

Water Pollution Risk Assessment for Water Transfer Projects

Lan-lan SONG^{a,*} and Jian-yun ZHANG^b

Nanjing Hydraulic Research Institute, Nanjing 210029, China

E-mail: ^amailsl@163.com, ^bjyzhang@nhri.cn

Abstract—Due to the imprecision of water environmental system and the repeated scarcity of quantitative information during transfer project, fuzzy theory might be an effective tool of the water pollution risk evaluation. Firstly, triangular fuzzy numbers of environmental parameters were defined. Then, fuzzy α -cut technique is introduced to figure out the fuzzy expected values. Based on the concept of fuzzy reliability of “recipient” water quality, the water pollution risk in fuzzy terms is calculated. Finally, the implementation process of the water risk assessment method is explained by the case study.

Keywords- water transfer project, triangular fuzzy number, α -cut technique, water pollution risk, Taihu Basin

I. INTRODUCTION

Ever-increasing water demand of a booming economy, environmental degradation, and potential climate-related threats are challenges of water resource management in china. To solve uneven distribution of water resources in time and space, the Ministry of Water Resources proposed holistic integrated water resource management-oriented inter-basin water transfer projects and water system connectivity to match the growing demands on these precious natural resources[1]. In fact, Chinese water transfer project traced back to 486 B.C, the Beijing–Hangzhou Grand Canal. To make up for the shortage water resources in north China, the South-to-North Water Diversion Project was brought up in the 1980s. Water transfer projects also have been effectively utilized to enhance water quality in many lakes, such as Lake Taihu, Xihu. However, the “donor” water quality takes effect on the “recipient” system. Yangtze River is the main “donor” river of these transfer projects. But, its N content doubled from 1980 to 1992[2]. These excess nutrients increase the production of “recipient” aquatic ecosystems, which often results in eutrophication. Inter-basin water transfers hydraulically connect two or more river basins that were hitherto unconnected. Diversions alter water allocation of river. Meanwhile, pollutants migration paths are changed with hydrological processes transmutation. River discharge is a key factor governing chemical components. Risk assessment is a sticking point for sustainable water management. It is necessary for prudence of the decision-maker to calculate the percentage impact on “recipient” the water quality during diversion project.

A consequence of damage or loss of an event can be explained by risk. Most of the hazards cannot be controlled or predicted with an acceptable degree of accuracy [3]. Therefore, uncertainty plays an important role in water quality management problems [4]. One of uncertainty theories that has been arisen in these last decades is fuzzy theory [5], which can be utilized to incorporate epistemic

uncertainty [6]. When quantitative information about environmental effects associated with the execution of activities and projects is restricted, imprecise and vague, fuzzy logic is a key solution to judge the optimal environmental harmony. Fuzzy logic has successfully involved in surface water quality management [7], groundwater contamination risk [8], water resource management [3] and environmental impact evaluation [9]. In addition, fuzzy sets and arithmetic can be found in several engineering applications [10]. With the development of fuzzy set theory, several new types of fuzzy numbers have been provided in succession in recent years. These new types include triangular or trapezoidal fuzzy numbers, Gaussian fuzzy number, lognormal-shaped fuzzy number, and Cauchy shaped fuzzy number. Numerous studies have developed triangular fuzzy numbers [11]. Since the concept of α -cut technique was advanced, it has been widely applied in various subjects. α -cut level reflects the different sets of numbers with a given minimum likeliness [12].

Therefore, fuzzy numbers of environmental parameters and suitable operators are put forward to estimate the “recipient” water pollution risk in transfer projects.

II. BASIC PRINCIPLES OF RISK ANALYSIS OF TRIANGULAR FUZZY NUMBERS

A. Triangular Fuzzy Numbers

Fuzzy numbers is a valid tool to compare consequence of the execution of activities and projects, especially to process incomplete data in environment impact and risk assessment.

The input space is mapped to a membership value (μ) by a membership function. If X is the input space and its elements are denoted by x , then a fuzzy set \tilde{A} in X is defined as a set of ordered pairs.

$$\tilde{A} = \{(x, \mu_{\tilde{A}}(x)) : x \in X\} \quad (1)$$

$\mu_{\tilde{A}}(x)$ is the membership function of x in \tilde{A} . Each element of X is transformed into membership value by the membership functions. The membership value varies between 0 and 1.

