Hybrid Active-passive Fault-tolerant Control of Nonlinear NCS based on Event-triggered Communication Scheme

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Abstract. The hybrid active-passive fault-tolerant control (FTC) problem based on discrete event-triggered communication scheme (DETCS) is studied for nonlinear NCS (NNCS) with time-varying delay and any actuator failure. A T-S fuzzy model is adopted to describe the fault model of NNCS in which the integration of event-triggered condition and actuator failure is realized. Furthermore, by using of the appropriate constructed Lyapunov-Krasovskii function and H_{∞} control theory, the sufficient condition that ensure the system possess integrality against any possible actuator failures is deduced and the fault detection observer (FDO) is properly designed, respectively. Moreover, the co-design of FDO and active fault-tolerant controller (AFTC) is also presented, so that the system could maintain stability whenever the actuator failure happens and whatever type the failure is belong to. Finally, a numerical example is given to show the

Introduction

effectiveness of the proposed method.

Researching about FTC for NCS has appeals to researcher's attention for years and as a result has managed to achieve some significant progresses[1] [2], but there also many biased.

On one hand, the existing researches mainly about linear NCS, however, for many realistic systems, the controlled plants tend to nonlinear characteristics frequently. At present, researching about FTC for NNCS is still in primary stage [3] [4], waiting for further studying.

On the other hand, the existing FTC methods, mainly divided as active FTC (AFTC) and passive FTC (PFTC), have disadvantages that couldn't be neglected. In spite of this, a new idea named hybrid active-passive fault-tolerant control, which combined the merits of AFTC and PFTC and consequently improved the system performance significantly, has not been widely researched, or in other words, almost none literature referring hybrid active-passive fault-tolerant control for NNCS can be found so far.

Besides this, making a general survey of the achieved results about FTC for NCS, many of which adopt periodic time-triggered communication scheme (PTTCS) as the transmitting scheme, in which data is transmitted with an equal period driven by the physical clock. Considering of the limited network resources, some scholars have recently presented DETCS [5], in which whether or not the sampled state should be transmitted is determined by the current-sampled state and the error between the current-sampled state and the latest transmitted state. Recently, a few scholars introduce the DETCS into fault-tolerant control field for NCS, soon after it is proved that this work is very interesting and valuable in [6] [7].

Above all, this paper mainly researched hybrid active-passive fault-tolerant control for NNCS with time-varying delay and any actuator failure under DETCS, hoping system realize the following functions: when known fault happens, the PFTC that already has been designed off-line, would ensure the system remain stable; whereas when unknown failure occurs, the PFTC would slow down the rate of performance deterioration at the initial period, meanwhile, FDO would estimate the value of fault as soon as possible, then reconstructing controller according to the estimated value to compensate the influence of actuator failure to the system. Consequently, the system would

always remain stability whenever the failure happens and whatever type the failure is belong to.

Preliminaries and system description

The introduction of DETCS. The structure of the hybrid active-passive fault-tolerant control of NNCS under DETCS is shown in Figure 1.

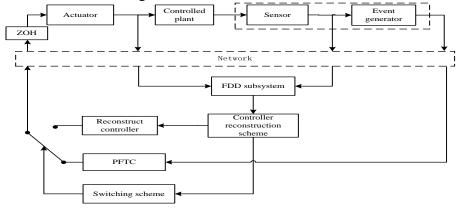


Fig. 1 Structure of the system

For case of convenient exposition, we made the following assumptions.

Assumption 1. Sensors are clock-driven. The system states are sampled at a constant period h, $i_k h$ is represented for sampled instants, and finally the set of sampled instants is represented by $\{i_k h | i_k \in N\}$.

Assumption 2. Controllers and actuators are event-driven. The transmitted instants $t_k h$ are determined by the sampled states $x(i_k h)$. The set of transmission instants is represented by $\{t_k h | t_k \in N\}$, which is of course a subset of $\{i_k h | i_k \in N\}$.

