Study on Effects of CSI 300 Stock Index Futures on Chinese Stock Market Volatility

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Keywords: CSI 300 Stock Index Futures, Volatility, GARCH model, TARCH model

Abstract. At present, there is a growing concern on the effects of CSI 300 stock index futures on Chinese stock market volatility. This paper mainly studies the effects of introduction and price volatility of stock index futures on Chinese stock market volatility, which is based on the analysis of CSI 300 index. Based on the TARCH model, we find that the introduction of CSI 300 stock index futures reduce the asymmetric volatility of the stock market. Based on the GARCH model, we find that the price volatility of CSI 300 stock index futures have no significant effect on the volatility of the stock market.

Introduction

After a long period of preparations, the CSI 300 stock index futures has officially launched on April 16, 2010.

There is a growing concern on the effects of CSI 300 stock index futures on Chinese Stock Market Volatility. However, the present study has not yet come to a unified conclusion. The first opinion is that the introduction has no significant effect on the volatility of the stock market. Pericli and Koutmos (1997) use EGARCH and EGARCH-M model and find that the introduction of stock index futures has no significant effect on the conditional volatility and unconditional volatility of the stock market, based on the analysis of the S&P 500 index. Baldauf and Santoni (1991) use the data from 1975 to 1989 of the Chicago Futures Market and New York Stock Exchange and conclusion is that the introduction of the S&P 500 index has no significant effect on the volatility of the stock market, despite that it speeds up the reaction of supply-demand relationship of the stock market. The second opinion is that the introduction increases the volatility of the stock market. Antoniou and Holmes (1995) have a research on the FR-SE100 index and find that stock index futures increase the volatility of the stock market, but it also improves the response speed and quality of the spot market information. Robbai and Bhuyan (2005) conclude that the introduction of stock index futures has attracted many ignorant irrational investors, which increases the volatility of the stock market. The third opinion is that the introduction decreases the volatility of the stock market. Bessembinder and Seguin (1996) find that the introduction of futures market decreases the volatility of the spot market, based on the analysis on the S&P 500 index. S.L. Zhou and L. Gui (2011) study on the asymmetric effect of stock index futures on the volatility of the stock market, and find that the introduction of stock index futures decreases the asymmetric volatility of the Chinese stock market.

Based on the analysis of CSI 300 index, this paper uses TARCH model and GARCH model to study the effects of introduction and price volatility of stock index futures on stock market volatility.

Data description and stability test

Since the constituent stocks of CSI 300 index contain both Shanghai Stock Exchange and Shenzhen Stock Exchange and have 10 different industries, we can say that CSI 300 index is a barometer of the overall trend of Chinese stock market. Therefore, this paper uses CSI 300 index to represent the overall trend of the stock market and its closing price is denoted as $P_{\rm e}$. In order to analyze the impact of stock index futures on the stock market volatility, this paper selects two sets of data to analyze. The first group is used to analyze the effect of the introduction of stock index futures: select day data of 1702 days before and after the introduction of stock index futures, which is from January 2, 2008 to

December 31, 2014. Moreover, we include a dummy variable D_t to distinguish between before and after the introduction of stock index futures. The second group is used to analyze the effect of the price volatility of stock index futures: select day data of 1143 days which is from March 19, 2010 to December 31, 2014 and also includes a dummy variable D_t . Let r be the logarithmic return rate of the CSI 300 index, and the calculation formula is as follows:

$$r = \ln P_t - \ln P_{t-1} \tag{1}$$

Then, we do the ADF unit root test for the logarithmic return series and the results show that t values are -40.46 and -33.82, P values are both 0.0000, less than 1% significant level. Thus, the the logarithmic return series do not have unit root effect. Namely, the time series are stationary.

The establishment of GARCH models

The logarithmic return series have a typical financial time series characteristics of leptokurtic and fat tailed, so we can consider building GARCH model for it. First, we do the autocorrelation analysis of the logarithmic return series and find that the P values of all lag orders are greater than 5%. Thus, there is no significant autocorrelation at level 5%.

