

The effect of the forced heat transfer on the eutectic ceramics preparation with zone melting process

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Abstract: The alumina-based eutectic ceramic is considered as a most promising candidate materials of aviation engines due to its excellent mechanical property and high temperature oxidation resistance. Effect of the forced heat transfer on the zone melting process of the eutectic ceramic is analyzed by finite element method. The results showed that: when the convective heat transfer coefficient increases, a higher heating power is required, especially at the initial growth stage; the melt convection intensity increases, and the convection pattern also changes. The depression degree of the solid-liquid growth interface increases significantly at the initial growth stage and this increase reduces as the interface moves away the crucible bottom.

1. Introduction

The strong demand for high temperature structural materials in the 21st century is the major motivation for the continuous development of new materials based on multi-compounds, because some of these compounds exhibit an interesting combination of high-temperature strength, oxidation resistance, optical or thermal emission properties, and so on [1].

The materials of aero engine turbine blade currently are mainly superalloys, of which highest working temperature is below 1100 °C [2]. The directionally solidified eutectic ceramic is considered to be a new promising candidate material to replace the superalloys due to its excellent properties. Compared with some major fabrication methods of the eutectic ceramics, the zone melting method can reach a higher temperature gradient to obtain high performance oxide eutectic ceramics. In the directional solidification process, the control of the heat and mass transfer in the liquid phase and the solid-liquid interface is very important to the crystal growth system [3].

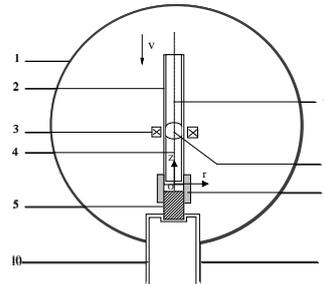
In the directional solidification process for eutectic ceramic, the interfacial relationships of different phases are parallel while the growth directions are not, and interfacial energy played a predominant role in controlling the solidification behavior of the eutectic crystal [4]. A flat interface is optimum through the zone melting process because a concave or convex interface may cause stress, crack, non-uniform impurities and bubbles [5]. Interface shape depends mainly on the hydrodynamics of the melt and the heat transfer of the whole system [6]. There are certain difficulties to predict and explain the evolution in the zone-melting process by the experimental method. Many researchers have studied the directional solidification process with numerical simulation method. Li etc. [7] simulated the evolution of the natural convection and the solid-liquid interface shape during the directional solidification process. The result show that: with the casting speed increases from 6 mm/min to 24 mm/min, the flow intensity of the vortex upward the center of the growth interface became stronger and the curvature of the interface has a significant increase. Sun etc. [8] studied the effect of the forced convection and the natural convection on the dendritic growth behavior. The results show that the convection accelerated the dendrite growth in the upstream direction and inhibit the growth in the downstream direction, forming a non-symmetrical

dendritic morphology. Chen etc. [9] developed a zone melting model to simulate the growth of Bi_2Te_3 columnar crystals. The results indicate that a high heating temperature and a low movement speed for the heater and the cooling devices should be used to obtain stable molten zone. The solidification interfaces were convex for a heater movement speed of 0.75 cm/h. Such interfaces were predicted to lead to larger columnar grains at the tail section. The shape of the solidification interface became level at a movement speed of 1.25 cm/h, allowing slender and straight columnar crystals to easily grow. The forced convection caused by the ACRT has a significant influence on the heat and mass transfer of the melt, and the temperature gradient near the solid-liquid interface would be obviously affected [10].

In order to obtain high-quality eutectic ceramic, the directional solidification process will be simulated by the FEM method to study the effect of forced heat transfer on the flow field and temperature field of the $\text{Al}_2\text{O}_3/\text{MgAl}_2\text{O}_4$ eutectic ceramics.

2. SIMULATION MODEL

The schematic view of the simulation model for the zone melting growth system is shown in Fig 1. The growth process is realized by the slow temperature profile moves upwards. The dissolution interface hits the hotter section of the temperature and dissolves the source material. This dissolution provides constantly the needed material to the liquid solution. At the same time, the growth interface hits the cooler section and the supersaturated solution in the vicinity of the growth interface solidifies on the crystals. Numerical simulation for the system needs to make some reasonable simplification as follows: The effect of the magnetic induction on the temperature distribution was ignored. A fixed temperature, 2100 °C, is applied at the crucible wall with the same height of the induction coil as the equivalent induction heating effect.



1-Furnace; 2-Crucible; 3-Induction coil; 4-Eutectic ceramics;
5-Corundum; 6-Pre-sintered source; 7-Melting zone; 8-Molybdenum; 9-Strut; 10-Flume

Fig.1 Schematic view of the zone-melting growth system

A calculation model of radiation heat transfer between outer wall of the crucible and the furnace has been built. The physical parameters of the adopted materials are isotropic, regarded as a function of temperature.