Assumption3. The system state is completely measured and it adopts the state-feedback control strategy. Networked-induced delays from sensor to controller $\tau_{t_k}^{sc}$, from controller to actuator $\tau_{t_k}^{ca}$ and

the computational delays $\tau_{t_k}^c$ are lumped together as $\tau_{t_k} = \tau_{t_k}^{sc} + \tau_{t_k}^{ca} + \tau_{t_k}^c$.

Assumption4. The detection of fault information is beyond the limitation of the event-triggered condition, that is to say, fault information can be transmitted to fault detection observer at every sampled instants.

Assumption5. The role of the ZOH is to store the latest data packet, in other words, the actuator keeps the control input unchanged until the output of the ZOH being updated to a new value.

In contrast to traditional NCS, the sample data needs to pass the event generator before being transmitted by the network, as depicted in Figure 1. The function of the event generator is to determine whether or not to transmit the latest sample signal to controller. The event-triggered condition is presented as following [5]

$$t_{k+1}h = t_kh + \min\{lh \mid e_x^{T}(i_kh) \equiv e_x(i_kh) \ge \sigma x^{T}(i_kh) \equiv x(i_kh)\}.$$
(1)

Where
$$e_x(i_kh) = x(i_kh) - x(t_kh)$$
. (2)

h is the sampling period, Ξ is symmetric positive definite matrix and σ is the bounded positive scalar. Only when $x(i_k h)$ and $x(t_k h)$ satisfied event-triggered condition (1), will the event generator be triggered and the sampled data $x(i_k h)$ be transmitted.

The description of NNCS model. Consider a T-S fuzzy system where *ith* rule of the system is expressed as following

$$R^{i}: \operatorname{If} \theta_{1}(t) \text{ is } N_{i1} \text{ and } \dots \theta_{g}(t) \text{ is } N_{ig}, \text{ then } \begin{cases} \dot{x}(t) = A_{i}x(t) + B_{i}u(t) + E_{i}f(t), i = 1, 2, \dots, n \\ y(t) = C_{i}x(t). \end{cases}$$

Where *r* is the number of rules; $x(t) \in \mathbb{R}^n$ is the state vector; $u(t) \in \mathbb{R}^m$ and $y(t) \in \mathbb{R}^p$ represent input and output vector of the system, respectively; $N_{is}(s = 1, 2, ..., g)$ is the fuzzy set; $\theta(t) = [\theta_1(t), \theta_2(t), ..., \theta_g(t)]^T$ denotes the premise variables and assume that it is not rely on u(t); and A_i , $B_i, C_i, E_i(i = 1, 2, ..., r)$ are constant matrices with appropriate dimensions.

The following T-S fuzzy system state equation can be inferred by using center-average defuzzifier, product inference and a singleton fuzzifier

$$\begin{cases} \dot{x}(t) = \sum_{i=1}^{r} h_i(\theta(t)) (A_i x(t) + B_i u(t) + E_i f(t)) \\ y(t) = \sum_{i=1}^{r} h_i(\theta(t)) C_i x(t). \end{cases}$$
(3)

Where $h_i(\theta(t)) = \mu_i(\theta(t)) / \sum_{i=1}^r \mu_i(\theta(t)), \mu_i(\theta(t)) = \prod_{s=1}^g N_{is}(\theta_s(t)), \text{ and } N_{is}(\theta_s(t)) \text{ is the membership value}$

of $\theta_s(t)$ in N_{is} . Suppose $\mu_i(\theta(t)) \ge 0, (i=1,2,...,r)$ and $\sum_{i=1}^r \mu_i(\theta(t)) \ge 0$, then $h_i(\theta(t)) \ge 0$ as well as

$$\sum_{i=1}^r h_i(\theta(t)) = 1$$

NNCS fault model based on DETCS. Based on the previous description of the controlled plant (3), the *ith* rule of the state-feedback control can be described as

