

# Numerical Simulation of GTM Asphalt Mixture Design Parameters Based on Discrete Element

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**Abstract.** The laboratory compaction method produces a huge effect on the design of mix proportion and performance testing of asphalt mixes. For the result of a performance test to yield reliable physical properties, it is necessary to ensure that laboratory specimens are fabricated in a manner that adequately simulates field compaction. However, the laboratory compaction based on Gyratory Testing Machine(GTM) is closed to field compaction.

This study simulated the compacting process of asphalt mixes based on GTM, and analyzed the displacement, stress and strain to changes in mold in order to reveal the physical properties during compacting by using discrete element theory.

The results indicated that the design method based on GTM is reasonable and adaptability, and the basic requirements that GSI must be less than or equal to 1.0, and GSF must be great than or equal to 1.0 is scientific. What is more, the study presents the reasonable value range of design parameters to GSI and GSF for engineering application, which is referred to in the study as GSI can be less than or equal to 1.05, and GSF can be great than or equal to 1.3.

## Introduction

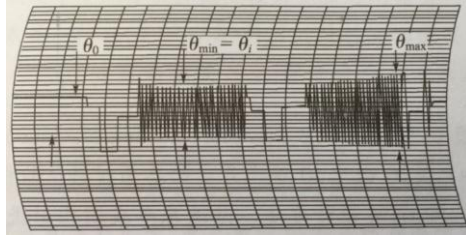
The corps of engineers invents Gyratory Testing Machine in the United States in the 1960 s in order to solve the design and research of air heavy bombers airport pavement, and it is in ASTM specification in 1978 in the United States<sup>[1]</sup>. The basic premise of the GTM method of surface courses mix design is that the test should empoly the tire contact pressure and compact the test specimen to the pavement density that will ultimately develop in a roadway under traffic<sup>[2]</sup>. The design density and bitumen content should be those values corresponding to the minimum bitumen content at which an increase in the gyratory angle is observed<sup>[3]</sup>. For bitumen contents higher than this the bitumen begins to display aggregate and the phenomenon of reduction in shear strength with increased compaction occurs. This manifests itself during the GTM compaction test by a progressive increase in the gyratory angle and by a reduction in roller pressure<sup>[4]</sup>.

However, the GSF value obtained should exceed one in order to insure against permanent shear deformation ie rutting in the wheel path. The GSF is not a valid measure of measure of stability when the GSI value exceed one because a GSI value greater than one indicates that the mix is on the rich side of compaction curve and progressive rutting will occur under hot weather traffic[5]. What is more, some researchers in China consider that the GSI value should less than or equal to 1.05 and the GSF value should exceed 1.3. The standard was more applied in Hebei province[6]. However, the value of GSI and GSF is an empirical value without a theory. It is necessary to follow some methodologies to model to study the reasonable value range of GSI and GSF.

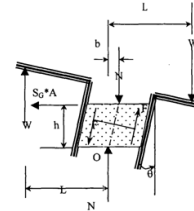
## Analysis of GSI and GSF

Gyratory Stability Index is expressed as the radio of measured shear strain  $\theta_{\max}$  at equilibrium state to the induced minimum shear strain  $\theta_{\min}$ , ie  $GSI = \theta_{\max} / \theta_{\min}$ . As shown in figure 1(a). The factor of

safety with regard to shear is expressed as the ratio of measured shear strength  $S_G$  to the induced maximum shear  $\tau_{\max}$ , ie  $GSF = S_G / \tau_{\max}$ .  $S_G$  is calculated by Eq. 1, the meaning of parameters is shown in figure 1(b).



(a) the relationship between shear strain and times



(b) mechanical characteristic

Fig. 1 parameters of GTM

$$S_G = \frac{2 \times (P \times L - F \times a) + N \times b}{A \times h} \times \left( \frac{\theta_{\max}}{\theta_0} \right) \quad \text{Eq. 1}$$

In addition, a stable mix does not show a significant increase in the gyratory angle during the compaction and the roller pressure does not show a significant decrease.

**Modeling and analysis of mechanism of GSI.** Whether stress and strain is in the elastic or plastic deformation range when asphalt mixture occurs a rotation angle can be considered as the decision criteria of the allowed angle, namely the value judgement standard of the GSI value.

