

Transmission module partition method based on fuzzy clustering

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Abstract. The transmission is widely used in various sectors of the important machinery and equipment, In this paper, based on fuzzy clustering analysis, the module of transmission is studied. Construct transmission components function and geometric correlation matrix, corresponding to the fuzzy equivalence matrix, and thus of the transmission were module division. By dividing the module of transmission and improve the efficiency of rapid design, laid the foundation for the different needs of transmission and more rapid response to the market.

Introduction

In the increasingly fierce competition in the market, large-scale custom production requires companies to respond quickly to market, to provide customers with low-cost, personalized products in the shortest time[1]. The product's modular design due to the relatively small number of parts can be used to reduce the cost of the product design, ease of disassembly recycling and maintenance or replacement, and easy to assemble, improving the product reusability and reconstruction. Thus, the modular design has become a mass product ordered most important success factor.

The modular design of the products is divided into two parts, module division and combination, reasonable module partition is the foundation and the key in modular design[2].

In recent years, some scholars at home and abroad have been studied in the field of modular design. Gu and Sosale[3][4] proposed life cycle oriented modular design methods, using genetic algorithm and simulated annealing algorithm to solve and optimize the model, and the designers of partition scheme, choose the best scheme, so as to realize the modular. National University of Defense Technology Li Guoxi[5] will iterative design topological model and modular combination, and discusses the dynamic modeling method, the function principle of behavior structure, modular design method is proposed based on analysis of the iterative process. Gao Fei[6] and so on from the point of view of product features, Proposed guidelines for functional module division and demand, established evaluation model based on coupling degree program. Zhejiang University Pan Shuangxia[7] taking into account the needs of customers, product assembly and equipment maintenance and other factors, put forward relevant guidelines and evaluation methods of fuzzy clustering based on information entropy. Xiangtan University Zhou Youhang[8], taking into account the complex mechanical product parts from the property, put forward a module partition method based on the important core part. Tang Tao[9] introduces the concept of green design, using the analytic hierarchy process and the green criteria for module division. Transmission as a widely used in automobiles, petrochemicals, agriculture, medicine, food, chemical and other industries of machinery and equipment, study the rapid design system, whether their own development, or the promotion of business interests are of great significance. The modular technology as a core technology to rapidly design, the design of the study transmission has not been molding applications. In this paper, the module partition method based on fuzzy clustering analysis method is adopted to divide the transmission to improve the design efficiency.

Transmission Introduction

Transmission is by way of a fixed or sub-file to change the output shaft and the input shaft of the transmission gear ratio of the transmission, traditionally based on different ratios, the transmission

are divided into two categories, A continuously variable transmission and the step transmission. In this paper, a continuously variable transmission(CVT) for the study, mainly comprising 24 parts (see Table 1), a cross-sectional view shown in Figure 1.

Table 1 parts list of continuously variable transmission

No	Name	No	Name
1	Eccentric bearing	13	Speed handle
2	Eccentric wheel	14	Small shaft
3	Input shaft	15	Output arm
4	Speed connecting shaft	16	Clutch
5	Left Speed Bearings	17	Output drive shaft
6	Right Speed Bearings	18	Output arm spring
7	Drive arm	19	Output drive gear
8	Drive arm bearing	20	Cover
9	Drive arm spring	21	Apron
10	Actuator box	22	Output shaft
11	Speed connecting block	23	Output gear
12	Fixed bearing	24	Output mechanism box

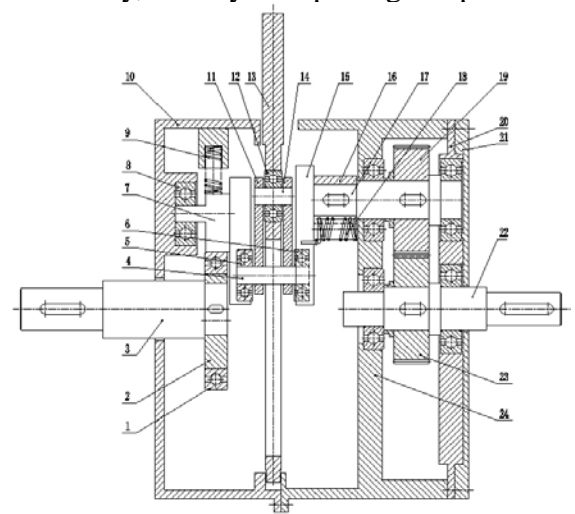


Figure 1 A cross-sectional view of CVT

Module Division of Mathematical Methods

Divide the product modules, mainly to the function and structure of the product of decomposition, and then by mathematical methods to analyze data decomposition and division. In this paper, we use the function correlation and structure correlation to establish matrix in the process of module division. Then the fuzzy clustering analysis algorithm to analysis and solve the problem.