 $R^{i}: \text{If }\theta_{1}(t) \text{ is } N_{i1} \text{ and } \dots \theta_{g}(t) \text{ is } N_{ig} \text{ , then } u(t) = K_{i}x(t_{k}h), t \in [t_{k}h + \tau_{t_{k}}, t_{k+1}h + \tau_{t_{k+1}}).$

Where K_i (i = 1, 2, ..., r) represent controller gain matrices to be determined in the following theorem, τ_{t_k} and $\tau_{t_{k+1}}$ are network-induced delay at the transmitting instants $t_k h$ and $t_{k+1}h$, respectively.

Meanwhile, considering the role of ZOH, when $t \in [t_k h + \tau_{t_k}, t_{k+1} h + \tau_{t_{k+1}})$, the state-feedback control law according to PDC algorithm is shown as following

$$u(t) = \sum_{i=1}^{r} h_i(\theta(t)) K_i x(t_k h).$$
(4)

Define $\tau(t) = t - i_k h.$ (5)

Obviously, $\tau(t)$ is a continuous linear function which meets the requirement of $0 < \tau_m \le \tau(t) \le \tau_M$, where τ_m and τ_M are the lower and upper bound of networked-induced delay, respectively.

Combined (2), (4) and (5), u(t) finally can be expressed as following

$$u(t) = \sum_{i=1}^{r} h_i(\theta(t)) K_i(x(t-\tau(t)) - e_x(i_k h)).$$
(6)

Supposing fault distribution matrix $E_i = -B_i$, i = 1, 2, ..., r, and we could define that Lu(t) = u(t) - f(t), where f(t) represents actuator failures and unknown matrix $L = diag\{l_1, \cdots , l_m\}$, $l_q \in [0,1], q = 1, 2, \cdots, m$ describes fault extent of system actuators, that is, $l_q = 0$ indicates that the *qth* actuator is totally invalid; $l_q = 1$ indicates that the *qth* actuator operates properly; $l_q \in (0,1)$ indicates that the *qth* actuator is at fault to some extent.

Then the fault model of NNCS can be transformed from (3) to (7) and (8)

$$\begin{cases} \dot{x}(t) = \sum_{i=1}^{r} h_i(\theta(t)) (A_i x(t) + B_i u(t) - B_i f(t)) \\ y(t) = \sum_{i=1}^{r} h_i(\theta(t)) C_i x(t). \end{cases}$$

$$(7)$$

$$\begin{cases} \dot{x}(t) = \sum_{i=1}^{r} h_i(\theta(t)) (A_i x(t) + B_i L u(t)) \\ y(t) = \sum_{i=1}^{r} h_i(\theta(t)) C_i x(t). \end{cases}$$
(8)

Remark 1. Obviously, the NNCS fault model (7) is equivalent to (8). The model integrates event-triggered condition, network-induced delay, actuator failures and control law into a unified framework, which lays a solid foundation for the following design of hybrid active-passive fault-tolerant controller for NNCS.

Related lemma. Lemma 1. For given symmetric matrix $Z = \begin{bmatrix} Z_{11} & Z_{12} \\ Z_{12}^T & Z_{22} \end{bmatrix}$, the following three conditions

are equivalent

1) Z < 0; 2) $Z_{11} < 0, Z_{22} - Z_{12}^T Z_{11}^{-1} Z_{12} < 0$; 3) $Z_{22} < 0, Z_{11} - Z_{12} Z_{22}^{-1} Z_{12}^T < 0$.