Let us define a triplet (a_1, a_2, a_3) as a triangular fuzzy number, where $a_1 \leq a_2 \leq a_3$. Suppose $\tilde{A} = (a_1, a_2, a_3)$, and its membership function is

$$\mu_{\tilde{A}}(x) = \begin{cases} 0 & \text{for } x < a_1 \\ \frac{x-a_1}{a_2-a_1} & \text{for } a_1 \leq x \leq a_2 \\ \frac{a_3-x}{a_3-a_2} & \text{for } a_2 \leq x \leq a_3 \\ 0 & \text{for } x > a_3 \end{cases} \quad (2)$$

B. α -Cut of A Triangular Fuzzy Number

The α -cut of fuzzy set \tilde{A} is a set consisting of those elements of the universe X whose membership values exceed the threshold level α . that is

$$\tilde{A}_\alpha = \{x | \mu_{\tilde{A}}(x) \geq \alpha\} \quad (3)$$

A crisp interval is obtained by α -cut operation. Then, $\square \alpha \in [0, 1]$ interval A^α is

$$A^\alpha = \{x | \mu_{\tilde{A}}(x) \geq \alpha\} \quad (4)$$

$$A^\alpha = [a_L^\alpha, a_R^\alpha] = [(a_2 - a_1) \alpha + a_1, (a_2 - a_3) \alpha + a_3] \quad (5)$$

III. WATER POLLUTION RISK ASSESSMENT METHOD FOR WATER TRANSFER PROJECTS

A. Definition of Triangular Fuzzy Numbers

Let us consider that monitoring (or calculation) data of the environmental component may lie in between “recipient” environmental background value and “donor” water environmental value during water transfer. Suppose that the most possible values of environmental component have normally been calculated by the complete river mixing mode.

The river mixing model is expressed as

$$c_m = (Q_s c_s + Q_b c_b) / (Q_s + Q_b) \quad (6)$$

Where, c_b and c_s denote the concentrations of a selected environmental component in the “recipient” and “donor” river, respectively; Q_b is the flow in “recipient” river before transfer project; Q_s is dilution flow in “donor” river.

Consequently, c_s as the lower, c_b as the upper and c_m as the most possible values, we can define a triangular fuzzy parameter \tilde{Z} in water diversion, namely

$$\tilde{Z} = (c_s, c_m, c_b) \quad (7)$$

We can approximately describe the membership function of fuzzy parameter \tilde{Z} by Eq. (2). Then the general form of the α -cut set of triangular fuzzy numbers is

$$Z^\alpha = [(c_m - c_s) \alpha + c_s, (c_m - c_b) \alpha + c_b] \quad (8)$$

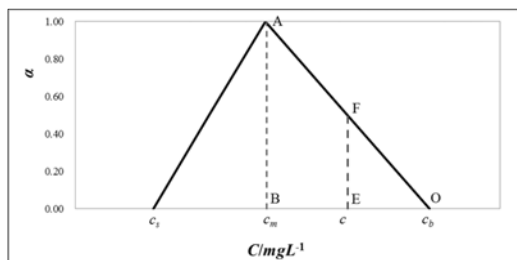


Figure 1. Triangular fuzzy curve of pollutant concentration.

B. Determination of Water Pollution Risk

Three possible types of “recipient” water quality exist during the transfer process. When $c_{j,i} > c_{b,j}$, the amount of degradation and dilution is less than that of any contaminants transported into the river from upstream; the pollution risk is 1. When $c_{j,i} < c_{m,j}$, the “recipient” water quality is improved considerably for high biodegradable speed and increased dilution flow; The pollution risk is zero. When $c_{m,j} \leq c_{j,i} \leq c_{b,j}$, the amount of degradation and dilution is greater than that of any contaminants transported into the river from upstream; Water transfer will improve the “recipient” water quality. But, there exists recontamination risk in the “recipient” water body. In order to assess the pollution risk of inter-basin transfer projects, a triangular risk coefficient (R) was introduced.

A fuzzy measure of reliability or water pollution risk may be obtained as

$$R = \begin{cases} 0 & \text{for } c < c_m \\ S_{ABEF} / S_{ABO} & \text{for } c_m \leq c \leq c_b \\ 1 & \text{for } c > c_b \end{cases} \quad (9)$$

S_{ABEF} is the area comprised between the representations of the membership function of \tilde{Z} and c and S_{ABO} is the area under the representation of the membership function of \tilde{Z} .