Therefore, we can establish random walk model and the mean equation is as follows:

$$\ln P_t = \alpha_0 \ln P_{t-1} + \varepsilon_t \tag{2}$$

The effect of the introduction of CSI 300 stock index futures

Due to the asymmetric volatility of stock return series, that is the volatility of stock return series when the stock price decline is greater than the volatility when the stock price increase. Thus, we use TARCH model to describe this phenomenon. The equation is as follows:

$$\sigma_{t}^{2} = \omega + \sum_{i=1}^{p} \alpha_{i} \varepsilon_{t-i}^{2} + \sum_{j=1}^{q} \beta_{j} \sigma_{t-j}^{2} + \sum_{k=1}^{r} \gamma_{k} \varepsilon_{t-k}^{2} I_{t-k}$$
(3)

In the above equation, σ_t^2 is conditional variance, ω is constant term and ε_t is random error term. In order to guarantee $\sigma_t^2 > 0$, α_t , β_f , γ_k must be non-negative. $\sum_{k=1}^r \gamma^k \varepsilon_{t-k}^2 \ I_{t-k}$ reflects leverage effect, which represents the effect of good news and bad news of preceding k periods to the conditional variance. The good news has only $\sum_{i=1}^p \alpha_i$ times impact, but the bad news has ($\sum_{i=1}^p \alpha_i + \sum_{k=1}^r \gamma_k$) times impact. I_{t-k} is dummy variable, $I_{t-k} = 1$ when $\varepsilon_{t-k} < 0$, and $I_{t-k} = 0$ when $\varepsilon_{t-k} > 0$. If γ_k is significantly not equal to 0, then it represents that there is leverage effect. Moreover, we include a dummy variable D_t to distinguish between before and after the introduction of stock index futures. Variance equation plus dummy variables D_t can be expressed as follows:

$$\sigma_{t}^{2} = \omega + \sum_{i=1}^{p} \alpha_{i} \varepsilon_{t-i}^{2} + \sum_{j=1}^{q} \beta_{j} \sigma_{t-j}^{2} + \sum_{k=1}^{r} \gamma_{k} \varepsilon_{t-k}^{2} I_{t-k} + \theta D_{t}$$
(4)

$$D_t = \begin{cases} 1, & \text{before the introduction} \\ 0, & \text{after the introduction} \end{cases}$$

The effect of the price volatility of CSI 300 stock index futures

This part we use GARCH model and the reasons are explained in empirical analysis. A specific GARCH(p, q) model is expressed as follows:

$$\ln P_t = \alpha_0 \ln P_{t-1} + \varepsilon_t$$

$$\sigma_t^2 = \beta_0 + \sum_{i=1}^q \beta_i \varepsilon_{t-i}^2 + \sum_{i=1}^p \gamma_i \sigma_{t-i}^2$$

$$\tag{5}$$

In the above equations, $\mathbf{z}_{\mathbf{z}}$ is random error term. $\boldsymbol{\beta}_{\mathbf{z}}$ as the coefficient of lag residuals is an information coefficient, representing the importance of the recent market news, used to measure the impact of the previous period volatility information to spot volatility. $\boldsymbol{\gamma}_{\mathbf{j}}$ is the coefficients of the conditional hetero variance of the lag period, used to measure the cumulative impact of previous period volatility. Then, we include a dummy variable $\boldsymbol{D}_{\mathbf{z}}$ to represent the price volatility of CSI 300 stock index futures. GARCH(p, q) model plus dummy variables $\boldsymbol{D}_{\mathbf{z}}$ can be expressed as follows:

$$\ln P_t = \alpha_0 \ln P_{t-1} + \varepsilon_t$$

$$\sigma_{t}^{2} = \beta_{0} + \sum_{i=1}^{q} \beta_{i} \varepsilon_{t-i}^{2} + \sum_{j=1}^{p} \gamma_{j} \sigma_{t-j}^{2} + \theta D_{t}$$
 (6)

 $D_t = \begin{cases} 1, & \text{when the price of stock index futures increases} \\ 0, & \text{when the price of stock index futures decreases} \end{cases}$