Lemma2. For any positive definite symmetric matrix $W \in \mathbb{R}^{n \times n}$, $W = W^T > 0$, scalar $0 \le h(t) \le h_M$ and vector function $\dot{x} : [-h_M 0] \rightarrow \mathbb{R}^n$, such that the following integration is well defined

$$-h(t)\int_{-h(t)}^{0} \dot{x}^{T}(t+s)W\dot{x}(t+s)ds \leq [x^{T}(t) \quad x^{T}(t-h(t))] \begin{bmatrix} -W & W \\ W & -W \end{bmatrix} \begin{bmatrix} x(t) \\ x(t-h(t)) \end{bmatrix}$$

Lemma3 [8].Let $f_1, f_2, \dots, f_N : \mathbb{R}^m \to \mathbb{R}$ have positive values in an open subset D of \mathbb{R}^m . Then, the reciprocally convex combination of f_i over D satisfies

$$\min_{\substack{\{\alpha_i \mid \alpha_i > 0, \sum_i \alpha_i = 1\}}} \sum_i \frac{1}{\alpha_i} f_i(t) = \sum_i f_i(t) + \max_{g_{i,j}(t)} \sum_{i \neq j} g_{i,j}(t).$$

Subject to

$$\{g_{i,j}: \mathbb{R}^m \to \mathbb{R}, g_{j,i}(t) = g_{i,j}(t), \begin{vmatrix} f_i(t) & g_{i,j}(t) \\ g_{i,j}(t) & f_j(t) \end{vmatrix} \ge 0\}$$

Main Results

Design of fault detection observer. Considering system model for NNCS (3), if there is no actuator failure, the state of the system can be observed. Supposing $\hat{x}(t) \in \mathbb{R}^n$ is the estimated state of x(t), $\hat{y}(t)$ is the output of the observer, according to PDC algorithm and NNCS model (7), fault detection observer is designed as following

$$\begin{vmatrix} \dot{\hat{x}}(t) = \sum_{i=1}^{r} h_i(\theta(t)) (A_i \hat{x}(t) + B_i u(t) + G_i(y(t - \tau(t)) - \hat{y}(t - \tau(t)))) \\ \hat{y}(t) = \sum_{i=1}^{r} h_i(\theta(t)) C_i \hat{x}(t). \end{aligned}$$

$$\tag{9}$$

Where G_i is gain matrix of the FDO.

Residual, state estimate error and residual error are defined as following, respectively.

$$r(t) = W(y(t) - \hat{y}(t)).$$
⁽¹⁰⁾

$$e(t) = x(t) - \hat{x}(t). \tag{11}$$

$$r_e(t) = r(t) - f(t).$$
⁽¹²⁾

Where W is residual gain matrix, and as a result

$$r(t) = \sum_{i=1}^{r} h_i(\theta(t)) W C_i e(t).$$
(13)

$$\dot{e}(t) = \sum_{i=1}^{r} \sum_{j=1}^{r} h_i(\theta(t)) h_j(\theta(t)) (A_i e(t) - G_i C_j e(t - \tau(t)) - B_i f(t)).$$
(14)

$$r_{e}(t) = \sum_{i=1}^{r} h_{i}(\theta(t)) (WC_{i}e(t) - f(t)).$$

$$(15)$$

The method of fault estimation based on observer is derived from H_{∞} control theory, in other words, observer and residual error of real system satisfied such relationship

 $\left\| r_{e}\left(t\right) \right\|_{2} \leq \gamma^{2} \left\| f\left(t\right) \right\|_{2}, f\left(t\right) \in L_{2}\left[0,\infty\right).$

Where γ is a given constant.

Thus, define H_{∞} performance index as $J_1 = \int_0^t \left(r_e^T(t) r_e(t) - \gamma^2 f^T(t) f(t) \right) dt$.

