# Accurate Fault Location for Double-Circuit Lines on the Same Tower with Asymmetrical Parameters 

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#### Abstract

Traditional six-sequence components can only be applied to the double-circuit lines with symmetrical parameters. In reality, there may appear partially coupled lines with asymmetrical parameter because of the difference in construction. A new decoupling method is adopted to solve this problem. Three phases are first decoupled to positive , negative and zero sequence component , but there are mutual inductance between zero sequence component. Then the zero sequence is divided into the same direction component and the reverse component. The method solves the problem of zero sequence mutual inductance of double circuit lines on the same tower with asymmetric parameters. The current and voltage of both ends of the transmission line can be decoupled into the new six sequence component by new six-sequence component method. The fault location formula can be obtained based on that the sequence voltage of fault point calculated by both ends are equivalent. PSCAD simulation results show that the method can accurately measure the distance of fault and is not affected by fault type, fault location , fault resistance and other factors.


## Introduction

Now the land resource is in short supply, the cost of setting up the transmission line is getting higher and higher, and the transmission capacity is increasing day by day. The double circuit lines on the same tower can improve the transmission capacity of the transmission corridor, so it has been widely used. When a fault occurs in power system, accurate fault location can quickly locate the fault position and the fault can be removed in time. It can save a lot of manpower and material resources, and reduce the economic losses due to power failure. Fault location of double circuit lines is difficult because of more fault types and interaction between lines. Most of ranging methods have been proposed for double circuit lines on the same tower are based on the condition of symmetric parameter. If the line parameters are asymmetrical, the coupling relationships will be more complex, and more fault types will exist. It is necessary to study a measurement method of double circuit transmission lines with asymmetric parameters.

At present, the fault location is mainly divided into single-ended method[1,2] and double-ended method[3,4]. Single-ended method just uses data of one end of the line, the realization is simple, but it is influenced by the transition resistance. Double-ended method is not affected by fault types and system impedance, the distance measurement is more accurate, but data synchronization of two ends is needed. According to characteristics of double circuit lines on the same tower based on distributed parameter model using asymmetrical parameter, the paper[5] proposes a new fault locating algorithm for double circuit lines on the same tower using asynchronous data of two terminals. The paper [6] proposes a new algorithm to solve simple faults of the double circuit lines on the same tower, and the symmetry of the power system parameters is not required.

Because the coupling of the double circuit lines is complicated, the six sequence[7,8] component method is used to decouple. The paper[9] proposes a decoupling method based on six sequence components, then uses asynchronous data of two terminals for fault location. But the six sequence component method is generally applied to the double circuit lines with symmetrical parameters. It is no longer suitable for the double circuit lines with asymmetrical parameters. The paper[10] proposes
a new sequence component method applied to double circuit lines on the same tower with asymmetrical parameters. In order to fully decouple the impedance matrix with asymmetrical parameters, the zero sequence four component method is proposed in paper [11].

The current and voltage of both ends of the transmission line can be decoupled into the new six sequence components by new decoupling method in this paper. The fault location formula can be established based on that the sequence voltage of fault point calculated by both ends are equivalent . Accurate fault distance can be obtained with the formula. The effectiveness of the proposed method is verified by PSCAD simulation.

## Characteristics of Double Circuit Lines with Asymmetrical Parameters

The model diagram of the double circuit transmission line is shown in Fig.1.The two circuit lines are coupled with each other. Where $E_{m}, ~ E_{n}$ is respectively power supply voltage of two ends of transmission line.is the impedance of line

I is the impedance of line II.


Fig. 1 System structure diagram
Fig. 2 shows the parameters of MN part of the line. The parameters of the two circuit lines are different, but the parameters of the circuit are symmetrical. Where $Z_{l 1}$ is the self inductance of line $\mathrm{I}, Z_{m 1}$ is the mutual inductance of line $\mathrm{I}, Z_{12}$ is the self inductance of line II, $Z_{m 2}$ is the mutual inductance of line II, $Z_{p}$ is the self inductance of two lines.


Fig. 2 Line parameter
From Fig.2, the relationship between voltage and current of the double circuit line is:

$$
\left[\begin{array}{c}
\Delta U_{\mathrm{IA}}  \tag{1}\\
\Delta U_{\mathrm{IB}} \\
\Delta U_{\mathrm{IC}} \\
\Delta U_{\mathrm{IIA}} \\
\Delta U_{\mathrm{IB}} \\
\Delta U_{\mathrm{IIC}}
\end{array}\right]=\left[\begin{array}{llllll}
Z_{l 1} & Z_{m 1} & Z_{m 1} & Z_{p} & Z_{p} & Z_{p} \\
Z_{m 1} & Z_{l 1} & Z_{m 1} & Z_{p} & Z_{p} & Z_{p} \\
Z_{m 1} & Z_{m 1} & Z_{\mathrm{ll}} & Z_{p} & Z_{p} & Z_{p} \\
Z_{p} & Z_{p} & Z_{p} & Z_{\mathrm{l2}} & Z_{m 2} & Z_{m 2} \\
Z_{p} & Z_{p} & Z_{p} & Z_{\mathrm{L2}} & Z_{\mathrm{ll}} & Z_{m 2} \\
Z_{p} & Z_{p} & Z_{m 2} & Z_{m 2} & Z_{\mathrm{l2}}
\end{array}\right]\left[\begin{array}{l}
I_{\mathrm{IA}} \\
I_{\mathrm{IB}} \\
I_{\mathrm{IC}} \\
I_{\mathrm{IIA}} \\
I_{\mathrm{IIC}}
\end{array}\right]
$$

Where $\Delta U_{\mathrm{IA}}, ~ \Delta U_{\mathrm{IB}}, ~ \Delta U_{\mathrm{IC}}, ~ \Delta U_{\mathrm{II} A}, ~ \Delta U_{\mathrm{IIB}}, ~ \Delta U_{\mathrm{IIC}}$ is voltage drop of the line, $\Delta U_{\mathrm{IA}}, ~ \Delta U_{\mathrm{IB}}$, $\Delta U_{\text {IC }}, ~ \Delta U_{\text {IIA }}, ~ \Delta U_{\text {IIB }}, ~ \Delta U_{\text {IIC }}$ is circuit of the line.

The impedance matrix is marked as Z , above formula can be simplified as $\Delta U_{A B C}=Z * I_{A B C}$.
Where $\Delta U_{A B C}$ is voltage drop of the line, $I_{A B C}$ is circuit of the line.

## The Decoupling Method of Line

Traditional Six-Sequence Components Method. The characteristics of double circuit transmission lines on the same tower are two lines coupling with each other. That means each phase owns self inductance and mutual inductance between each other. There are also mutual inductance between lines. The six sequence component method is applied to the double circuit lines with symmetrical parameters. The self inductance and mutual inductance of the line are equivalent. The essence of the six sequence component method is to eliminate the mutual inductance between lines. First realize the decoupling between the lines, the voltage and current of the double lines is divided into the same direction vector T and reverse direction vector F .

Then realize the decoupling between the phases. The same direction vector and reverse direction vector can be divided into the same direction positive sequence, the same direction negative sequence, the same direction zero sequence, reverse direction positive sequence, reverse direction negative sequence and reverse direction zero sequence. These six components are independent of each other.

Decoupling Method Of Double Circuit Lines With Asymmetrical Parameters. Due to the asymmetry of the double circuit lines parameters, lines can not be decoupled first as six sequence component method. The decoupling between the phases can be realized first with the method proposed by paper[9].The double circuit lines are divided into positive sequence, negative sequence and zero sequence component with matrix $Q$.

$$
Q=\left[\begin{array}{cccccc}
1 & 1 & 1 & & & \\
1 & a^{2} & a & & & \\
1 & a & a^{2} & & & \\
& & & 1 & 1 & 1 \\
& & & 1 & a^{2} & a \\
& & & 1 & a & a^{2}
\end{array}\right]
$$

The formula (1) can be expanded as follows:

Where zero sequence impedance of I is $Z_{10}=Z_{l 1}+2 Z_{m 1}$, zero sequence impedance of II is $Z_{\text {II } 0}=Z_{l 2}+2 Z_{m 2}$, positive and negative sequence impedance of I is $Z_{\mathrm{I} 1}=Z_{\mathrm{I} 2}=Z_{l 1}-Z_{m 1}$, positive and negative sequence impedance of II is $Z_{\mathrm{II1}}=Z_{\mathrm{II} 2}=Z_{12}-Z_{m 2}$.

Formula(2)shows positive and negative sequence components are independent of each other, but there are mutual inductance between zero sequence components. Zero sequence components need to be decoupled. The impedance matrix needs diagonalization processing. And that processing, the corresponding characteristic value is the impedance value on the diagonal. Corresponding feature vectors can be composed of a decoupled matrix $M$. The zero sequence component is decoupled by $M$.

$$
M=\left[\begin{array}{cccccc}
1 & & & 1 & & \\
& 1 & & & & \\
& & 1 & & & \\
k_{1} & & & k_{2} & & \\
& & & & 1 & \\
& & & & & 1
\end{array}\right]
$$

$$
\begin{align*}
& k_{1}=\frac{Z_{\text {II0 }}-Z_{\text {I0 }}+\sqrt{\left(Z_{\text {II } 0}-Z_{10}\right)^{2}+36 * Z_{p}^{2}}}{6 Z_{p}}  \tag{3}\\
& k_{2}=\frac{Z_{\text {II0 }}-Z_{\text {I0 }}-\sqrt{\left(Z_{\text {II0 }}-Z_{10}\right)^{2}+36 * Z_{p}^{2}}}{6 Z_{p}} \tag{4}
\end{align*}
$$