Empirical analysis based on the CSI 300 Index

The effect of the introduction of CSI 300 stock index futures

First, we use least square method to model the mean equation of GARCH model and the result is as follows:

$$\ln P_t = 1.00 \ln P_{t-1} + \hat{\varepsilon_t} \tag{7}$$

The t value of independent variable coefficient is 17910.41, p value is 0.0000, the fitting coefficient $R^2 = 0.9918$, log likelihood value is 4403.10, AIC=-5.17,SC=-5.17. Thus, the coefficient of this equation is significantly positive, and R^2 is quite high. The residual plot is as follows:

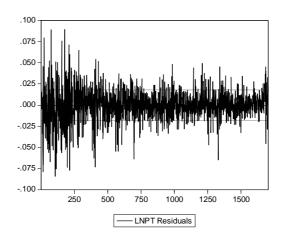


Fig.1 The residual plot of equation

It can be seen from the figure that the residuals of equation show obvious fluctuation aggregation, which indicates that the residual series may have conditional heteroskedasticity. Then, we do ARCH LM test for the equation, and the result when the lag order is 1 is that P value is 0.0000, which indicates that we should reject the original hypothesis at 5% level of significance, and the residual series may have conditional heteroskedasticity. Therefore, TARCH(1, 1) model is as follows:

$$\sigma_t^2 = \omega + \alpha \varepsilon_{t-1}^2 + \gamma \varepsilon_{t-1}^2 I_{t-1} + \beta \sigma_{t-1}^2 + \theta D_t$$
 (8)

The estimation results of TARCH(1, 1) model are shown in the following table:

Table 1 The estimation results of 17 meet (1, 1) model						
	variable	coefficient	Z value	P value		
Mean equation	$\ln P_{\varepsilon-1}$	1.00	21847.53	0.0000		
Variance equation	ω	5.44E-06	4.35	0.0000		
	ε_{t-1}^2	0.0375	4.78	0.0000		
	$\varepsilon_{t-1}^2 I_{t-1}$	0.0364	3.70	0.0002		
	σ_{t-1}^2	0.9185	89.53	0.0000		
	D_{ϵ}	8.02E-06	3.42	0.0006		

Table 1 The estimation results of TARCH(1, 1) model

It can be seen in the above table that the fitting coefficient $\mathbb{R}^2 = 0.9918$, all the coefficients are significant, log likelihood value is 4609.55, AIC=-5.41, SC=-5.39. Thus, the log likelihood value increases and the value of AIC and SC decrease, which indicates that TARCH(1, 1) model fits the data better. Moreover, the leverage effect coefficient γ is significantly positive at 1% level of significant, which indicates that the leverage effect is obvious, and the bad news results in greater volatility compared to good news. The coefficient β presents the impact of the last period on the current period. In the above table we can see that β is 0.9207, thus the volatility of the last period is the main factor that affects the current volatility. The coefficient of dummy variable is significantly positive at 1% level of significant, which indicates that the volatility decreases after the introduction of stock index futures.

At last, we do ARCH LM test for the TARCH(1, 1) model, and the result when the lag order is 1 is that P value is bigger than 5%, which indicates that we cannot reject the original hypothesis at 5% level of significance, and the residual series do not have ARCH effect. Therefore, TARCH(1, 1) model is better to simulate the volatility of the stock market.

The effect of the price volatility of CSI 300 stock index futures

First, we use least square method to model the mean equation of GARCH model and the result is as follows:

$$\ln P_t = 1.00 \ln P_{t-1} + \mathcal{E}_t \tag{9}$$

The t value of independent variable coefficient is 19379.17, p value is 0.0000, the fitting coefficient $R^2 = 0.9891$, log likelihood value is 3281.59, AIC=-5.74, SC=-5.74. Thus, the coefficient of this equation is significantly positive, and R^2 is quite high. The residual plot is as follows:

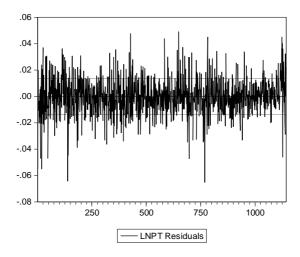


Fig.2 The residual plot of equation

It can be seen from the figure that the residuals of equation show obvious fluctuation aggregation, which indicates that the residual series may have conditional heteroskedasticity. Then, we do ARCH LM test for the equation, and the result when the lag order is 2 is that P value is 0.0003, which indicates that we should reject the original hypothesis at 5% level of significance, and the residual series may have conditional heteroskedasticity. Therefore, TARCH(1, 2) model is as follows:

$$\sigma_t^2 = \omega + \alpha_1 \varepsilon_{t-1}^2 + \alpha_2 \varepsilon_{t-2}^2 + \gamma \varepsilon_{t-1}^2 I_{t-1} + \beta \sigma_{t-1}^2 + \theta D_t$$
 (10)

