

Fig. 2. The predigested block diagram of harmonic drives system.

III. PERFORMANCE ANALYSIS OF SINGLE SPEED LOOP

To make the system to track the given trajectory, it needs to design the closed loop controller for the system. It assumes that the speed loop controller is in the single loop system.

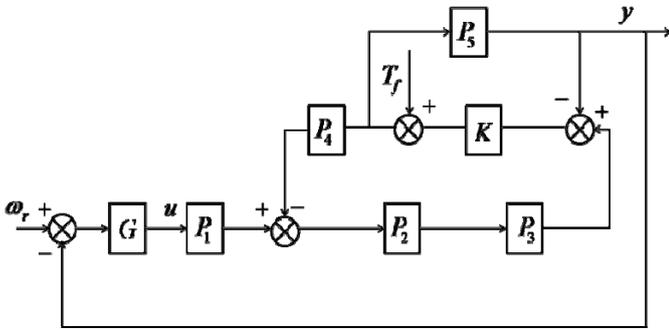


Fig. 3. The block diagram of single speed closed loop.

According to the block Fig. 3 of system, it can get the output y of system:

$$y = \frac{\frac{K}{N} P_1 P_2 P_5 G \cdot \omega}{1 + K P_5 + \frac{P_2 K}{N^2} + \frac{K}{N} P_1 P_2 P_5 G} + \frac{P_5 \cdot T_f}{1 + K P_5 + \frac{P_2 K}{N^2} + \frac{K}{N} P_1 P_2 P_5 G} \quad (2)$$

Generally, during designing the controller, since the reduction ratio of harmonic gear is large, the quadratic term of reduction ratio can be neglected. Then:

$$y = \frac{\frac{K}{N} P_1 P_2 P_5 G \cdot \omega}{1 + K P_5 + \frac{K}{N} P_1 P_2 P_5 G} + \frac{P_5 \cdot T_f}{1 + K P_5 + \frac{K}{N} P_1 P_2 P_5 G} \quad (3)$$

Besides, when the controller is designed, the bandwidth needs to meet:

$$|1 + K P_5 + \frac{K}{N} P_1 P_2 P_5 G| \gg 1. \quad (4)$$

Therefore, it can get:

$$y = \frac{\frac{1}{N} P_1 P_2 G \cdot \omega}{1 + \frac{1}{N} P_1 P_2 G} + \frac{\frac{1}{K} T_f}{1 + \frac{1}{N} P_1 P_2 G} \quad (5)$$

As the (5) shown, the disturbance of system is mainly restrained by the controller G(s). And the output of system also needs the controller to ensure tracking the given signal. Therefore, it must bring some difficult for adjusting the controller G(s).

On the other hand, in the (5), it can see that the stiffness coefficient of harmonic gear will have great influence on the system. Comparing with others driving, harmonic drive belongs to the flexible driving. So its stiffness coefficient K will be lower than others driving. This will cause that the friction of single speed loop will have the large influence than others driving.

IV. PERFORMANCE ANALYSIS OF DOUBLE SPEED LOOPS

To enhance the performance of system, the control method of double speed loops is introduced in the system. It assumes that the inner loop controller is G₁(s) and the outer loop controller is G₂(s). The control block of double speed loops is showed in Fig. 4.

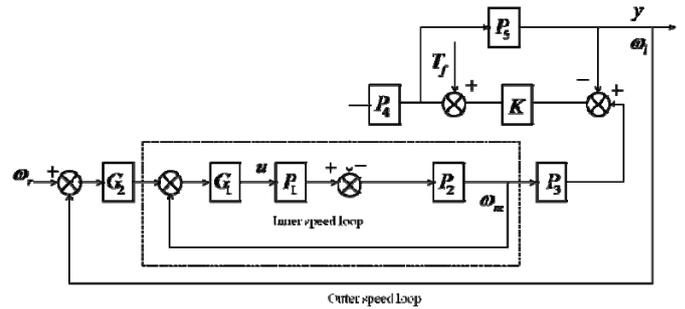


Fig. 4. The block diagram of double speed closed loops.