Theorem 1. For given positive scalar τ_m , τ_M , τ_s , a, b, c, ε , if there exist positive definite symmetric matrices P, Q_i , V_i , W which satisfied the following Linear Matrix Inequality (LMI)

	Φ_{11}	$\Phi_{\!\!12}$	Φ_{13}	$\Phi_{\!\!14}$	$\Phi_{\!15}$	$\Phi_{\!16}$	$\Phi_{\!\!17}$	$\Phi_{\!18}$	Φ_{19}^{-}	
	*	Φ_{22}	Φ_{23}	$\Phi_{\!$	0	0	$\Phi_{\!\scriptscriptstyle 27}$	$\Phi_{\!\scriptscriptstyle 28}$	$\Phi_{_{29}}$	
	*	*	Φ_{33}	$\Phi_{\!_{34}}$	0	0	0	0	0	
	*	*	*	$\Phi_{\!$	0	0	0	0	0	
Φ=	*	*	*	*	Φ_{55}	$\Phi_{\!\!56}$	$\Phi_{\!_{57}}$	$\Phi_{\!\scriptscriptstyle 58}$	$\Phi_{\!_{59}}$	< 0.
	*	*	*	*	*	$\Phi_{\!_{66}}$	0	0	0	
	*	*	*	*	*	*	Φ_{77}	0	0	
	*	*	*	*	*	*	*	$\Phi_{\!\scriptscriptstyle 88}$	0	
	*	*	*	*	*	*	*	*	Φ ₉₉ _	

Where * represents the corresponding matrix to be obtained through the symmetric matrix.

$$\begin{split} \Phi_{11} &= PA_i + A_i^T P + Q_1 - Q_3 - Q_4, \\ \Phi_{12} &= -V_i C_j, \\ \Phi_{13} &= Q_3, \\ \Phi_{14} &= Q_4, \\ \Phi_{15} &= -PB_i, \\ \Phi_{16} &= C_j^T W^T, \\ \Phi_{17} &= \tau_m A_i^T P, \\ \Phi_{18} &= \tau_m A_i^T P, \\ \Phi_{19} &= \tau_s A_i^T P, \\ \Phi_{22} &= -2Q_5 + M_{12}^T + M_{12}, \\ \Phi_{23} &= Q_5 - M_{12}, \\ \Phi_{24} &= Q_5 - M_{12}^T, \\ \Phi_{27} &= -\tau_m C_j^T V_i^T, \\ \Phi_{28} &= -\tau_m C_j^T V_i^T, \\ \Phi_{29} &= -\tau_s C_j^T V_i^T, \\ \Phi_{33} &= Q_2 - Q_1 - Q_3 - Q_5, \\ \Phi_{34} &= M_{12}^T, \\ \Phi_{44} &= -Q_2 - Q_4 - Q_5, \\ \Phi_{55} &= -\gamma^2 I, \\ \Phi_{56} &= -I, \\ \Phi_{57} &= -\tau_m B_i^T P, \\ \Phi_{58} &= -\tau_m B_i^T P, \\ \Phi_{59} &= -\tau_s B_i^T P, \\ \Phi_{66} &= -I, \\ \Phi_{77} &= -2aP + a^2 Q_3, \\ \Phi_{88} &= -2bP + b^2 Q_4, \\ \Phi_{99} &= -2cP + c^2 Q_5. \end{split}$$

Then we can obtain observer gain matrix through formula $G_i = P^{-1}V_i$ and the fault detection observer could ensure the fault estimation error meets the requirement of $\|r_e(t)\|_2 \le \gamma^2 \|f(t)\|_2$.

The proof to theorem 1 is omitted, if there is a need for it, please contact the author.

Design of PFTC. Aimed at system fault model (8), PFTC is designed as following.

According to formula (6), the state-feedback controller could be written as

$$u_p(t) = \sum_{i=1}^r h_i(\theta(t)) K_{pi} \left(x(t-\tau(t)) - e_x(i_k h) \right).$$

Where K_{pi} represents gain matrix of the PFTC, which ensure the system keeps asymptotically stable in the event of any possible actuator failure.