Uniformly distributed load  $P$  is on both ends of asphalt mixture which use rigid board restrictions on both sides. When the reference angle is  $\theta$ , the rotation angle  $A$  of rigid plate is regarded as input, taking a analysis of the internal stress and strain response of asphalt mixture. At this point,  $\theta$  can be regarded as the induced minimum shear strain  $\theta_{\min}$ ,  $(\theta + A)$  can be regarded as the measured shear strain  $\theta_{\max}$  at equilibrium state. Gyratory Stability Index is expressed as the ratio of  $(\theta + A)$  to  $\theta$ , ie  $GSI = (\theta + A) / \theta$ .

Taking  $P$ ,  $\theta$  and  $(\theta + A) / A$  as variables,  $P = 0.7 \text{ MPa}, 0.9 \text{ MPa}, 1.1 \text{ MPa}$ ,  $\theta = 0^\circ, 0.8^\circ, 1.2^\circ$ ,  $(\theta + A) / A = 1.0, 1.05, 1.08$ . Through different combinations of the value of variables, the reasonable value range of GSI can be inferred by judging whether stress and strain is in the elastic or plastic deformation range.

**Modeling and analysis of mechanism of GSF.** As shown in fig.1(b), shear strength  $S_G$  is calculated based on two-dimensional model which contains a series of assumptions without considering vertical pressure and the viscoelasticity-anelasticity of asphalt mixture. The paper bulids two-dimensional numerical analysis model to explain shear strength  $S_G$ .

Using static analysis model, uniformly distributed load  $P$  is on both ends of asphalt mixture. Taking  $P$  and  $\theta$  as variables,  $P = 0.7 \text{ MPa}, 0.9 \text{ MPa}, 1.1 \text{ MPa}$ ,  $\theta = 0^\circ, 0.8^\circ, 1.2^\circ$ . Building the relationship between  $S_G$  and  $W$ . The reasonable value range of GSF can be inferred by comparing the relationship with Eq. 1.

## Numerical simulation based on the discrete element

Particle Follow Code 2 Dimension (PFC2D) is a kind of effective means to simulate the movement and interaction of circular particle medium the solid mechanics and particle flow problem.

The structure model in PFC2D software is a two-dimensional aggregate made up of hundreds to tens of thousands of typical circular particles, which assumed to be the rigid body. The internal force between particles based on GTM is transmitted through the contact and bite, the deformation of material under loads comes from sliding, rotation, opening and closure along the contact surface between particles mainly. It can be inferred that numercial simulation based on the discrete element can reveal the physical properties of asphalt mixture based on GTM.

The asphalt mixture particle can be considered as the particle flow code unit when modeling. Structuring different shape of asphalt mixture particles, and simulating the effects of particles in asphalt mixture. Using four basic shape of particles and their combination to study the changing rules

of the displacement , deformation and stress in the process of compaction. As shown in fig.2(a). Numerical simulation model and boundary conditions are shown in fig.2(b) and (c).

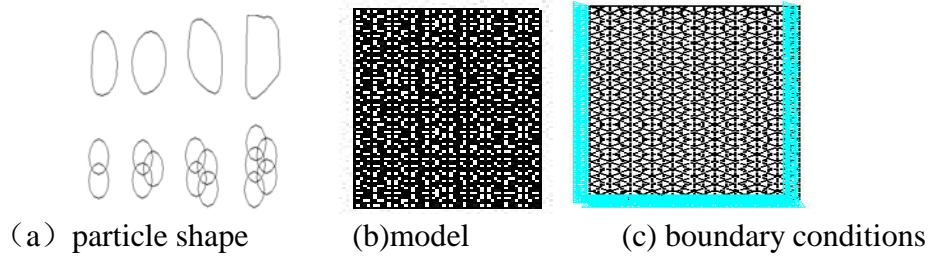


Fig. 2 Numerical simulation analysis

The basic parameters of asphalt mix are shown in Table 1 and Table 2, temperature is shown in Table 3.