The formula (2)can be expanded as follows:

$$
\left[\begin{array}{c}
\Delta U_{01}  \tag{5}\\
\Delta U_{11} \\
\Delta U_{12} \\
\Delta U_{02} \\
\Delta U_{11} \\
\Delta U_{112}
\end{array}\right]=\left[\begin{array}{llllll}
Z_{01} & & & & & \\
& Z_{11} & & & & \\
& & Z_{12} & & & \\
& & & Z_{02} & & \\
& & & & Z_{11} & \\
& & & & & Z_{12} 2
\end{array}\right]\left[\begin{array}{c}
I_{01} \\
I_{11} \\
I_{12} \\
I_{22} \\
I_{112} \\
I_{12}
\end{array}\right]
$$

Where $\Delta U_{01}, ~ \Delta U_{02}$ is the first and second zero sequence component of voltage after decoupling, $I_{01}, ~ I_{02}$ is the first and second zero sequence component of current after decoupling, $Z_{01}, ~ Z_{02}$ is the first and second zero sequence component of impedance after decoupling.

$$
\begin{align*}
& Z_{01}=\left(Z_{\text {II0 }}+Z_{\text {I0 }}+\sqrt{\left(Z_{\text {II } 0}-Z_{I 0}\right)^{2}+36 * Z_{p}^{2}}\right) / 2  \tag{6}\\
& Z_{02}=\left(Z_{\text {II0 }}+Z_{\text {I0 }}-\sqrt{\left(Z_{\text {II }}-Z_{\text {I0 }}\right)^{2}+36 * Z_{p}^{2}}\right) / 2 \tag{7}
\end{align*}
$$

The total decoupling matrix is:

$$
N=\mathrm{QM}=\left[\begin{array}{cccccc}
1 & 1 & 1 & 1 & & \\
1 & a^{2} & a & 1 & & \\
1 & a & a^{2} & 1 & & \\
k_{1} & & & k_{2} & 1 & 1 \\
k_{1} & & & k_{2} & a^{2} & a \\
k_{1} & & & k_{2} & a & a^{2}
\end{array}\right]
$$

01, 02, I 1, I 2, II 1 , II 2 the six independent sequence components can be got after decoupling by N.

Fault Location Principle Of Double Circuit Lines On The Same Tower.Fig. 3 shows fault location principle of double circuit lines on the same tower, considering the influence of distributed capacitance. Where $Z_{i}$ is sequence impedance of each line, $Y_{i}$ is sequence admittance of each line, $L$ is total length of line, D the distance from the M side bus to the fault point, $Z_{M S i}$ and $Z_{N S i}$ are system impedance, $R_{f}$ is transition resistance.


Fig. 3 Mutation sequence network of parallel lines
Voltage and current values are recorded before and after the failure of both sides of the bus, the fault value is equal to the subtraction of which. Six independent sequence components of voltage and current can be got after decoupling by matrix N . The fault location formula can be obtained based on that the sequence voltage of fault point calculated by both ends are equivalent.

$$
\begin{equation*}
\left|\Delta U_{M i}-\left(\Delta I_{M i}-\Delta U_{M i} \frac{D Y_{i}}{2}\right) D Z_{i}\right|=\left|\Delta U_{N i}-\left(\Delta I_{N i}-\Delta U_{N i} \frac{D Y_{i}}{2}\right)(L-D) Z_{i}\right| . \tag{8}
\end{equation*}
$$

Formula (8) shows that if the fault voltage and current of both ends of the line is fixed, $\left|U_{F M i}\right|$ decreases with the increase of $D$ and $\left|U_{F N i}\right|$ increases with the increase of $D$. So there will only be the only solution and there will be no pseudo root. In practical solution, a global one-dimensional search of $D$ can be carried out in the range of $0 \sim L$. Search step is $\Delta d . D$ is the correct fault distance when the difference value on both sides of formula (8) is minimal.

## The Simulation Verification

The simulation system diagram is shown in Figure 1. The length of double circuit line is 100 km . The system voltage of both sides of the line is 220 kv . Positive sequence impedance is $\mathrm{j} 90 \Omega$.The self inductance of line I is $Z_{l 1}=(25.76+\mathrm{j} 132.55) \Omega$, the mutual inductance of line I is $Z_{m 1}=(18.25+\mathrm{j} 47.86) \Omega$, the self inductance of line II is $Z_{l 2}=(22.56+\mathrm{j} 112.37) \Omega$, the mutual inductance of line II is $Z_{m 2}=(15.34+\mathrm{j} 40.33) \Omega$, the self inductance of two lines is $Z_{p}=(25.68+\mathrm{j} 142.93) \Omega$.