Theorem 2. Under the event-triggered condition (1) in the DETCS, for the given constants $\sigma \in [0,1), \tau_m, \tau_M, \tau_s$, if there exist some positive definite symmetric matrices $R_i > 0, i = 1, 2, ...5$ and V, Y_i , for any possible actuator failures in mode set *L*, these parameters satisfy the following LMI

	Φ_{11}	$\Phi_{\!\!12}$	$\Phi_{\!13}$	$\Phi_{\!\!\!14}$	Φ_{15}	$\Phi_{\!16}$	$\Phi_{\!\!17}$	$\Phi_{\!18}^{-}$	
Φ=	*	Φ_{22}	Φ_{23}	$\Phi_{\!_{14}}$ $\Phi_{\!_{24}}$	0	Φ_{26}	Φ_{27}	$\Phi_{\!28}$	< 0.
	*	*	$\Phi_{_{33}}$	$\Phi_{\!_{34}}$	0	0	Ο	0	
	*	*	*	$\Phi_{\!$	0	0	0	0	
	*	*	*	*	0 Ф ₅₅	Φ_{56}	$\Phi_{\!57}$	$\Phi_{\!58}$	
	*	*	*	*	*	$\Phi_{\!66}$	0	0	
	*	*	*	*	*	*	Φ_{77}	0	
	*	*	*	*	*	*	*	$\Phi_{\!\scriptscriptstyle 88}$	

Where * represents the corresponding matrix to be obtained through the symmetric matrix. $\Phi_{11} = A_i X + X A_i^T - 2X - R_1 + R_3 + R_4, \Phi_{12} = B_i L Y_j, \Phi_{13} = 2X - R_3, \Phi_{14} = 2X - R_4, \Phi_{15} = -B_i L Y_j, \Phi_{16} = \tau_m X A_i^T, \Phi_{17} = \tau_m X A_i^T, \Phi_{18} = \tau_s X A_i^T, \Phi_{22} = \sigma (2X - V) + 2R_5 - R_6 - R_6^T, \Phi_{23} = R_6 - R_5, \Phi_{24} = R_6^T - R_5, \Phi_{26} = \tau_m Y_j^T L B_i^T, \Phi_{27} = \tau_m Y_j^T L B_i^T, \Phi_{28} = \tau_s Y_j^T L B_i^T, \Phi_{33} = R_1 + R_3 + R_5 - R_2 - 4X, \Phi_{34} = 2X - R_6^T, \Phi_{44} = R_2 + R_4 + R_5 - 6X, \Phi_{55} = -2X + V, \Phi_{56} = -\tau_m Y_j^T L B_i^T, \Phi_{57} = -\tau_m Y_j^T L B_i^T, \Phi_{66} = -R_3, \Phi_{77} = -R_4, \Phi_{88} = -R_5.$

Then there exist state-feedback control law (6) which keeps the NNCS fault model (8) asymptotically stable. That is, (6) denotes the state-feedback control law with which the NNCS fault model (8) possesses robust integrity, where controller gain matrix and event-triggered weight matrix could be computed through $K_j = Y_j X^{-1}$ and $\Xi = V^{-1}$, respectively.

The proof to theorem 2 is omitted, if there is a need for it, please contact the author.

Design of hybrid fault-tolerant controller. Assuming $rank(F, E_i) = rank(F)$ is true firstly, according to theorem from literature [7], under the circumstance of the previous assumption, there exists matrix $F^+ \in R^{m \times n}$ makes the following equality $(I - FF^+)E_i = 0$ true.

Set hybrid fault-tolerant compensation controller based on fault detection observer is

$$u(t) = u_p(t) - F^+ E_i f(t).$$
⁽¹⁶⁾

Where F^+ is the right false inverse matrix of B_i , $u_p(t)$ is the designed PFTC from theorem 2, $\hat{f}(t)$ represents the estimate value of failure.