Fuzzy clustering analysis.

When using the traditional method of transitive closure, it is needed to establish the fuzzy equivalent matrix on the X. But the disadvantage of this approach is the calculated amount is very large, because often order matrix will be very high. Using the direct clustering method, the amount of calculation will be much smaller, and it is easy to understand. The so-called direct clustering method is a method of fuzzy similarity clustering matrix R directly use, is not necessary to calculate its transitive closure. Principles of its clusters are: x_i and x_j grade in the horizontal \Leftrightarrow In the fuzzy clustering Figure R formed in the presence of a significant right of way than or equal to λ connection x_i and x_j . Direct clustering methods include two categories, netting and maximum tree method, consistent with their core principles, the difference is netting method is a direct form of clustering method, and the largest tree method is a graphical method of direct clustering method, In contrast, netting method more intuitive and clear.

The so-called netting method is to take a λ levels, fuzzy similar matrix R for λ - intercept array R_λ , write symbolic elements in the main diagonal λ - intercept matrix R_λ . In the lower part of the main diagonal with an asterisk "*" instead of 1, spaces instead of 0. And from the "*" the location of the vertical line upward lead, lead horizontal line to the right, through the contact points are connected to each other in order to achieve classification. Now take the domain $X = \{I, II, III, IV, V\}$ have similar matrix R:

$$R = \begin{bmatrix} 1 & 0.88 & 0.68 & 0.24 & 0.12 \\ 0.88 & 1 & 0.88 & 0.24 & 0.12 \\ 0.68 & 0.88 & 1 & 0.36 & 0.24 \\ 0.24 & 0.24 & 0.36 & 1 & 0.72 \\ 0.12 & 0.12 & 0.24 & 0.72 & 1 \end{bmatrix}$$

When $0.7 < \lambda \leq 0.8$, get:

$$R_{0.7} = \begin{bmatrix} 1 & & & & \\ * & 1 & & & \\ & * & 1 & & \\ & & & 1 & \\ & & & * & 1 \end{bmatrix}$$

To analyze the type of netting by an asterisk "*" to the right lead up straight, to give the results shown below. {I, II, III}, {IV, V}.

$$R_{0.7} = \begin{bmatrix} I & & & & \\ * & II & & & \\ & * & III & & \\ & & & IV & \\ & & & * & V \end{bmatrix}$$

Since the value of λ can be within the [0,1] range, when λ different values, the matrix R classification will also change, constituting a different classification by changing the value of λ and thus the formation of the elements in between dynamic clustering map, dynamic clustering view of the similarity matrix R shown in Figure 2.

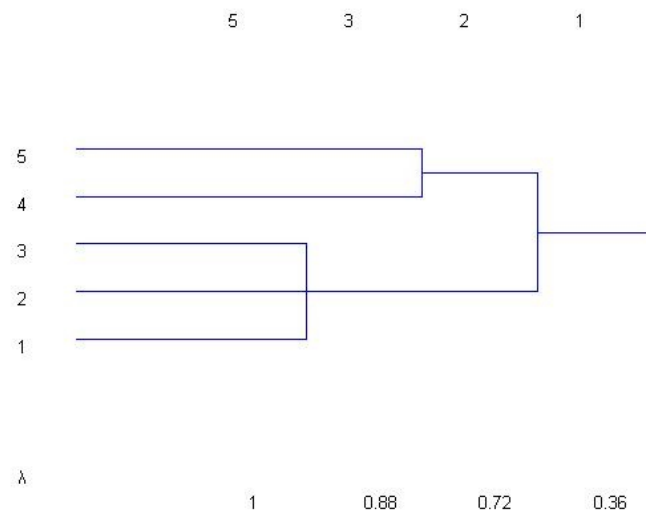


Figure 2 Dynamic clustering map

Correlation Analysis.

