33 & 0.27 & 0.29 \\ u_{16} & 348 & 330 & 336 & 354 \\ u_{21} & 426 & 390 & 324 & 450 \\ u_{22} & 306 & 288 & 198 & 234 \\ u_{31} & 102 & 116 & 83 & 115 \\ u_{32} & 176 & 203 & 168 & 196 \\ u_{33} & 1.34 & 1.58 & 1.43 & 1.18 \\ u_{34} & 186 & 222 & 198 & 246 \end{bmatrix} \quad (15)$$

Because each element may be expressed in different units, a normalization process is generally applied, as Eq. (16):

$$ME_{normalized} = \begin{bmatrix} & S_1 & S_2 & S_3 & S_4 \\ u_{11} & 0.636 & 0.318 & 0.000 & 1.000 \\ u_{12} & 1.000 & 0.000 & 0.754 & 0.541 \\ u_{13} & 0.333 & 1.000 & 0.000 & 0.474 \\ u_{14} & 0.412 & 0.282 & 0.000 & 1.000 \\ u_{15} & 1.000 & 0.000 & 0.667 & 0.444 \\ u_{16} & 0.250 & 1.000 & 0.750 & 0.000 \\ u_{21} & 0.190 & 0.476 & 1.000 & 0.000 \\ u_{22} & 0.000 & 0.167 & 1.000 & 0.667 \\ u_{31} & 0.424 & 0.000 & 1.000 & 0.030 \\ u_{32} & 0.771 & 0.000 & 1.000 & 0.200 \\ u_{33} & 0.600 & 0.000 & 0.375 & 1.000 \\ u_{34} & 1.000 & 0.400 & 0.800 & 0.000 \end{bmatrix} \quad (16)$$

Thus, the standard matter element is defined as Eq. (17):

$$ME_{standard} = \begin{bmatrix} & S_- & S_+ \\ u_{11} & 0 & 1 \\ u_{12} & 0 & 1 \\ u_{13} & 0 & 1 \\ u_{14} & 0 & 1 \\ u_{15} & 0 & 1 \\ u_{16} & 0 & 1 \\ u_{21} & 0 & 1 \\ u_{22} & 0 & 1 \\ u_{31} & 0 & 1 \\ u_{32} & 0 & 1 \\ u_{33} & 0 & 1 \\ u_{34} & 0 & 1 \end{bmatrix} \quad (17)$$

So the decision value of scenario i can be calculated based on the following Eq. (18):

$$S_i = \sum_{j=1}^{PI} \left[w_j (S_+ - S_{ij}) \right]^2 - \sum_{j=1}^{PI} \left[w_j (S_{ij} - S_-) \right]^2 \quad (18)$$

Where PI is the number of indicators in transfer station, S_{ij} is the normalized value of indicator j in scenario i , w_j is weight of indicator j , w_j can also be calculated based on entropy weight coefficient method which can be found from Eq. (5) and Eq. (6).

The result was: $S_1 = -0.99581$, $S_2 = -0.12445$, $S_3 = -0.65961$, $S_4 = 0.01604$. Because $S_4 > S_2 > S_3 > S_1$, so the best scenario is Scenario 1.

Table.3 Evaluation indicator values of different scenarios

Evaluation indicators	Scenario 1(S_1)	Scenario 2(S_2)	Scenario 3(S_3)	Scenario 4(S_4)
Affect of conflict u_{11}	1.75	1.82	1.89	1.67
Flow imbalance of conflict u_{12}	0.462	0.523	0.477	0.49
Direction Imbalance of Conflict u_{13}	0.325	0.467	0.254	0.355
Affect of high density u_{14}	0.845	0.883	0.965	0.674
Distribution of high density u_{15}	0.24	0.33	0.27	0.29
Evacuation time u_{16}	348	330	336	354
Average transfer time u_{21}	426	390	324	450
Maximum average transfer time u_{22}	306	288	198	234
Average transfer distance u_{31}	102	116	83	115
Maximum average transfer distance u_{32}	176	203	168	196
Detour coefficient u_{33}	1.34	1.58	1.43	1.18
Average waiting time u_{34}	186	222	198	246

5. Conclusion

Developing transit system can effectively solve the traffic congestion problem in big cities. Improving

safety and convenience of transfer can attract more people to use public transport. It is useful to enhance level of service of urban public transport and keep the sustainable development of urban transport system in china. In this paper, a dynamic evaluation indicators

system for crowd management in transfer stations was proposed based on pedestrian simulation tool. Practical application showed that the dynamic evaluation indicators system could reflect pedestrian traffic status in transfer station accurately and it could be used to quantitatively evaluate the pros and cons of pedestrian facilities planning and layout, traffic organization and operations management in transfer station. Actually, except transfer stations, it could be used to evaluate crowd management in other place, such as subway station, commercial building and venues for special events.

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