

# Design of Efficient Dynamic Digital Channelization Structure

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**Abstract.** In order to solve the problem of inflexible parameter settings in traditional dynamic channelization structure, a weighted overlap-add (WOLA) filter bank is proposed to implement dynamic channelization structure. The filter bank is deduced and emulated through MATLAB. The simulation results show that the WOLA dynamic channelization structure enhances the flexibility of parameter setting and the reconstruction error is within  $5 \times 10^{-3}$ . Comparing with the Discrete Fourier transform (DFT) polyphase filter structure, the system reconstruction error is reduced by an order of magnitude, it is verified the feasibility and good reconstruction characteristics of the WOLA dynamic channelization structure.

**Key words:** dynamic channelization structure, weighted overlap-add(WOLA), feasibility.

## INTRODUCTION

With the development of communication technology, the different communication standards and modulations continue to emerge [1]. The receiver bandwidth of wideband receiver contains many unknown signals whose carrier frequency and bandwidth are random. It has brought great challenges to the reconnaissance broadband signal.

Channelization is a key technique for extracting independent signals within the receiving bandwidth. The traditional channelization is achieved by DFT polyphase filter structure and Multi-channel DDC structure. But it only applies to the situation where signals are known within the receiver bandwidth. Therefore, it is significant to study an efficient and dynamic channelization structure.

Abu-Al-Saud [2] proposed a wideband channelization method based on nonuniform subband decomposition in 2004. The subband technology was first introduced in channelization and had breakthrough significance. Bing Li [3] improved this structure in 2007. He proposed using energy detection to determine the position of the signal and then confirming the subband combining scheme. It was really realized the dynamic channelization of blind signals. However, the above-mentioned dynamic channelization structure are based on the DFT polyphase filter structure whose decimating factor and channel number must be equal. In order to break this restriction, a new dynamic channelization structure is proposed. The WOLA (Weighted overlap-add) filter bank [4] is introduced in the new structure to realize dynamic channelization. It is an efficient structure that makes setting of channel parameters more flexible and has a better reconstitution performance.

## MATHEMATICAL MODEL OF DYNAMIC CHANNELIZATION

The development of filter banks drives the channelization technology [5]. Figure 1 shows the structure diagram of dynamic channelization.

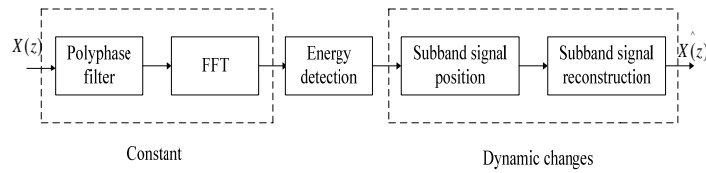


FIG.1. structure diagram of dynamic channelization

DFT Polyphase filter banks divide the input signals into several subbands. And synthesis filter banks reconstruct the subbands containing the signal determined by energy detection. This structure dynamically determines reconstruction scheme based on energy detection. Therefore, it was realized the dynamic channelization of blind signals. But the DFT Polyphase filter banks limits the flexible of setting parameters. So, we need study a new flexible and efficient dynamical channelization structure.

## WOLA FILTER BANKS

### WOLA Analysis Filter Bank

In the DFT polyphase filter bank, the  $k$ th channel output signal can be expressed as [6]:

$$\begin{aligned} X_k(m) &= \left[ x(n)e^{-jw_k n} \right] * h(n) \Big|_{n=mR} \\ &= \sum_{i=-\infty}^{\infty} h(mR - i)x(i)e^{-jw_k i} \end{aligned} \quad (1)$$

$R$  is decimating factor.  $K$  is channel numbers.  $w_k = 2\pi k / K$  expresses the center frequency of the  $k$ th channel. Assuming  $q = i - mR$ :

$$\begin{aligned} X_k(m) &= \sum_{q=-\infty}^{\infty} h(-q)x(q + mR)e^{-jw_k(q+mR)} \\ &= e^{-jw_k mR} \sum_{q=-\infty}^{\infty} h(-q)x(q + mR)e^{-jw_k q} \\ &= e^{-jw_k mR} \tilde{X}_k(m) \end{aligned} \quad (2)$$

$$\begin{aligned} \tilde{X}_k(m) &= \sum_{q=-\infty}^{\infty} h(-q)x(q + mR)e^{-jw_k q} \\ &= \sum_{q=-\infty}^{\infty} x_m(q)e^{-jw_k q} \end{aligned} \quad (3)$$

In equation (3),  $x_m(q) = h(-q)x(q + mR)$ . Since the number of channels is  $K$ , the number of samples of output sequence is  $K$  in each  $m$  moment. Therefore  $x_m(q)$  needs to be folded into a sequence of  $K$  points. Let  $q = p + lK$  that  $p = 0, 1, \dots, K - 1$ , then:

$$\begin{aligned} \tilde{X}_k(m) &= \sum_{p=0}^{K-1} \sum_{l=-\infty}^{\infty} x_m(p+lK)e^{-jw_k(p+lK)} \\ &= \sum_{p=0}^{K-1} \left[ \sum_{l=-\infty}^{\infty} x_m(p+lK) \right] e^{-jw_k p} \\ &= \sum_{p=0}^{K-1} \tilde{x}_m(p) e^{-jw_k p} \end{aligned} \tag{4}$$

$$\begin{aligned} \tilde{x}_m(p) &= \sum_{l=-\infty}^{\infty} x_m(p+lK) \\ &= \sum_{l=-\infty}^{\infty} x(mR+p+lK)h(-p-lK) \end{aligned} \tag{5}$$

According to the above formula, we can get the structure diagram of WOLA Analysis filter bank in figure 2.