Table 1 Mechanical parameters

Particle paraments	Number	Initial void ratio (%)	dry density (g/cm <sup>3</sup> )	Diameter (mm)	Normal contact stiffness (N/m)	Tangential contact stiffness (N/m)	Normal bond strength (N)	Tangential bond strength (N)
Asphalt mix	2000	15%-16%	3	0.075-26.5	$8.2 \times 10^8$	$6.0 \times 10^8$	0	0

Table 2 Other parameters

Elasticity modulus (MPa)	Normal elasticity coefficient kn(MPa)	Tangential elasticity coefficient kt(MPa)	Damping coefficient of the quality ( $\alpha$ )	Friction coefficient ( $\mu$ )	Time step (s)
2.2	Eb/2(R1+R2)	0.2kn	0.05	0.3	0.0005

Table 3 The value of temperture ( °C )

Field temperature	Paving temperature	Initial pressure	Re-pressing	Termination
160~170	150~160	140~160	135~150	90~100

## Results of numerical simulation

### Results of GSI.

**( $\theta+A$ )/A=0.95.** Partial enlarged vector diagram of stress, strain and displacement deformation is shown in fig.3. All of them turn out to be elastic changes, uniform distribution and no obvious plastic deformation.

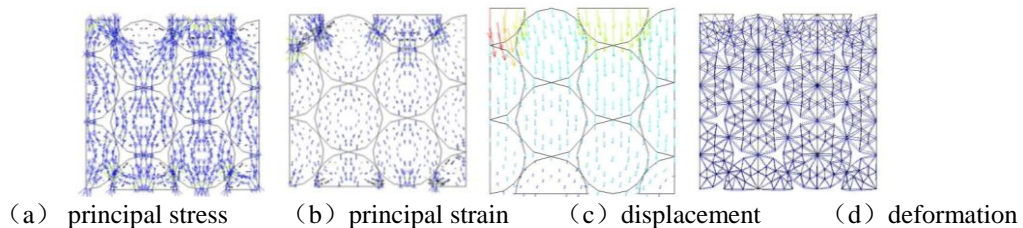


Fig.3 Partial enlarged vector diagram ( $\theta + A$ )/A=0.95

**( $\theta+A$ )/A=1.00.** Partial enlarged vector diagram of stress, strain and displacement deformation is the same with ( $\theta+A$ )/A=0.95. All of them turn out to be elastic changes, uniform distribution and no obvious plastic deformation.

**( $\theta+A$ )/A=1.05.** Most of them turn out to be elastic changes, uniform distribution. But plastic deformation occurs, which is not so large to cause damage. As shown in fig.4.

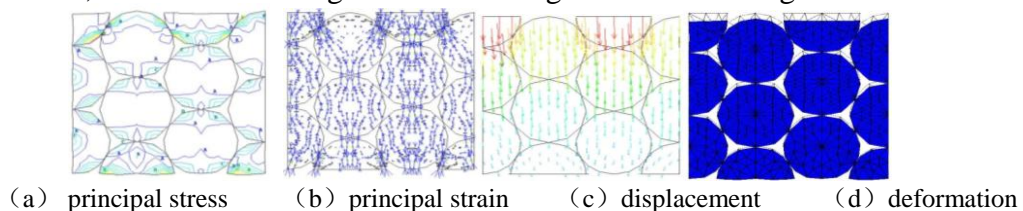
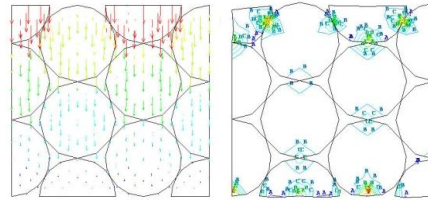


Fig.4 Partial enlarged vector diagram ( $\theta + A$ )/A=1.05

$(\theta+A)/A=1.06$ . Plastic deformation is lagrer and the plastic damage occurs, which can be considered to be cut-off point between elastic changes and plastic changes. As shown in fig.5. It can be inferred that  $(\theta+A)/A$ , ie GSI, should be not exceed 1.05.