The area between the membership function of \tilde{Z} and its triangular approach in the descending section of the curve is

$$S_{ABEF} = \int_{c_m}^c \mu_{\tilde{Z}}(c) dc \quad (10)$$

The area under the triangular approach (S_{ABO}) is

$$S_{ABO} = \int_{c_m}^{c_b} \mu_{\tilde{Z}}(c) dc \quad (11)$$

IV. CASE STUDY

The well-investigated Taihu River transfer project was utilized in this study as an example to assess water pollution risk.

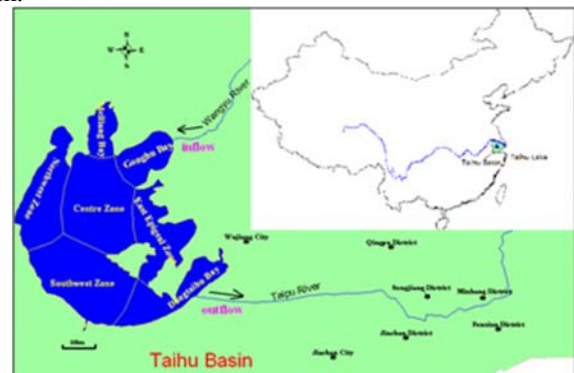


Figure 2. Seven subzones of Lake Taihu. The arrows in bold indicate the direction of the water transferred from Yangtze River to Lake Taihu.

Located in the Yangtze River Delta Lake, Taihu basin, the most developed area in China, is approximately 36,900 km² [13]. As a large shallow (mean depth of 1.9 m) eutrophic lake, Lake Taihu is divided into seven subzones, Gonghu Bay, Meiliang Bay, Northwest Zone, Southwest Zone, Centre Zone, East Epigeal Zone, and Dongtaihu Bay, based on its hydrological characteristics, aquatic plant distribution, water quality condition, and topography (Fig.2). There are drinking water intakes around East Epigeal Zone and Dongtaihu Bay, as water quality good for aquatic macrophytes purification [14]. In order to improve water quality and suppress algal blooms, water transfer from the Yangtze River has been implemented since 2002 [13]. Preliminary experiment began on January 31 in 2002, ended on August 23 in 2007. Roughly 4512 million m³ water was transferred from the Yangtze River. Approximately 5 percent good-quality water entered Lake Taihu [15]. Wangyu River was served as inflow channel and Taipu River was served as outflow channel [14].

Taipu River is a channel that connects Lake Taihu and Huangpu River and has multiple functions of flood control, drainage of waterlogged areas, water supply, irrigation, shipping, and tourism. To date, six main water plants are dispersed along Taipu River and in the upstream of Huangpu River. From these rivers, approximately 5.98 million m³ of water are obtained every day as drinking water sources of surrounding cities, such as Shanghai, Wujiang, and Jiashan. However, water pollution and eutrophication in recent years have become chief limiting factors of sustainable development of the economy in Lake Taihu basin [16, 17]. The water transfer to Huangpu River in 2006 began on March 17, ended on April 7. The inflow water quantity was controlled by Taipu sluice gate. When the water level of Dongtaihu Bay reached 3.14m, the sluice gate was opened to allow the water from Dongtaihu Bay to enter Taipu River until the level in the upstream sluice was equal to that in the downstream. The period from March 22 to March 29 is called the gate control period. Pump control period is from March 29 to April 4, where the sluice gate along Lake Taihu was closed and the pump stations of Taipu River were operated. Daily scheduling period is when the sluice gate was opened and the water level of Dongtaihu Bay exceeded 2.8m but was less than 3.5m (Table I). By the end of the transfer, the total water from Dongtaihu Bay, 280 million m³, was added into Taipu River. NH₄⁺ concentration and water input rate were obtained from the seven sites (Fig.3). All sampling sites were monitored every day during the transfer experiment.



Figure 3. Map of the monitoring section of the water transfer experiment.