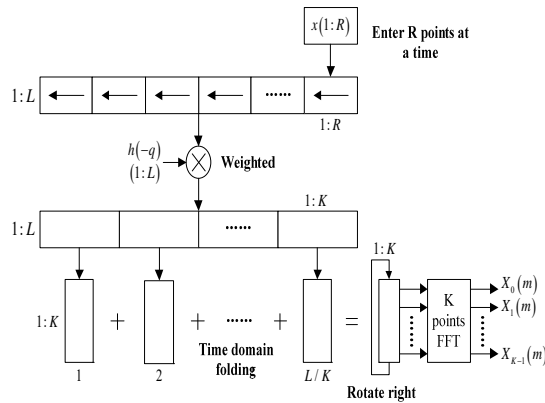


FIG.2. WOLA Analysis Filter Bank Implementation structure

The enter analysis filter bank signal processing flow can be divided into data segmentation, data weighting, splicing accumulation, rotate right and FFT.

### WOLA Synthesis Filter Bank

In the DFT polyphase filter bank, the synthesis of the output can be expressed as:

$$\begin{aligned} \hat{x}(n) &= \frac{1}{K} \sum_{k=0}^{K-1} \left[ Y_k(n) * f(n) \times e^{jw_k n} \right] \\ &= \frac{1}{K} \sum_{k=0}^{K-1} \sum_{m=-\infty}^{\infty} \hat{X}_k(m) f(n-mR) e^{jw_k n} \end{aligned} \tag{6}$$

Among (6),

$$Y_k(n) = \begin{cases} \hat{X}_k(m) & n = mR \\ 0 & \text{other} \end{cases} \quad (7)$$

Let  $n = r + MR$ ,  $r=0, 1, \dots, R-1$  and  $M$  is an integer.

$$\begin{aligned} \hat{x}(r + MR) &= \frac{1}{K} \sum_{k=0}^{K-1} \sum_{m=M-\alpha}^M \hat{X}_k(m) f(r + MR - mR) e^{jw_k(r+mR)} \\ &= \sum_{m=M-\alpha}^M f(r + (M - m)R) \frac{1}{K} \sum_{k=0}^{K-1} \hat{X}_k(m) e^{jw_k mR} e^{jw_k(r+(M-m)R)} \\ &= \sum_{m=M-\alpha}^M f(r + (M - m)R) \frac{1}{K} \sum_{k=0}^{K-1} \tilde{\hat{X}}_k(m) e^{jw_k(r+(M-m)R)} \end{aligned} \quad (8)$$

Among (8),  $\tilde{\hat{X}}_k(m) = \hat{X}_k(m) e^{jw_k mR}$ . Let

$$\begin{aligned} U_m(r + (M - m)R) &= \frac{1}{K} \sum_{k=0}^{K-1} \tilde{\hat{X}}_k(m) e^{jw_k(r+(M-m)R)} \end{aligned} \quad (9)$$

Because the  $e^{jw_k(r+(M-m)R)}$ 's period is  $K$ , so  $e^{jw_k(r+(M-m)R)} = e^{jw_k(r+(M-m)R)_{\text{mod } K}}$ .

$$\begin{aligned} U_m(r + (M - m)R) &= \frac{1}{K} \sum_{k=0}^{K-1} \tilde{\hat{X}}_k(m) e^{jw_k(r+(M-m)R)_{\text{mod } K}} \\ &= U_m((r + (M - m)R)_{\text{mod } K}) \end{aligned} \quad (10)$$

Substituting equation (10) into (8),

$$\begin{aligned} \hat{x}(r + MR) &= \sum_{m=M-\alpha}^M f(r + (M - m)R) U_m((r + (M - m)R)_{\text{mod } K}) \\ &= f(r) U_M(r) + f(r + R) U_{M-1}((r + R)_{\text{mod } K}) + \\ &\quad f(r + 2R) U_{M-2}((r + 2R)_{\text{mod } K}) + \\ &\quad \dots + \\ &\quad f(r + \alpha R) U_{M-\alpha}((r + \alpha R)_{\text{mod } K}) \end{aligned} \quad (11)$$

According to the above formula, we can get the structure diagram of WOLA Synthesis filter bank in figure 3.

The enter synthesis filter bank signal processing flow can be divided into IFFT, loop left, data weighting and splicing accumulation.