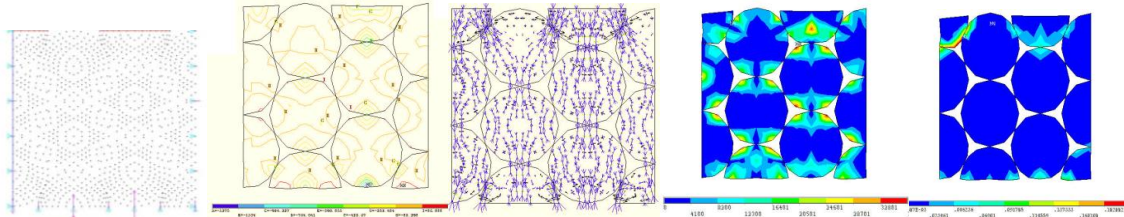


(a) displacement (b) plasticity stress

Fig.5 Partial enlarged vector diagram  $(\theta +A) /A=1.06$

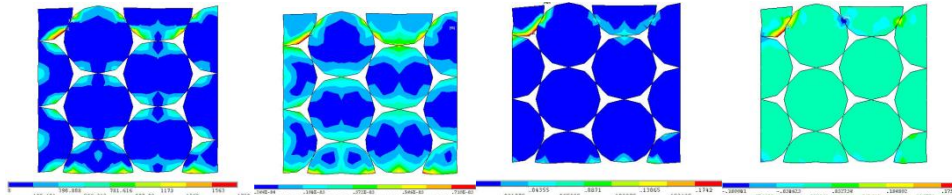
### Results of GSF.

The parameters are the same with GSI in calculating GSF. Numerical simulation model and boundary conditions are shown in fig.6(a).



(a)Model (b)principal stress (1.0) (c)principal strain (1.0) (d)principal stress(1.3) (e) principal strain(1.3)

Fig.6 Model and Partial enlarged vector diagram (0.7Mpa)



(a) principal stress (1.5) (b) principal strain (1.5) (c) principal strain (1.8) (d) principal strain inXY (1.8)

Fig.7 Partial enlarged vector diagram (0.9Mpa、 1.1Mpa)

The vertical pressure equals 0.7 Mpa in fig.7, the GSF value equals 1.0 in (b)(c), the GSF value equals 1.3 in (d)(e). The vertical pressure equals 0.9 Mpa and the GSF value equals 1.5 in fig.8(b)(c). The vertical pressure equals 1.1 Mpa and the GSF value equals 1.8 in fig.8(d)(e).

As shown in fig.6 and fig.7, changing the parameters (pressure stress, GSF) influenced the value of stress, strain ,displacement and deformation.It is possible to simulate the physical properties of particles by changing the parameters. Increasing the GSF assited in developing dynamic pressure, shearing strength and compaction. SGC increases to 1.8, physical properties of asphalt mixture shifted from the linear elastic range to elastic-plastic deformation, asphalt mixture particles began to appear broken, and compaction began to appear not obvious .

The relationship between  $S_G$  and  $W$  can be inferred by Cramer method. As shown in Eq. 2.

$$S_G = (1.85 \times W \times L) / (A \times h) \quad \text{Eq. 2}$$

$GSF \geq (1.85 \times 1.3) / 2 = 1.2$ . To avoid the plastic deformation, in order to guarantee the stability of materials, GSF should be greater than 1.3.

### Entity engineering

The results of experiment with field cores of rut section in GZ expressway are shown in table 4. The results indicated that the different field core in location and severity in GZ expressway produces similar numerical range of GSI and GSF ,which is GSI should be not exceed 1.05 and GSF should be exceed 1.3.

Table 4 The results of rotary shear test in GZ expressway

Structural layer	The compaction times (lap)	GSI	GSF
The top layer	284	1.07	1.54
	202	1.05	0.97
	300	1.03	2.04
	262	1.05	1.52
The following layer	156	1.12	1.04
	244	1.08	1.27
	320	1.05	2.21
	240	1.08	1.51

## Conclusions

This study simulated the compacting process of asphalt mixes based on GTM, and analyzed the displacement, stress and strain to changes in mold in order to reveal the physical properties during compacting by using discrete element theory.

The results indicated that the design method based on GTM is reasonable and adaptability, and the basic requirements that GSI must be not exceed 1.0, and GSF must exceed 1.0 is scientific. What is more, the study presents the reasonable value range of design parameters to GSI and GSF for engineering application, that is GSI should not exceed 1.05, and GSF should exceed 1.3.

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