

# Path planning for mobile robot using the novel repulsive force algorithm

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**Abstract.** A new type of repulsive force algorithm is proposed to solve the problem of local minimum and the target unreachable of the classic artificial potential field method in this paper. The Gaussian function that is related to the distance between the robot and the target is added to the traditional repulsive force, solving the problem of the goal unreachable with the obstacle nearby; variable coefficient is added to the repulsive force component to resize the repulsive force, which can solve the local minimum problem when the robot, the obstacle and the target point are in the same line. The effectiveness of the algorithm is verified by simulation experiments based on MATLAB.

## 1. Introduction

Robot path planning is an important part of the discipline of robotics. The idea of a path planning approach is to make the robot move from its starting point towards a destination point, while avoiding obstacles on its way [1]. There are many algorithms for robot path planning; the artificial potential field method is particularly attractive because of its mathematical elegance and simplicity [2]. The traditional artificial potential field method assumes that the target point of the robot has a strong appeal, while obstacles applied repulsive force to the robot, and with the robot close to obstacles, the repulsive force will become increasingly large, which means that around obstacles there exists a potential field, hindering the robot proximity [3]. However, this method has some inherent limitations. When the target point is near the obstacle, the robot cannot reach the goal and reciprocate oscillation around the target point because of the repulsion of the obstacle [4]. Due to the force balance, the robot will fall into local minimum and cannot avoid obstacle when the robot, the obstacle and the target point are in the same line [5]. To overcome the above two problems, the repulsive force function is improved in this paper.

## 2. The model of the APF

### 2.1 The model of the classic APF

The repulsive potential function of the obstacle takes the following equation by Khatib [6]:

$$\Phi = \begin{cases} \frac{1}{2} \eta \left( \frac{1}{\rho} - \frac{1}{\rho_0} \right)^2 & \rho < \rho_0 \\ 0 & \rho \geq \rho_0 \end{cases} \quad (1)$$

Where  $\eta$  is a positive gaining factor,  $\rho$  is the distance between the robot and the obstacle,  $\rho_0$  is a positive constant denoting the distance of influence of the obstacle, when  $\rho < \rho_0$ , the obstacle produces the effect of repulsion to the robot.

The negative gradient of the potential field is used as the virtual force acts on the robot, so the repulsive force is given by (2):

$$Frep = -grad(\Phi) = \frac{\eta}{\rho^2} \left( \frac{1}{\rho} - \frac{1}{\rho_0} \right) \left[ \frac{\partial \Phi}{\partial x}, \frac{\partial \Phi}{\partial y} \right] \quad (2)$$

The size of repulsive force is as follows:

$$|Frep| = \begin{cases} \frac{\eta}{\rho^2} \left( \frac{1}{\rho} - \frac{1}{\rho_0} \right) & \rho < \rho_0 \\ 0 & \rho \geq \rho_0 \end{cases} \quad (3)$$

The calculation of the angle between the robot and the obstacle is given by (4):

$$\theta = \arccos \left( \frac{x - x_o}{\sqrt{(x - x_o)^2 + (y - y_o)^2}} \right) \quad (4)$$

Where  $[x_o, y_o]$  is the coordinate of the obstacle.

## 2.2 The model of the modified APF

An improved repulsive force method is proposed aiming at the two problems of the target unreachable and the local minimum in this paper. To solve the problem of the target unreachable, the Gaussian function that is related to the distance between the robot and the target is added to the traditional repulsive force (5).

$$|Frep|_{modified} = \begin{cases} \frac{\eta}{\rho^2} \left( \frac{1}{\rho} - \frac{1}{\rho_0} \right) \left[ 1 - e^{-\frac{(x-x_g)^2 + (y-y_g)^2}{R^2}} \right] & \rho < \rho_0 \\ 0 & \rho \geq \rho_0 \end{cases} \quad (5)$$

In comparison with the equation (3), the equation (5) solves the problem of repulsive effect at the target point which is within the distance of influence of the obstacle, ensuring the force balance of the robot. Taking into consideration the robot's radius, it makes the path more secure and reliable at the same.