The estimation results of TARCH(1, 2) model are shown in the following table:

	variable	coefficient	Z value	P value
Mean equation	$\ln P_{t-1}$	1.00	19954.80	0.0000
Variance equation	ω	5.37E-06	1.654346	0.0981
	s_{t-1}^2	-0.017947	-1.058115	0.2900
	$\varepsilon_{t-1}^2 I_{t-1}$	-0.007283	-0.584736	0.5587
	ε_{t-2}^2	0.064241	3.673237	0.0002
	σ_{t-1}^2	0.928252	70.98412	0.0000
	D_{ε}	-2.27E-07	-0.040370	0.9678

Table 2 The estimation results of TARCH(1, 2) model

It can be seen in the above table that the fitting coefficient $\mathbb{R}^2 = 0.9891$, the leverage effect coefficient γ is not significantly positive at 5% level of significant, which indicates that the leverage effect decreases after the introduction of stock index futures. Therefore, we change to use GARCH model to analyze the effect. Using GARCH(1, 1), GARCH(1, 2), GARCH(2, 1), GARCH(2, 2)

models to fit data and we finally choose GARCH(1, 1) model based on the AIC and SC standards. The GARCH(1, 1) model is as follows:

$$\ln P_t = \alpha_0 \ln P_{t-1} + \varepsilon_t$$

$$\sigma_t^2 = \beta_0 + \beta \varepsilon_{t-1}^2 + \gamma \sigma_{t-1}^2 + \theta D_t \tag{11}$$

The estimation results of GARCH(1, 1) model are shown in the following table:

Tuble 5 The estimation results of Graveria, 1) model						
	variable	coefficient	Z value	P value		
Mean equation	$\ln P_{\varepsilon-1}$	1.00	20359.42	0.0000		
Variance equation	$oldsymbol{eta}_0$	3.57E-06	1.52	0.1297		
	ε_{t-1}^2	0.0350	4.58	0.0000		
	σ_{z-1}^2	0.9390	81.18	0.0000		
	D_{\star}	2.29E-06	0.5626	0.5737		

Table 3 The estimation results of GARCH(1, 1) model

It can be seen in the above table that the fitting coefficient $\mathbb{R}^2 = 0.9891$, all the coefficients are significant, log likelihood value is 3309.05, AIC=-5.78, SC=-5.76. Thus, the log likelihood value increases and the value of AIC and SC decrease, which indicates that GARCH(1, 1) model fits the data better. The coefficient of dummy variable is not significantly positive at 5% level of significant, which indicates that the price volatility of stock index futures has no significant impact on the volatility of stock market.

At last, we do ARCH LM test for the GARCH(1, 1) model, and the result when the lag order is 1 is that P value is bigger than 5%, which indicates that we cannot reject the original hypothesis at 5% level of significance, and the residual series do not have ARCH effect. Therefore, GARCH(1, 1) model is better to simulate the volatility of the stock market.

Conclusions

The introduction of CSI 300 index futures shows that Chinese financial derivatives market has begun to take shape, and it also plays an important role in promoting Chinese gradual opening up of financial markets. This paper mainly studies the effects of introduction and price volatility of stock index futures on Chinese stock market volatility, which is based on the analysis of CSI 300 index. Based on the TARCH model, we can find that the introduction of CSI 300 stock index futures reduce the asymmetric volatility of the stock market. Based on the GARCH model, we can find that the price volatility of CSI 300 stock index futures have no significant effect on the volatility of the stock market. This may be due to CSI 300 stock index futures exists for such a short time that the stock index futures market is not mature and the function of hedging is relatively small. Therefore, we can only say that the price volatility of stock index futures has no significant impact on Chinese stock market volatility in the short term.

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