Fault Location of Different Fault Type. The length of the line is 100 km . Different types of faults occurred in 30 km and 50 km respectively. Fault location are carried out by using the negative sequence component of line I. The results of simulation and calculation are shown in table 1. From table 1,it can be known that the error of fault location based on the fault location method proposed in this paper is within $1 \%$.

Tab. 1 Fault location of different fault type

| Fault Type |  |  |  |
| :---: | :---: | :---: | :---: |
| Actual Fault |  |  |  |
| Distance[km] |  |  |  | | Fault |
| :---: | :---: | :---: |
| Location[km] |$\quad$ Error[\%]

Notes: I AG means A phase of line I to ground short circuit ;I BC means $A$ phase and $B$ phase of line I short circuit; I BCG means $B$ phase and $C$ phase of line I to ground short circuit; I B II CG means $B$ phase of line I and $C$ phase of line II to ground short circuit; I A II BCG means $A$ phase of line I, $B$ phase and $C$ phase of line II to ground short circuit.

Fault Location of Different Transition Resistance. The length of the line is 100 km . Different types of grounding faults occurred in 30 km with different transition resistance. Fault location are carried out by using the negative sequence component of line I. The results of simulation and calculation are shown in table 2. From table 2, it can be known that the method proposed in this paper is not affected by the transition resistance.

Fault Location of Different Sequence Component .The length of the line is 100 km . A variety of metal grounding fault occurs in 30km.Fault location are carried out by using different sequence components. The results of simulation and calculation are shown in table 3.From table 3, it can be known that the error of fault location with positive sequence is larger and the range accuracy of
negative sequence component and zero sequence component is relatively higher. Positive sequence component is widespread. When the negative sequence component is used for fault location , if the single circuit line fails, it is required to determine which circuit the fault occurred in . Zero sequence component is zero in the event of symmetrical faults and non ground faults. So in the actual situation, the negative sequence component and the zero sequence component after decoupling can be used for ranging.

| Tab.2 Fault location of different transition resistance |  |  |
| :---: | :---: | :---: |
| Fault Type | Fault Location[km] | Error[\%] |
|  | 30.17 | 0.17 |
| I AG | 30.18 | 0.18 |
|  | 30.22 | 0.22 |
|  | 29.87 | 0.13 |
| I BCG | 30.19 | 0.19 |
|  | 30.14 | 0.14 |
|  | 29.79 | 0.21 |
| I B II CG | 29.86 | 0.14 |
|  | 29.85 | 0.15 |
|  | 30.11 | 0.11 |
| I A II BCG | 30.18 | 0.18 |
|  | 29.86 | 0.14 |


| Tab.3 Fault location of different sequence component |  |  |  |
| :---: | :---: | :---: | :---: |
| Fault Type | Actual Fault <br> Distance[km] | Fault <br> Location[km] | Error[\%] |
| I AG | I 1 | 25.74 | 4.26 |
|  | I 2 | 30.13 | 0.13 |
|  | 01 | 30.16 | 0.16 |
|  | 02 | 29.88 | 0.12 |
|  | I 1 | 25.87 | 4.13 |
|  | I 2 | 30.16 | 0.16 |
|  | 01 | 30.17 | 0.17 |
|  | 02 | 29.89 | 0.11 |
|  | I 1 | 24.76 | 5.24 |
| I A II BCG | I 2 | 30.18 | 0.18 |
|  | 01 | 29.95 | 0.05 |
|  | 02 | 30.23 | 0.23 |
|  | I 1 | 25.11 | 4.99 |
|  | I 2 | 29.89 | 0.11 |
|  | 01 | 29.86 | 0.14 |
|  | 02 | 30.25 | 0.25 |

## Summary

In this paper, the characteristics of double circuit lines with asymmetrical parameters are analyzed. Two lines are divided into positive ,negative and zero sequence component by using the symmetrical component method. The positive negative sequence components are independent of each other, but there are mutual inductance between zero sequence component. The mutual inductance between the zero sequence can be eliminated by the new decoupling method and the zero sequence is divided into
the same direction component and the reverse direction component. The new six sequence components are mutually independent. The fault location formula can be obtained based on that the sequence voltage of fault point calculated by both ends are equivalent.

Fault location method proposed in this paper not only has the advantages of the existing two terminal fault location method, but also not be effected by fault location, fault type and transition resistance. It owns high precision and can be applied to fault location of partly coupling double circuit lines and multiple circuit lines ,which has important practical significance.

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