Simulation analysis of helical gears in the gear box of the rolling mill

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Abstract. This paper studies the helical gears in the gear box of cold rolling mill in a steel, using software SolidWorks to make one pair of meshing helical gears a solid model, and import the entity model into ADAMS to creat a virtual prototype model, using IMPACT function to define the contact between gears, based on Hertz elastic collision theory, determine the parameters in the IMPACT function. By loading simulation, The speed characteristic curve of the drive shaft and the gear meshing force curve simulation are obtained, compared with theoretical analysis, the correctness of the simulation is verified.

1. Introduction

With the development of rolling technology, The mill has become more automatic and continuous. The rolling speed of high speed wire rolling mill can be achieved hundreds of meters per second, and bear the load changing. The gear box is an important transmission system, if there is a fault, it will cause an enormous economic loss^[1]. With the aid of software ADAMS, in the stage of product design, can carry out a complete analysis of the whole system, to obtain the optimal design; In the engineering application stage, aiming at the practical problems arising in the work, can find out the root problem ^[2]. The virtual prototype of a gearbox in meshing helical gear based on ADAMS, through dynamic simulation analysis, research the gear rotational speed, meshing force and meshing frequency, provide the basis for fault analysis and optimum design of the gear box.

2. To establish the virtual prototype model of helical gear

According to table 1,design a three-dimensional modeling by using SolidWorks.

Table 1 model of helical gear parameters							
Gear	The number of teeth	Modulus m/mm	Pressure angle/(°)	Width b/mm	Addendum coefficient	Coefficient of top clearance	Spiral angle/(°)
Big gear	41	25	20	350	1	0.25	14(Left)
Small gear	30	25	20	350	1	0.25	14(Right)

The helical gear has been established and import ADAMS to establish the virtual prototype model, edit attributes for each component, set the elastic modulus of each gear and shaft for $E=2.10\times10^{5}$ Mp, Poisson's ratio is v=0.29, the density is $\rho=7.8\times10^{-9}$ t/mm³. Add rotation pair on the shaft, add a fixed vice between the gear and shaft, add contact between the gear and the gear, add speed drive on the input shaft, add load torque in the output shaft. The virtual prototype model as shown in figure 1.



Figure.1 The virtual prototype model of helical gear pair **2.1 The selection of virtual prototype model of parameter**

In order to make the simulation analysis more close to actual work condition, do not use

idealized geometric constraint definition of helical gear meshing, but the choice of contact force based on constraint relationship. The contact force between the gear by using Impact function method to calculate, the Impact function can be expressed by the following:

$$F = \begin{cases} 0 & q \ge q_0 \\ K(q_0 - q)^e - C \cdot \frac{d_q}{d_t} \cdot step(q, q_0 - d, 1, q_0, 0) & q < q_0 \end{cases}$$
(1)

the step is a step function, the q_0 is the two movement of objects before the distance, the q is the two object contact the actual distance in the process of collision, the $(q_0 - q)$ is in contact with the actual deformation in the collision process, when $q \ge q_0$, the two objects do not contact or just contact, the contact force at this time is 0; When $q < q_0$, in the formation of contact force between two objects, contact force and Contact stiffness coefficient K, deflection $(q_0 - q)$, the collision force index e and damping coefficient C have relations^[3].

The contact stiffness coefficient K depends on the material and structure in the shape of an object, by the Hertz contact theory ^[4], an object of the contact stiffness by two contact equivalent cylinder to describe, The helical gear contact stiffness coefficient calculation formula is^[5]:

$$\begin{cases}
K = \frac{4}{3}R^{\frac{1}{2}}E^{*} \\
R = \frac{id_{1}\cos\alpha_{t}\tan\alpha_{t}}{2(1+i)\cos\beta_{b}} \\
\beta_{b} = \arctan(\tan\beta\cos\alpha_{t}) \\
\frac{1}{E^{*}} = \frac{1-v_{1}^{2}}{E_{1}} + \frac{1-v_{2}^{2}}{E_{2}}
\end{cases}$$
(2)

i is transmission ratio, d_1 is pitch diameter of the driving wheel, α_t is transverse pressure angle, α_t is end face engagement angle, β_b is base helix angle, β is helix angle, *E* is Modulus of elasticity, v is Poisson ratio. The stiffness coefficient is K=1.35×10⁶ calculated by the calculation. According to the empirical data, the calculation speed and convergence, after simulation experiment, the collision force index is e=2.2, damping coefficient is C=50Ns/mm, penetration depth is d=0.1mm.