In the module division of the process, only a certain correlation components will be combined in the same module, the paper from the functional correlation and geometric correlation between two aspects to analyze.

Independent function is an important characteristic of a module, in the process of module partition, in order to improve the functional independence of modules, will achieve the same function parts combined together, and that these combinations in between the parts together with correlation function, which is defined as table 2 shows [10].

Table 2 functional definition of the two parts

RELATIONSHIP	Relevance	Correlation value
To accomplish certain functions, must be used in pairs	Very Strong	1.0
To accomplish the same function, there is a flow of energy	Strong	0.8
Presence information flow, have some relevance, interaction	Medium	0.6
The existence of material flow, moderate association	Weak	0.4
Functional differences exist essentially independent	Very Weak	0.2
There is no relationship	None	0

Geometric relativity refers to the physical connection between parts of the geometry and spatial relations, fastening, verticality, size, parallelism and coaxial degree. Through the contrast analysis, primarily from the connection relation and the geometric relationship accounted for the two important proportion of aspects to consider the geometric correlation between components, which is defined as shown in Table 3.

Table 3 definition of geometric correlation between two parts

RELATIONSHIP	Relevance	Correlation value
Tight junctions, is difficult to split, such as welding	Very Strong	1.0
With strict tolerances, it is difficult to split the connection.	Strong	0.8
With tolerance requirements, fixed connection, easy to split	Medium	0.6
With the size of the general requirements, it is easy to split	Weak	0.4
Contact, but no fit size	Very Weak	0.2
Not connected	None	0

Construction of the correlation matrix.

According to the theory, it can build functional parts respectively associated sub-matrix A_m and geometric correlation sub-matrix A_n , each relevant matrix by the designer based on the correlation function or geometric definition assessment. Then, the fuzzy relation matrix of components is built according to the related function sub matrix and the geometric sub matrix $A_{n \times n}$, Using R_{ij} to express the correlation between i and j two parts, and its algorithm is:

$$R_{n \times n} = \begin{cases} \omega_1 A_{ij}^m + \omega_2 A_{ij}^n & (i \neq j) \\ 1 & (i = j) \end{cases} \quad (i, j \in \{1, 2, \dots, n\}) \quad (1)$$

In the above formula: A_{ij}^m —Function relevance between i and j ;

A_{ij}^n —Geometric relevance between i and j ;

ω_1 —Function correlation weighting factor;

ω_2 —Geometric correlation weighting factor;

Analytic Hierarchy Process (AHP) or according to the designer's own experience can be obtained for each correlation weighting factor, $\sum_{k=1}^n w_k = 1$. And fuzzy relationship matrix is symmetric matrix:

$$R = \begin{bmatrix} R_{11} & R_{12} & \cdots & R_{1n} \\ R_{21} & R_{22} & \cdots & R_{2n} \\ \vdots & \vdots & \vdots & \vdots \\ R_{n1} & R_{n2} & \cdots & R_{nn} \end{bmatrix}$$

Correlation matrix fuzzy clustering analysis method.

Obtained after the relevant fuzzy relation matrix R through the above steps, the use of fuzzy cluster analysis fuzzy clustering. Take different thresholds λ fuzzy equivalent matrix \tilde{R} interception get different intercept array R_λ , where:

$$R_\lambda(i, j) = \begin{cases} 1, R(i, j) \geq \lambda \\ 0, R(i, j) < \lambda \end{cases}$$

In the same row or column intercept array, the elements of the aggregate value of 1 becomes the same module, others into one another, so that each element is divided into different modules. When λ change between 1-0, they will have different classification result, a dynamic clustering module. According to this principle, applied to specific related products, select an appropriate value λ , will be able to get the last module division scheme.