The energy equations of the melt zone, eutectic ceramics and crucible are shown as follows:

$$\rho_m C_{p,m} \frac{\partial T}{\partial t} + \rho_m C_{p,m} (\vec{u} \cdot \nabla) T = \nabla(k_m \nabla T) \quad (1)$$

$$\rho_c C_{p,c} \frac{\partial T}{\partial t} = \nabla(k_c \nabla T) \quad (2)$$

$$\rho_a C_{p,a} \frac{\partial T}{\partial t} = \nabla(k_a \nabla T) \quad (3)$$

\vec{u} , k , ρ , c are the velocity vector, thermal conductivity, density and specific heat.

The right boundary of temperature field is the symmetry axis. The heat transfer between the furnace and the crucible follows the radiation form, and the heat flux is calculated as:

$$q_{12} = \varepsilon \sigma F_{12} (T_1^4 - T_2^4) \quad (4)$$

Where T_1 is the surface temperature of the crucible and T_2 the temperature of the inner surface of the furnace. σ , ε , F_{12} are the Boltzman constant, radiation coefficient and view factor.

The ceramic solidification process is accompanied with the release of latent heat. This part of the energy has a significant impact on the crystal growth process. The latent heat of crystallization is equivalent to an internal heat source during the solidification process. An enthalpy method of solving phase change problems can be used for this process, assuming latent heat release within $0.1\text{ }^\circ\text{C}$.

$$\Delta H(T) = \int_{t_1}^{t_2} \rho C(t) dt \quad (5)$$

In the model the liquid solution is assumed to be an incompressible, Newtonian viscous liquid, and the flow in the liquid solution is laminar. The melt flow field meets the Navier-Stokes equations, so the Continuity equations are taken as follows:

$$\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial r} + w \frac{\partial u}{\partial x} = -\frac{1}{\rho} \frac{\partial p}{\partial r} + \frac{\mu}{\rho} \left(\frac{\partial^2 u}{\partial r^2} + \frac{\partial^2 u}{\partial x^2} + \frac{1}{r} \frac{\partial u}{\partial r} - \frac{u}{r^2} \right) + \frac{v^2}{r} \quad (6)$$

$$\frac{\partial v}{\partial t} + u \frac{\partial v}{\partial r} + v \frac{\partial v}{\partial x} = -g - \frac{1}{\rho} \frac{\partial p}{\partial x} + \frac{\mu}{\rho} \left(\frac{\partial^2 v}{\partial r^2} + \frac{\partial^2 v}{\partial x^2} + \frac{1}{r} \frac{\partial v}{\partial r} \right) \quad (7)$$

$$\frac{\partial w}{\partial t} + u \frac{\partial w}{\partial r} + v \frac{\partial w}{\partial x} = \frac{\mu}{\rho} \left(\frac{\partial^2 w}{\partial r^2} + \frac{\partial^2 w}{\partial x^2} + \frac{1}{r} \frac{\partial w}{\partial r} - \frac{w}{r^2} \right) - \frac{uw}{r} \quad (8)$$

Where u , v and w are the velocity components in the radial, vertical and circumferential directions, respectively.

The continuity equation of the fluid flow is as follow:

$$\frac{\partial u}{\partial r} + \frac{\partial v}{\partial z} + \frac{u}{r} = 0 \quad (9)$$

The rigid no-slip boundary condition was applied at solid-liquid interface.

$$u = 0, v = 0, \omega = \omega_a, \frac{\partial p}{\partial z} = 0, \frac{\partial F}{\partial z} = 0. \quad (10)$$

The right boundary of the flow field is the symmetry axis, rigid free-slip boundary condition, and the left side of the flow field is set to be a rigid non-slip boundary condition.

$$u = 0, \frac{\partial v}{\partial r} = 0, \omega = 0, \frac{\partial p}{\partial r} = 0, \frac{\partial F}{\partial r} = 0. \quad (11)$$

$$u = 0, v = 0, \omega = \omega_a, \frac{\partial p}{\partial r} = 0, \frac{\partial F}{\partial r} = 0. \quad (12)$$

The materials' physical properties of the growth system were listed in table 1.

TABLE 1 The materials' physical properties

	Density $\rho(\text{Kg}/\text{m}^3)$	Thermal conductivity $\lambda \text{ W}/(\text{Kg} \cdot ^\circ\text{C})$	Specific heat $C \text{ J}/(\text{Kg} \cdot ^\circ\text{C})$	Emissivity ε
Mo	10220	$118+0.03T-2.4*10^{-5} T^2$	$589-0.489T+1.8*10^{-4}T^2$	0.1~0.3
$\text{Al}_2\text{O}_3/\text{MgAl}_2\text{O}_4$	3580	5.9	836	0.9
Corundum	3600	21	800	0.9
1Cr18Ni9Ti	7850	12.1~ 27.8	502~692	0.36~0.44
Copper coil	8920	336	394	0.8

In order to study the effect of the forced heat transfer on the directional solidification process, four examples were set as the following table 2.