According to the control block of double speed loops, it can get that the output y of system is,

$$y = \frac{\frac{K}{N} P_1 P_2 P_5 G_1 G_2 \cdot \omega}{1 + K P_5 + \frac{P_2 K}{N^2} + \frac{K}{N} P_1 P_2 P_5 G_1 G_2 + P_1 P_2 G_1 + K P_1 P_2 P_5 G_1} + \frac{(P_5 + P_1 P_2 P_5 G_1) T_f}{1 + K P_5 + \frac{P_2 K}{N^2} + \frac{K}{N} P_1 P_2 P_5 G_1 G_2 + P_1 P_2 G_1 + K P_1 P_2 P_5 G_1} \quad (6)$$

Similarly, the quadratic term of reduction ratio is neglected. The bandwidth needs to meet:

$$|1 + KP_5 + \frac{P_2K}{N^2} + \frac{K}{N} P_1P_2P_5G_1G_2 + P_1P_2G_1 + KP_1P_2P_5G_1| \gg 1;$$

$$|1 + \frac{1}{N} P_1P_2G_1G_2 + \frac{P_1P_2G_1}{KP_5} + P_1P_2G_1| \gg 1. \quad (7)$$

It can get:

$$y = \frac{\frac{1}{N}G_2 \cdot \omega}{\frac{1}{N}G_2 + \frac{1}{KP_5} + 1} + \frac{T_f}{(\frac{K}{N}G_2 + \frac{1}{P_5} + K)P_1P_2G_1} + \frac{T_f}{\frac{K}{N}G_2 + \frac{1}{P_5} + K}. \quad (8)$$

In the (10), it can see that the output of system can be adjusted by the outer loop controller $G_2(s)$ and the disturbance of system can be adjusted by the inner loop controller $G_1(s)$. During the double speed loops, though the influence which is brought by the disturbance includes two parts, the stiffness coefficient of harmonic gear is still a large dimension. So the influence of last term will be lower than the influence in single speed loop. And the disturbance of the second term can be restrained by the controller $G_1(s)$. Therefore, by the coordination control of two controllers $G_1(s)$ and $G_2(s)$, the control precision of system can be enhanced effectively. The experiments of last section will state that the double speed loops will have a perfect performance in the harmonic drive system.

V. EXPERIMENT RESULTS

The high speed BLDC is selected as the driving motor. The maximum speed of the motor is 3000r/min. A rotary encoder which is installed in the motor side is selected as the position sensor. The reduction ratio of harmonic gear is 100. A tachometer and an optical encoder are installed in the load side, which can measure the velocity and angle position of load. To compare the control performance of two kinds of control methods, two kinds of controller are designed for the system. The given reference trajectory is $\theta = 4.5\sin(0.33t)^\circ$.

1) Single speed loop PI controller. The angle velocity of load which is measured by the tachometer is considered as the velocity feedback signal in the controller. The angle position of load which is measured by the optical encoder is considered as the position feedback signal. Then the speed loop controller and position loop controller can be designed.

2) Double speed loops PI controller. The angle velocity of motor which is got by differencing angle position signals of motor. Besides, it can use the angle velocity of load to design another speed loop controller. Finally, it can use the angle position of load to design the load position loop controller.

The tracking results of two controllers are shown in the Fig. 5 and Fig. 6. It can see that the precision of system has a big promotion when the controller of two speed loops is applied. When the single speed loop controller is applied, the maximum error of system is about 0.132'. But when the double speed loops controller is applied, the maximum error

of system is about 0.062'. The precision of system increase over one times.

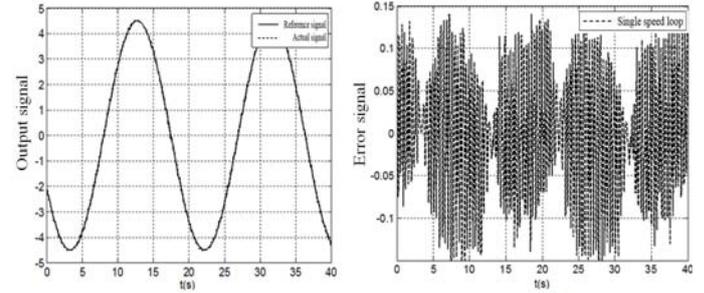


Fig. 5. The load tracking result of single speed closed loop.

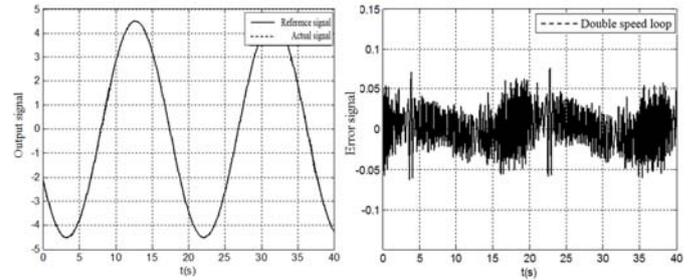


Fig. 6. The load tracking result of double speed closed loops.

VI. CONCLUSION

To solve these nonlinear problems of flexibility, backlash and friction, a kind of multi-loops control method based on double speed loops is proposed in this paper. Besides, the performance of two control structures is analyzed in theory. Finally, by comparing with the traditional single speed loop, it is stated that the harmonic drive system will have the higher tracking precision when the double speed loops control methods is applied. The system precision increases over one times.

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