CVT module division

According to the above steps, first of all, to calculate the correlation between the various parts. For example, eccentric wheel bearings and eccentric wheel, in the transfer of power to complete the input function, mutual coordination. So its functional relevance takes 0.8, geometric correlation takes 1.0. According to equation (1) weighting coefficients ω_1 and ω_2 respectively, 0.6 and 0.4. Calculated to obtain the correlation eccentric bearing and the eccentric 0.88, the correlation can be calculated the same way all the other parts, through the correlation analysis and calculate the fuzzy relation matrix R:

$$R = \begin{bmatrix} 1.00 & 0.88 & 0.68 & 0.24 & 0.12 & 0.12 & 0.64 & 0.60 & 0.80 & 0.72 & 0.12 & 0.00 & 0.00 & 0.00 & 0.12 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 \\ 0.88 & 1.00 & 0.88 & 0.24 & 0.12 & 0.12 & 0.72 & 0.72 & 0.60 & 0.80 & 0.12 & 0.00 & 0.00 & 0.00 & 0.12 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 \\ 0.68 & 0.88 & 1.00 & 0.36 & 0.24 & 0.12 & 0.60 & 0.52 & 0.72 & 0.62 & 0.12 & 0.00 & 0.00 & 0.00 & 0.12 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 \\ 0.24 & 0.24 & 0.36 & 1.00 & 0.72 & 0.72 & 0.32 & 0.12 & 0.12 & 0.00 & 0.72 & 0.56 & 0.56 & 0.52 & 0.20 & 0.12 & 0.12 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 \\ 0.12 & 0.12 & 0.24 & 0.72 & 1.00 & 0.80 & 0.24 & 0.24 & 0.12 & 0.00 & 0.52 & 0.48 & 0.44 & 0.32 & 0.24 & 0.12 & 0.12 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 \\ 0.12 & 0.12 & 0.12 & 0.72 & 0.80 & 1.00 & 0.24 & 0.16 & 0.00 & 0.00 & 0.52 & 0.48 & 0.44 & 0.32 & 0.60 & 0.12 & 0.12 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 \\ 0.64 & 0.72 & 0.60 & 0.32 & 0.24 & 0.24 & 1.00 & 0.80 & 0.72 & 0.40 & 0.32 & 0.12 & 0.12 & 0.12 & 0.40 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 \\ 0.60 & 0.72 & 0.52 & 0.12 & 0.24 & 0.16 & 0.80 & 1.00 & 0.44 & 0.60 & 0.12 & 0.12 & 0.12 & 0.00 & 0.12 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 \\ 0.80 & 0.60 & 0.72 & 0.12 & 0.12 & 0.00 & 0.72 & 0.44 & 1.00 & 0.72 & 0.12 & 0.12 & 0.12 & 0.00 & 0.12 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 \\ 0.72 & 0.80 & 0.62 & 0.00 & 0.00 & 0.00 & 0.40 & 0.60 & 0.72 & 1.00 & 0.12 & 0.12 & 0.20 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 \\ 0.12 & 0.12 & 0.12 & 0.72 & 0.52 & 0.52 & 0.32 & 0.12 & 0.12 & 0.12 & 1.00 & 0.80 & 0.80 & 0.68 & 0.24 & 0.00 & 0.12 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 & 0.56 & 0.48 & 0.48 & 0.12 & 0.12 & 0.12 & 0.12 & 0.80 & 1.00 & 0.88 & 0.72 & 0.24 & 0.00 & 0.12 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 & 0.56 & 0.44 & 0.44 & 0.12 & 0.12 & 0.12 & 0.20 & 0.80 & 0.88 & 1.00 & 0.88 & 0.24 & 0.00 & 0.12 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 & 0.52 & 0.32 & 0.32 & 0.12 & 0.00 & 0.00 & 0.00 & 0.68 & 0.72 & 0.88 & 1.00 & 0.24 & 0.00 & 0.12 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 \\ 0.12 & 0.12 & 0.12 & 0.20 & 0.24 & 0.60 & 0.40 & 0.12 & 0.12 & 0.00 & 0.24 & 0.24 & 0.24 & 0.24 & 1.00 & 0.72 & 0.60 & 0.52 & 0.52 & 0.12 & 0.24 & 0.32 & 0.40 & 0.32 & 0.40 & 0.32 \\ 0.00 & 0.00 & 0.00 & 0.12 & 0.12 & 0.12 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.72 & 1.00 & 0.64 & 0.40 & 0.52 & 0.20 & 0.12 & 0.24 & 0.32 & 0.20 & 0.20 \\ 0.00 & 0.00 & 0.00 & 0.12 & 0.12 & 0.12 & 0.00 & 0.00 & 0.00 & 0.00 & 0.12 & 0.12 & 0.12 & 0.12 & 0.60 & 0.64 & 1.00 & 0.72 & 0.72 & 0.12 & 0.24 & 0.52 & 0.60 & 0.52 & 0.52 \\ 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.52 & 0.40 & 0.72 & 1.00 & 0.52 & 0.88 & 0.32 & 0.24 & 0.40 & 0.60 & 0.60 \\ 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.52 & 0.52 & 0.72 & 0.52 & 1.00 & 0.32 & 0.24 & 0.56 & 0.88 & 0.24 & 0.24 \\ 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.12 & 0.20 & 0.12 & 0.08 & 0.32 & 1.00 & 0.72 & 0.40 & 0.48 & 0.80 & 0.80 \\ 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.24 & 0.12 & 0.24 & 0.32 & 0.24 & 0.72 & 1.00 & 0.40 & 0.32 & 0.80 & 0.68 \\ 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.32 & 0.24 & 0.52 & 0.24 & 0.56 & 0.40 & 0.40 & 1.00 & 0.80 & 0.68 & 0.68 \\ 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.40 & 0.32 & 0.60 & 0.40 & 0.88 & 0.48 & 0.32 & 0.80 & 1.00 & 0.52 & 0.52 \\ 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.32 & 0.20 & 0.52 & 0.60 & 0.24 & 0.80 & 0.80 & 0.68 & 0.52 & 1.00 & 1.00 \end{bmatrix}$$