TABLE I. OPERATING STATE IN TRANSFER EXPERIMENT

Time interval	Time	TPflo odgat e	TP pump	TP River inlet	HP River inlet	Control flow(m ³ /s)
Water storage	2006/3/17-2006/3/21	C	C	G	G	0-50
Gate control	2006/3/22-2006/3/29	C	C	G	G	50-300
Pump control	2006/3/29-2006/4/4	C	O	C	C	280-400
Daily scheduling	2006/4/4-2006/4/7	O	O	G	G	50-100

TP: Taipu HP: HuangPu O: open C: Close G: good operation

Taihu lake water is contaminated by continuous discharge of industrial and domestic wastes for fast industrialization and urbanization. Meanwhile, raising fish culture in net-cage is major source of revenue of local residents of East Taihu (Dongtaihu Bay). Fish culture in this area has raised some environmental problems [18]. Riverine NH₄⁺ may come from industrial wastewater and domestic sewage along rivers [19]. The rapid ammonia nitrogen accumulation in the water is a result of farmed fish caused by fish excretion and the decomposition of unconsumed fish food. Ammonia nitrogen is toxic to all vertebrates, and the tolerable concentration levels of this compound for an aquacultural system are quite low, usually being much less than 1 mg/L [20]. Water flow speed and the nitrification rate constant significantly increase during water transfer projects [21]. Ammonia nitrogen easy nitrifies under aerobic conditions. We also found that ammonia nitrogen is appropriate for the description of water quality changes during water transfer experiments. Therefore, we selected ammonia nitrogen to assess the degree of water pollution risk in the “recipient” water body.

A. Definition of Triangular Fuzzy Numbers

In this scenario, NH₄⁺ concentration of 36# was concentration of the “donor” area and reflected the quality of Dongtaihu Bay. The background concentration was the monitoring value of monitoring section (Table II).

TABLE II. AMMONIA CONCENTRATION INTRANSFER EXPERIMENT (UNIT:MG/L)

Date	36#	Taipu Gate	Pingwang	Fenhu	Liantang	Xiaziwei	Songpu
3/21	0.18	0.63	0.79	1.17	0.63	1.71	2.10
3/22	0.22	0.35	0.50	1.40	0.84	1.71	2.05
3/23	0.11	0.23	0.32	2.07	0.93	2.47	2.29
3/24	0.26	0.34	0.48	1.20	1.04	2.51	2.60
3/25	0.24	0.51	0.40	1.23	0.95	2.34	2.29
3/26	0.25	0.27	0.31	0.96	0.79	1.91	2.50
3/27	0.32	0.33	0.60	0.79	0.57	0.70	2.30
3/28	0.28	0.38	0.46	0.69	0.47	1.30	2.13
3/29	0.21	0.36	0.44	0.60	0.39	1.26	1.99
3/30	0.22	0.31	0.39	0.62	0.45	1.00	1.73
4/1	0.3	0.33	0.60	0.60	0.33	0.75	1.42
4/3	0.18	0.38	0.54	0.51	0.21	0.82	1.21
4/5	0.11	0.22	0.38	0.39	0.22	1.10	1.41
4/6	0.1	0.23	0.38	0.51	0.21	1.32	1.36
4/7	0.1	0.21	0.74	0.91	0.29	1.39	1.53
Quality level pre-experiment		III	III	IV	III	V	>V

Take Taipu gate section as example. NH_4^+ concentration of 36# and Taipu Gate were 0.18mg/L and 0.63mg/L on Mar. 21 before the transfer. The water inflow was 50m³/s, and the water discharge of Taipu Gate was 49m³/s (Table III). The modal value of Taipu Gate was 0.40mg/L by the river mixing model after the transfer. Then, the triangular fuzzy numbers of Taipu Gate section was (0.18, 0.40, 0.63). By use of α -cut technique, we can transform C_{T1} into the intervals of confidence at a certain α -level. We can obtain

$$C_{T1}^{\alpha}=[0.18\alpha+0.22, 0.23\alpha+0.63] \quad (12)$$

TABLE III. WATER DISCHARGE IN TRANSFER EXPERIMENT (UNIT:M³/S)

Date	water flow	Taipu Gate	Pingwang	Fenhu	Liantang	Xiaziwei	Songpu
3/22	50	49	116	128	225	173	288
3/23	100	63	109	207	231	176	267
3/24	100	104	172	288	348	272	451
3/25	200	134	176	343	278	179	286
3/26	200	222	247	155	197	111	198
3/27	300	292	260	199	172	125	160
3/28	300	308	299	160	117	84	98
3/29	300	170	192	169	107	172	198
3/30	280	282	246	189	157	117	99
4/1	280	276	217	175	188	135	183
4/3	280	277	193	182	234	176	230
4/5	50	94	77	181	128	151	185
4/6	50	49	112	149	143	263	455
4/7	50	62	168	217	325	319	549
gate control		168	196	206	209	318	450
pump control		283	208	184	182	318	283
daily scheduling		68.5	119	182	198	318	675