Applying (16) to (7), we obtain

$$\begin{vmatrix} \dot{x}(t) = \sum_{i=1}^{r} h_{i}(\theta(t)) \Big[A_{i}x(t) + B_{i}(u_{p}(t) - F^{+}E_{i}\hat{f}(t)) + E_{i}f(t) \Big] \\ = \sum_{i=1}^{r} h_{i}(\theta(t)) \Big[A_{i}x(t) + B_{i}u_{p}(t) - E_{i}(\hat{f}(t) - f(t)) \Big] \\ = \sum_{i=1}^{r} h_{i}(\theta(t)) \Big[A_{i}x(t) + B_{i}u_{p}(t) - E_{i}e_{f}(t) \Big] \\ y(t) = \sum_{i=1}^{r} h_{i}(\theta(t)) C_{i}x(t) \end{vmatrix}$$
(17)

Where $e_f(t)$ represents fault estimate error.

In consideration of fault detection observer designed in theorem 1 which satisfied the following performance index $||r_e(t)||_2 \le \gamma^2 ||f(t)||_2$, $f(t) \in L_2[0,\infty)$ and according to theorem 2, $u_p(t)$ could ensure the system (8) asymptotically stable, so we can get the conclusion that the formula (17) is asymptotically stable as well.

Simulation Experiment and Result Analysis

Adopt NNCS model data in literature [8] and the fuzzy membership function as $M_1(x_2) = \sin^2 x_2$

and $M_2(x_2) = \cos^2 x_2$, then the system model could be expressed as the following T-S fuzzy system of two rules.

$$R^{1}: \text{ If } x_{2} \text{ is } M_{1}, \text{ then } \begin{cases} \dot{x}(t) = A_{1}x(t) + B_{1}u(t) + E_{1}f(t) \\ y(t) = C_{1}x(t) \end{cases}.$$

$$R^{2}: \text{ If } x_{2} \text{ is } M_{2}, \text{ then } \begin{cases} \dot{x}(t) = A_{2}x(t) + B_{2}u(t) + E_{2}f(t) \\ y(t) = C_{2}x(t) \end{cases}.$$

$$re \quad A_{1} = \begin{bmatrix} -3 & 1 \\ 1 & -1 \end{bmatrix}, A_{2} = \begin{bmatrix} -2 & 1 \\ 1 & 0 \end{bmatrix}, B_{1} = \begin{bmatrix} 1 & 0 \\ 0 & -0.5 \end{bmatrix}, B_{2} = \begin{bmatrix} 1 & 0 \\ 0 & 0.5 \end{bmatrix}, C_{1} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}, C_{2} = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}.$$

Where

Setting parameters as following h = 0.05s, $\tau_m = 0.2$, $\tau_M = 0.3$, $\tau_s = 0.1$, $\sigma = 0.3$, a = 0.1, b = 0.2, c = 0.5.

For actuator normal or fault, matrix L is defined as following:

$$L_0 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}, \quad L_1 = \begin{bmatrix} 0.2 & 0 \\ 0 & 0.8 \end{bmatrix}, \quad L_2 = \begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix}.$$

According to theorem 2, we obtain the state-feedback controller gain matrices and the event-triggered weight matrix as following:

$$K_1 = \begin{bmatrix} -0.1666 & -0.0602 \\ -0.1996 & 0.5762 \end{bmatrix}, \quad K_2 = \begin{bmatrix} -0.1922 & -0.2265 \\ -0.2978 & -0.2203 \end{bmatrix}, \quad \Xi = \begin{bmatrix} 0.0033 & -0.0009 \\ -0.0009 & 0.0016 \end{bmatrix}.$$

Similarly, according to theorem 1, we obtain the fault detection observer gain matrices and the residual gain matrix as following:

$$G_1 = \begin{bmatrix} -0.3506 & 0.5883 \\ 0.4193 & 0.5824 \end{bmatrix}, \quad G_2 = \begin{bmatrix} 0.1181 & 0.6818 \\ 0.4257 & 0.4437 \end{bmatrix}, \quad W = \begin{bmatrix} 1.5662 & -0.1369 \\ -0.1369 & -1.6215 \end{bmatrix}.$$

Assuming the system operates normally before t = 5s, and known faults begin to appear at the

instant
$$t = 5s$$
, unknown fault such as $f = \begin{bmatrix} 0\\ 0.5 \end{bmatrix}$ begins to appear at the time $t = 10s$.