Through the λ intercept array analysis, dynamic clustering diagram shown in figure 3:

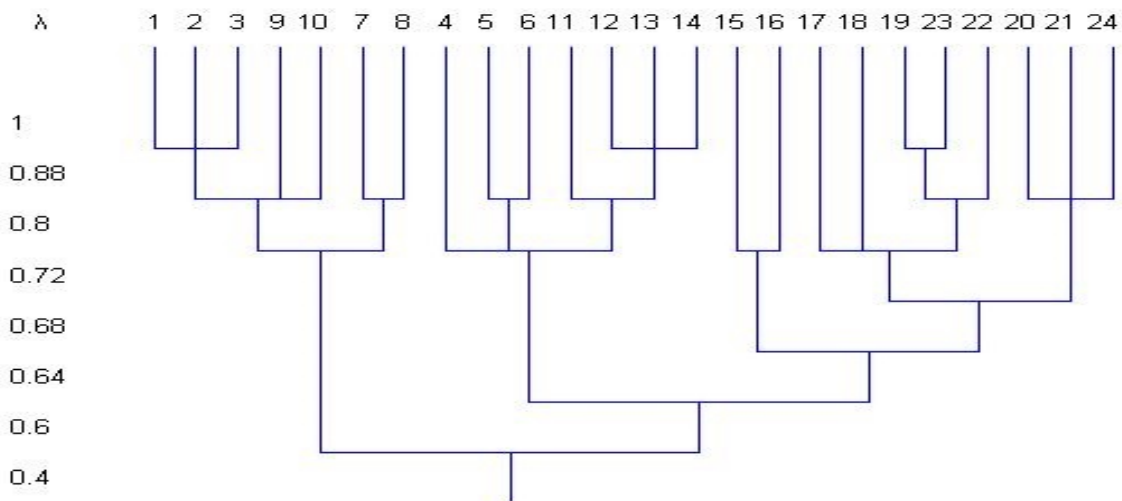


Fig. 3 Dynamic clustering map of CVT module

As can be seen from Figure 3, when $\lambda > 0.72$ the module classification too more, the appropriate λ is 0.68 or 0.64, since the output arm 15 and clutch 16 acts on the output portion of the transmission, into the output of the module. So, take $\lambda = 0.64$. The continuously variable transmission is divided into three modules, input part of the module, ratio adjustment section module, the output of the module, broadly consistent with the actual situation.

Conclusion

Transmission is an important mechanical equipment widely used in various industries, Based on fuzzy clustering analysis, the paper studies the creation and division of the transmission module. The function of the transmission parts and the correlation matrix of the function of the transmission parts are constructed respectively, and the corresponding fuzzy equivalent matrix is obtained. Threshold $\lambda=0.64$ intercept fuzzy equivalence matrix, the transmission is divided into 3 modules: input module, speed regulation module and output module. Through the division of the module, the design of the transmission is improved, which lays the foundation for the different needs of the market.

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