TABLE 2 Parameters of the numerical examples

	Inside radius of crucible (cm)	The maximum crucible wall temperature (°C)	heat transfer coefficient (W/m ² ×°C)
a	0.5	2100	0
b	0.5	2100	100
c	0.5	2100	200
d	0.5	2100	300

3. Results and discussion

3.1 The Effect of the Forecd Heat Transfer on the Heating Power of the Eutectic Ceramics Growth System

According to Fig. 2 it can be known, with the eutectic growth process proceeds, the required heating power reaches the maximum when their growth stages reach 70%. When the growth stage reaches 30%, the required heating power values of the four examples are 23.46 KW, 23.53 KW, 23.60 KW, and 23.67 KW respectively. With the heat transfer coefficient increases from 0 W/m²×°C to 300 W/m²×°C, the heating power of the eutectic ceramic growth furnace increases in some extent. As the growth stages reach 90%, the difference of the heating power with different heat transfer coefficient is insignificant. It is because the heat transfer process mainly occurs in the bottom region of the crucible, with the zone melting process proceeds, the influence is less.

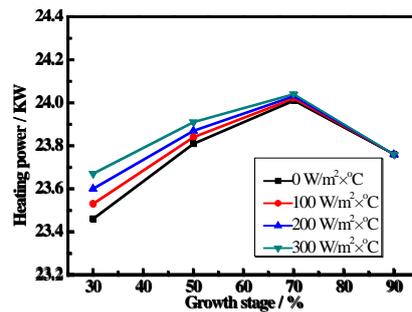


Fig. 2 The effect of forecd heat transfer on the system heating power

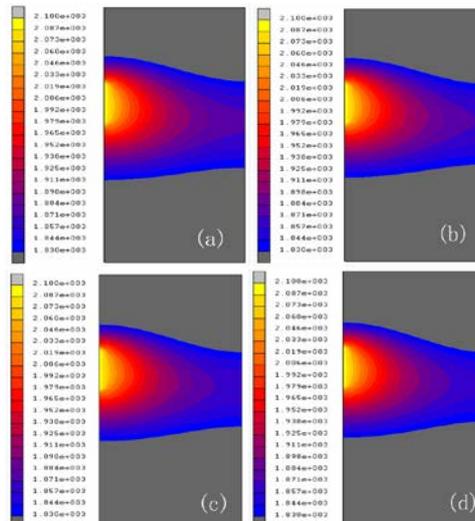


Fig. 3 Temperature fields of the four examples when the solidification stages reach 30%

3.2 The Effect of the Forecd Heat Transfer on the Temperature Field of the Ceramics Growth System

The temperature fields of zone-melting growth system reached 30% with different heat transfer

coefficients are shown in Fig. 3. The gray area above the melting is source materials and the gray area below the melting area is eutectic ceramics. The interface between the melt zone and the source material is the dissolution interface, and the interface between the melt zone and eutectic ceramics is the growth interface.

The growth interfaces of the four examples were depressed to the melting zone, the depression points fall on the center axis of the melt zone. The growth interfaces depression values are 0.95 mm, 1.06 mm, 1.11 mm, and 1.29 mm with the heat transfer coefficient changes from $0 \text{ W/m}^2 \times ^\circ\text{C}$ to $300 \text{ W/m}^2 \times ^\circ\text{C}$. With the heat transfer coefficient increases within the set range, the growth interfaces show a more obvious depression, this would have an unfavorable influence to the eutectic growth process.

3.3 The Effect of the Forecd Heat Transfer on the Growth Interface of the Eutectic Ceramics Growth System

Depression values of the solidification interface with different heat transfer coefficients are shown in Fig. 4. As the forced heat transfer is applied, the depression value of the growth interface is reduced. With the heat transfer coefficient increases from $0 \text{ W/m}^2 \times ^\circ\text{C}$ to $300 \text{ W/m}^2 \times ^\circ\text{C}$, the depression values of the growth interface show a increasing tendency. When the heat transfer coefficient is $300 \text{ W/m}^2 \times ^\circ\text{C}$ at 30% growth stage, the growth interface depression values of the four stages are 1.29 mm, 1.67 mm, 1.79 mm and 1.62 mm, the average value of which is 1.59 mm. Therefore, it can be shown that applying the forced heat transfer can increase the depression value of the eutectic growth interface. This result would go against the quality of the eutectic ceramic.