B. Calculation of the Water Pollution Risk Based on Triangular Fuzzy Numbers under α -Cut

According to measured data of Taipu Gate on Mar.22, (NH_4^+ :0.35mg/L) was less than the modal value (0.40mg/L). So, the water pollution risk R_{T1} is zero. In the same way, the triangular fuzzy numbers of the other monitoring section can be obtained, where $\tilde{C}_{P1}=(0.18, 0.61, 0.79)$, $\tilde{C}_{F1}=(0.18, 0.89, 1.17)$, $\tilde{C}_{L1}=(0.18, 0.55, 0.63)$, $\tilde{C}_{X1}=(0.18, 1.37, 1.71)$ and $\tilde{C}_{S1}=(0.18, 1.82, 2.10)$ on Mar. 22. Based on the water pollution risk R when considering five α -cut for each fuzzy number, we can get the results that $R_{P1}=0$, and $R_{F1}=R_{L1}=R_{X1}=R_{S1}=1.0$. The results presented in Table IV. The pollution risk of water quality in the different periods was shown in Table V.

TABLE IV. POLLUTION RISK OF WATER QUALITY IN DIFFERENT PERIODS

Date	Taipu Gate	Pingwang	Fenhu	Liantang	Xiaziwei	Songpu
3/22	0	0	1	1	1	1
3/23	0	0	1	1	1	1
3/24	1	1	0	1	1	1
3/25	1	0.75	1	0.97	0.99	0.96
3/26	0	0	0.87	0.90	0.93	1
3/27	1	1	0.90	0.74	0	0.99
3/28	1	0.50	0.93	0.78	1	0.99
3/29	0.94	0.98	0.92	0.76	1.00	0.99
3/30	0.78	0.91	1	1	0.91	0.97
4/1	1	1	1.00	0.51	0.85	0.93
4/3	1	0.93	0.85	0	1	0.94
4/5	0	0	0	1	1	1
4/6	1	1	1	0.97	1	0.99
4/7	0.95	1	1	1	1	1
average	0.69	0.65	0.82	0.83	0.91	0.98

TABLE V. POLLUTION RISK OF WATER QUALITY IN DIFFERENT PERIODS

Site Name	Gate control period	Pump control period	Daily scheduling period
Taipu Gate	0.62	0.93	0.65
Pingwang	0.53	0.95	0.67
Fenhu	0.83	0.95	0.67
Liantang	0.89	0.50	0.99
Xiaziwei	0.87	0.92	1.00
Songpu	0.99	0.95	1.00

V. CONCLUSION

Based on the fuzzy numbers, a new approach for fuzzy pollution risk analysis during transfer projects was put forward and proved to be very effective. From the transfer experiment, we found the "recipient" water quality improved remarkably when the transfer inflow was in range of 50-200m³/s. Notable abatement was in the concentration of ammonia nitrogen during the gate control period. When transfer inflow increase greater than 200m³/s in pump control period, there is high pollution risk. The limited success of water transfer operation is a result of sediment re-suspension by scouring and more pollutants from upstream enters into water diversion channel. Therefore, the dilution inflow in a specific range reduces the degree of pollution risk. In the late daily scheduling period, high pollution risk means low dilution inflow can't maintain water good conditions. The water quality status returned to their original state. Contrast to the gate control period, dilution flow about 100-200m³/s is appropriate. The highest pollution risk at Songpumeans water transfer experiment has little and no long-term effect on the water quality of upstream Huangpu River. Reducing the inputs of ammonia to the watershed would be a more feasible strategy to improve water quality than the transfer project, which seems to provide only a temporary improvement.

In this case, triangular fuzzy numbers can be converted into interval values that correspond to a specified confidence level of α through the use of α -cut technique. This procedure not only decreases the fuzziness of the parameters but also

enhances the practicability and flexibility of fuzzy arithmetic. The results of risk value estimations and the fuzzy expected values reflect the river pollution risk, which would provide the government and engineers with a more suitable and invaluable guide and overview on water quality and would clearly outline the policy and practice of conducting water transfer assessment. With fuzzy α -cut technique, river pollution risk can be quantitatively evaluated and managed in a more effective manner. The total damage that arises from the transfer project can be minimized, and the effectiveness of water resource management can be enhanced. Lastly, if no measured data are collected, mathematical model of water quantity and quality is used for water pollution risk analysis.

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