In order to make the robot escape from the local minimum, the variable coefficients are added to the components of the repulsive force in the X and Y axes, the equations are given by (6) and (7).

$$|FrepX| = \begin{cases} (1 + \alpha) |Frep|_{modified} * \cos \theta & \rho < \rho_0 \\ 0 & \rho \geq \rho_0 \end{cases} \quad (6)$$

$$|FrepY| = \begin{cases} (1 + \beta) |Frep|_{modified} * \sin \theta & \rho < \rho_0 \\ 0 & \rho \geq \rho_0 \end{cases} \quad (7)$$

Where  $\alpha$  and  $\beta$  are the constants of -1 to 1, (6) and (7) are designed to change the direction of the repulsive force through altering the size of the repulsive in the X axis and the Y axis. Such a change is able to transfer the direction of the robot's resultant force, leading the robot to march to the target and escape the local minimum point avoiding the obstacles. It can be concluded that  $\alpha$  and  $\beta$  should not be given the same value, otherwise, the direction of the repulsive force will not be changed and the robot cannot escape from the local minimum.

## 3. Simulation

In order to verify the effectiveness of the algorithm, this paper uses MATLAB to carry out the simulation experiment.

The position of the goal is (50, 50), the obstacles are (15, 18), (30, 35), (52, 53), the distance of influence of obstacle  $\rho_0 = 30$ ,  $\eta = 300$ , the radius of the robot is  $R = 8$ . It can be seen from Fig.1 that the modified repulsive force algorithm has solved the problem of goal unreachable; the robot is

not affected by the obstacle (52, 53).

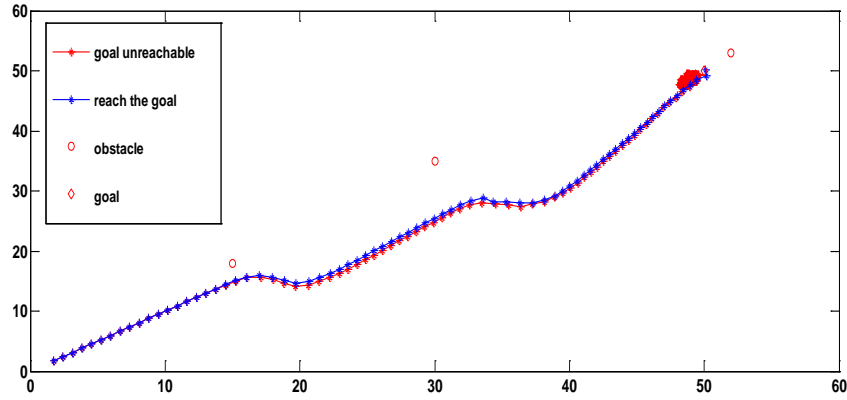


Fig.1 solved the goal unreachable

Take the variable coefficients  $\alpha = -0.8$ ;  $\beta = 0.8$  the obstacles are (15,15), (20,25), (30,35), other parameters are same as the Fig.1. It can be seen from Fig.2 that the robot escapes from local minimum after add the coefficients in the components of the repulsive force.

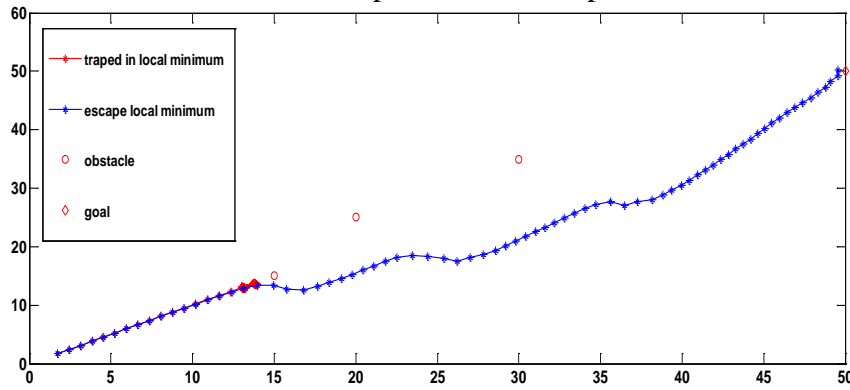


Fig.2 escape from local minimum

Set the obstacles coordinates are (15,15), (20,25), (30,35), (40,40), (52,53), other parameters are the same as above.