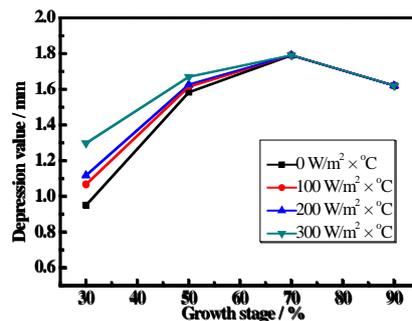


Fig. 4 Effect of the forecd heat transfer on the depression value of the solidification interface

3.4 The Effect of the Forced Heat Transfer on the Flow Field of the Eutectic Ceramics Growth System

The calculated flow vector field and flow intensity field with different heat transfer coefficients when the growth systems reach to 30% are shown in Fig. 5 and Fig. 6 respectively, the unit of the flow field intensity is “cm/s”.

As can be shown from Fig. 5, the flow field of the melt includes a clockwise convection cell near the crucible wall and a counterclockwise convection cell close to the axis of the computation area. As can be shown in Fig.6, the velocity intensity of the counterclockwise convection cell is significantly stronger than the clockwise convection cell. The contact position of the two convection cell exhibits the strongest velocity intensity because of the combined action of the two convection cells. The maximum flow field velocity increases from $2.75e^{-4} \text{ cm/s}$ to $3.09e^{-4} \text{ cm/s}$ with the heat transfer coefficient changes from $0 \text{ W/m}^2 \times ^\circ\text{C}$ to $300 \text{ W/m}^2 \times ^\circ\text{C}$. With the increase of the heat transfer coefficient, the velocity intensity of the counterclockwise convection cell is stronger than that of the clockwise convection cell. The area occupied by the clockwise convection cell increases and the area occupied by the counterclockwise convection cell is squeezed correspondingly. The convection intensity of the flow field become stronger with increase of the heat transfer coefficient during the directional solidification process, the result leads to a higher intensity of the heat and mass transfer, so the uniformity of the crystalline component and the completeness of the crystal may be affected.

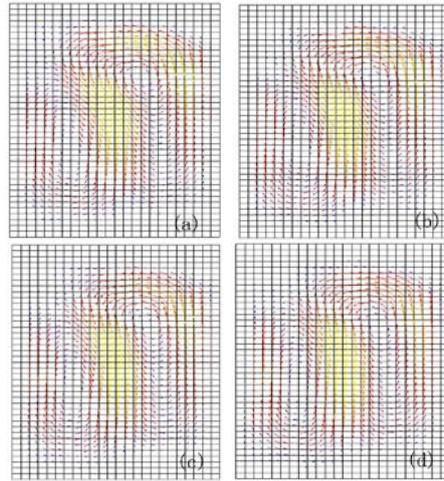


Fig. 5 Fluid vector fields of the four examples when the solidification stages reach 30%

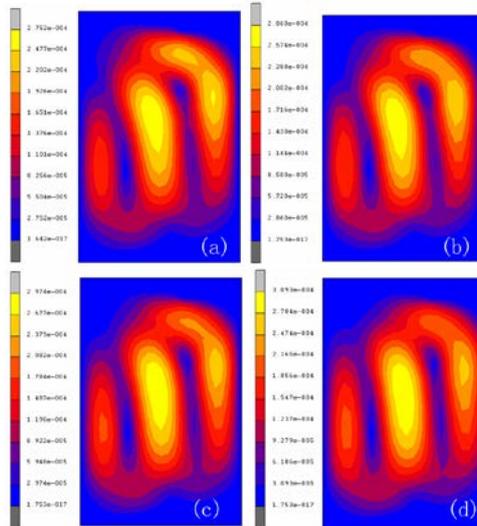


Fig. 6 Fluid velocity fields of the four examples when the solidification stages reach 30%

4. Conclusion

Effect of the forced heat transfer on the zone melting process of the $Al_2O_3/MgAl_2O_4$ eutectic ceramic is analyzed by the finite element method. The main conclusions are as follows:

In the eutectic ceramics growth process, when the forced heat transfer is applied, the required heating power needs to be increased for maintaining the temperature at a constant value a higher heating power is required in the low growth stage especially. The required heating power reaches the maximum value when the growth stage is 70%.

The depression values of the four examples reach the maximum value when the growth process reaches 70%. Applying the forced heat transfer can increase the depression value of the crystal growth interface.

When the growth process stage reaches 30%, the flow field includes a clockwise convection cell near the crucible wall, and a counterclockwise convection cell close to the axis of the calculation area. The integral intensity of the flow field becomes stronger with the heat transfer coefficient increases during solidification process. With the increase of the heat transfer coefficient, the flow field intensity increases and the fluid morphology has a change in some extent.

Acknowledgment

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