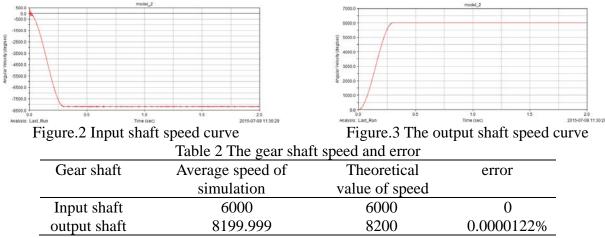
The gears in the meshing process of rotation, to consider the friction between teeth, the working environment of the gear pair after lubrication, according to mechanical design manual and related simulation experience, the static friction coefficient of the gear is 0.08, the dynamic friction coefficient is 0.05, the static slip velocity is 0.1mm/s, the dynamic slip velocity is 10mm/s.

3. Simulation and analysis of the results

Based on virtual prototype model, applying a constant speed drive on the input shaft 6000° /s, in order to make no mutations exert speed, then use the STEP function (time step function) so that the rotating speed reaches the maximum value in 0.3s, STEP(time,0,0d,0.3,6000d), where time is the time variable, select the type of loading velocity, add the load torque output shaft 260KN·m, with the direction of the input shaft in the same direction. The simulation time is set to 2s, the number of steps is20000, use Wstiff and SI2 integration scheme can get better simulation results.

3.1 Simulation analysis of gear shaft speed

Figures 2 and 3 respectively for the input shaft and the output shaft speed curve,.In the model of virtual prototype, specified clockwise forward direction, from Figure 3 and Figure 4 can be seen, the direction of rotation of the input shaft is positive, the direction of rotation of the output shaft is negative, the direction of rotation of the gear shaft meet external gear transmission direction relation. In 0~0.3s, the input shaft and the output shaft in a slow acceleration state, the speed curve is relatively small fluctuations, to avoid severe shock and vibration, in 0.3~2s, the gear in a stable state of motion, the input shaft and the output shaft speed fluctuation in a mean near, it can be seen from table 2, the simulation speed of input shaft and the output shaft of the average value are close to the theoretical value of speed, speed error can be ignored.



3.2 Analysis of gear meshing force

The gear tooth surface meshing force calculation formula is:

$$F_n = \frac{2T}{d \cdot \cos \alpha_n \cdot \cos \beta} \tag{3}$$

T is orque,*d* is gear pitch circle diameter, α_n is the gear normal pressure angle,*B* is helix angle.To get data transmission theory of helical gear meshing force is 7.89×10^5 N.

The gear rotation frequency formula such as 4 formula, *n* is gear shaft speed (r/min),

$$f_r = \frac{n}{60} \tag{4}$$

The gear meshing frequency formula such as 5 formula, z is number of gear teeth.

 $f_z = f_r z$ (5) Into the data can be calculated, the driving wheel rotation frequency is $f_{r1} = 16.67$ Hz, the follower

wheel rotation frequency is $f_{r2}=22.78$ Hz, the gear meshing frequency is $f_z=683.47$ Hz.

Through ADAMS simulation, helical gear meshing contact force in time domain is shown in Figure 4. We can see from Figure 6, in the stage of accelerated 0~0.3s, in the beginning of the *moment* to start, the impact of gear vibration, the meshing force is relatively large, in the constant speed stage in 0.3~2s, the running gear is relatively stable, the meshing force of gear under the periodic fluctuations in the mean, the simulation results of the meshing force of the average value is 7.69×10^5 N, the error is compared with the theoretical value is 2.53%, the errors were acceptable.

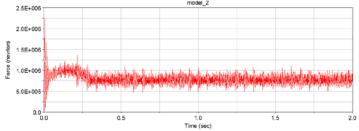


Figure.4 Helical gear transmission meshing force time domain graph

By Fast Fourier Transformation, get the helical gear meshing force frequency is shown in Figure 5, the maximum amplitude frequency at 683.357Hz, the theory of gear meshing frequency is 683.47Hz, the meshing force fluctuation frequency and gear meshing frequency almost equal, at the same time with multi frequency, reflects the periodicity of tooth mesh in and out of the meshing process.We can see from figure 6, there are equal interval frequency, the frequency interval is 16.48Hz and 22.89Hz, close to the active rotation frequency and the follower wheel rotation frequency, reflects the cyclical fluctuation of tooth contact force.

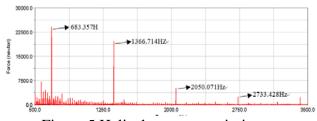
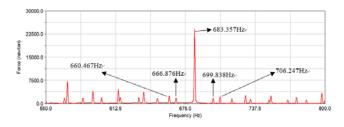


Figure.5 Helical gear transmission Figure.6 Helical gear transmission meshing meshing frequency diagram



local amplification frequency chart

4. Summary

The dynamic simulation of the helical gear is carried out by using ADAMS, the gear speed and meshing force were obtained with the theoretical value, the correctness of the established model is verified, it is revealed that the periodicity of the contact force fluctuation during the meshing process of the helical gears, provide the basis for the optimization design of the gear box.

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