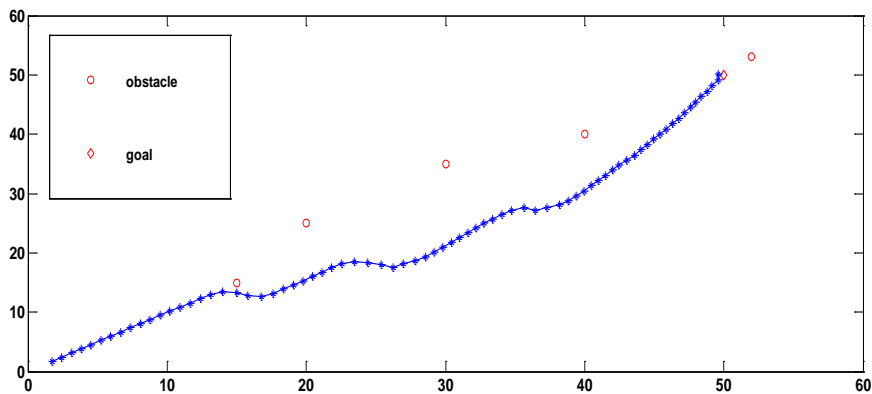


Fig.3 Path planning in two cases

In the Fig.3, the two cases of the problems of the local minimum and the goal unreachable are overcome by the improved repulsive method. After the robot escaped from the local minimum point, the robot continues to get closer to the target and eventually stopped at the goal without the influence of the obstacle.

Set  $\alpha = -0.5$ ,  $\beta = 0.5$  other parameters are the same as Fig.3; the path is as Fig.4.

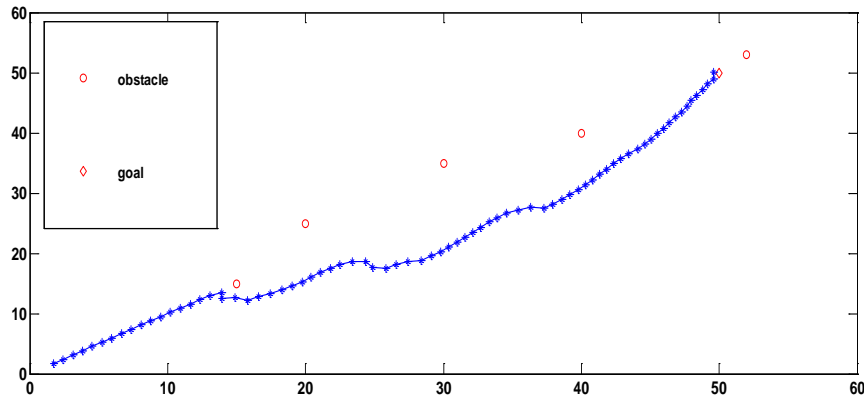


Fig.4 Path of different variables

In comparison with Fig.3, Fig.4 indicates when the variable coefficients are changed; the smoothness of the path in which the robot escapes from local minimum is also changing.

#### 4. Summary

Through the simulation experiments, it can be observed that when the target is in the range of influence of the obstacle; the proposed repulsive algorithm avoids the robot to be affected by the obstacle and solves the problem of goal unreachable. Moreover, by changing the size of the repulsive force in the X axis and the Y axis, we can overcome the problem of the local minimum on the condition that the robot, the obstacle and the target are at the same line. In addition, it can be seen from the Figure 3 and Figure 4 that the values of the variables that are added to the components of the repulsive force will affect the escaping path from the local minimum of the robot, if the value is not appropriate, the path of the robot may have a mutation and lead easily to an oscillation.

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