The simulation results are shown as following: The response curve of the estimation of faults is shown in Figure 2.

From Figure 2 we could make out that even though the fault estimated value lag behind fault input value at the instants t = 5s and t = 10s, they are fit closely at all other times, which illustrated the validity of the fault estimation method that we have adopted.

Setting initial condition $x(0) = \begin{bmatrix} 2 & -2 \end{bmatrix}^T$, under the aforementioned actuator failures in mode set *L* and the results contrasting figures of state component x_1, x_2 in passive (S1), active (S2) and hybrid (S3) fault-tolerant control are shown in Figure 3 and 4, respectively.

Observing Figure 3 and 4, we can conclude that, when actuator operates normally, both AFTC and PFTC could keep the system stable; when actuator appears known faults, PFTC could tolerant the fault effectively as well as keeps the system stable, whereas AFTC needs to reconstruct the controller according to the value of detected failure, and this certainly will waste some time to help the system recovery stable; on the contrary, when there happen unknown faults, PFTC lost the ability to tolerant faults and the system become unstable, but AFTC begins to show its superiority, compared to PFTC, AFTC reacts more quickly to failure. Though there appears amplitude jump at the initial period of failure, it executes fault detection and controller reconstruction rapidly and finally the system become stable again; the most significant aspect is that compared to AFTC and PFTC, adopting hybrid fault-tolerant control method not only can keeps the system stable when known fault occurs, meanwhile, reconstructing controller rapidly and finally makes the system recovery stable. Above all, hybrid active-passive fault-tolerant control method combined the merits of AFTC and PFTC, which contribute much to the improving of the system's stability.

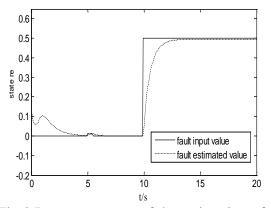


Fig.2 Response curve of the estimation of faults

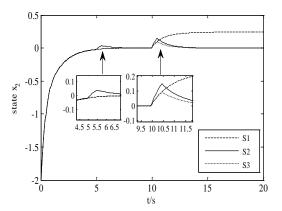


Fig.4 Response curve of state x_2 in different control action

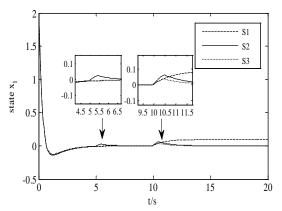


Fig.3 Response curve of state x_1 in different control action

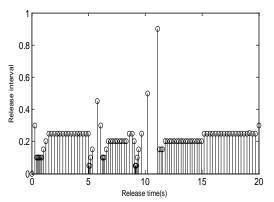


Fig.5 Release time(s) and release interval of data transmission for hybrid active-passive fault-tolerant control of NNCS based on DETCS

Similarly, under event-triggered condition (1) in the DETCS and with simulation time t = 20s, the relationship between release time(s) and release interval of data transmission is shown in Figure 5 as following.

As can be seen in Figure 5, the quantity of data transmission significantly decreases and as a consequence we can conclude that the DETCS driven by control demand is indicated to occupy less network resources than the PTTCS driven by a physical clock.

Conclusions

This paper mainly researched NNCS with time-varying delay based on DETCS, under the circumstance of reduce network resources, has realized the integrated-design of NNCS fault-detection observer and hybrid active-passive fault-tolerant controller. As has demonstrated in the above chapter, this new method not only can detect failures effectively, whether they are time-varying or not, but also can ensure the system keeps stability whatever type the failure is belong to. Finally, a numerical example is given to show the effectiveness of the proposed method.

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