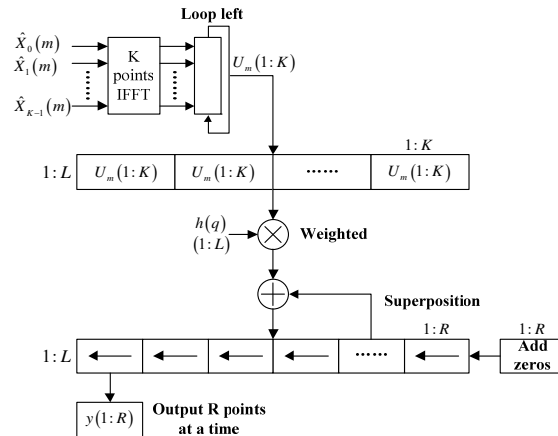


FIG.3. WOLA Synthesis Filter Bank Implementation structure

According to the above introduction, the advantages of WOLA structure can be drawn:

- 1 Releasing the multiples limitation of the number of channels  $K$  and the decimating factor of  $R$ .
- 2 Weighting with filter coefficients instead of convolution greatly reduces the amount of system computation.

### Dynamic Digital Channelization Structure Based on WOLA Filter Bank

Comprehending WOLA structure analysis filter bank and synthesis filter bank structure can get the dynamic digital channelization structure based on WOLA filter bank in figure 4.

The input signal is divided into several subbands by WOLA analysis filter bank. And then determining the position of the subchannel occupied by each subband signal by detection. Finally, the subbands which exist signal are inputted to synthesis filterbank to achieve signal's extraction.

This structure can make set of channel para-meters more flexible and has a better reconstitution performance.

### SIMULATION

This section will verify the WOLA dynamic-al channelization structure. The sampling rate of the input signal is  $f_s=1280$  MSPS, the channel number is  $K=256$  and the decimating factor is  $R=176$ . The sampling rate and the effective channel bandwidth of the channel baseband output are  $f_s/R=7.3$  MSPS and  $f_s/K=5$  MHz. A prototype filter with reconstructed characteristics is designed by raised cosine function. The length of prototype filter is 11264. The amplitude frequency characteristic curve of prototype filter is shown in figure 5. The sum of adjacent subband filters on power spectrum is shown in figure 6.

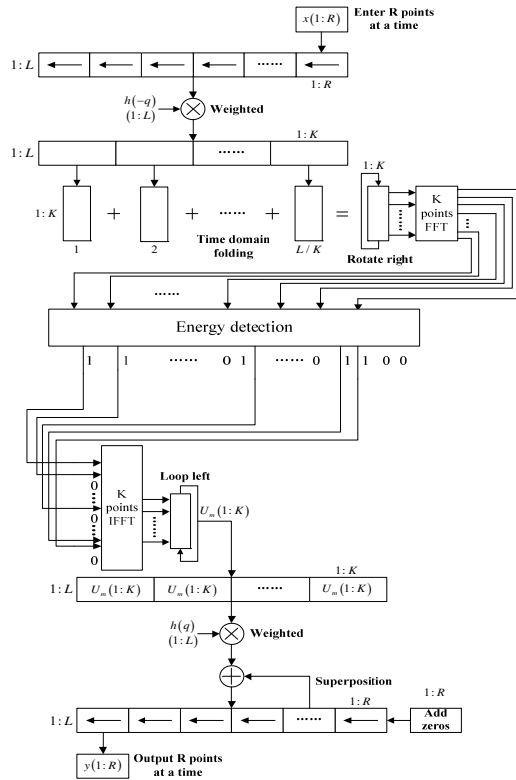


FIG.4. Dynamic Digital Channelization Structure Based on WOLA Filter Bank

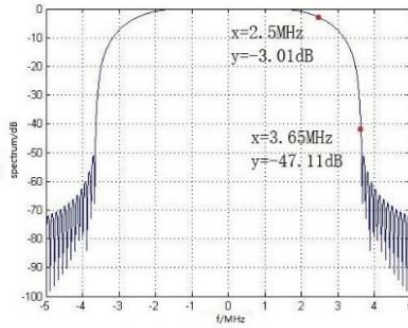


FIG.5. Amplitude-frequency response

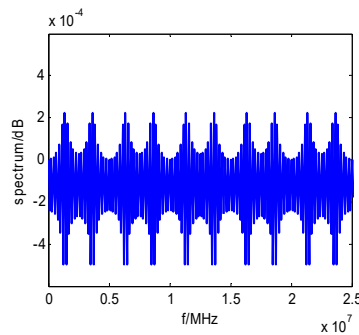


FIG.6. Subband power spectrum addition results

The prototype filter bank, whose bandwidth is 5 MHz and stopband frequency's attenuation is greater than -40 db. Figure 6 shows the error of the sum of spectrum is within  $1 \times 10^{-3}$  db. Therefore, this filter has good reconfiguration. Input test signal, one is sinusoidal signal, an-other is LFM signal.

$$x(t) = \cos(2\pi f_0 t) + \cos(2\pi f_1 t + \pi\lambda t^2) \tag{12}$$

$f_0=99\text{MHz}$ ,  $f_1=110\text{MHz}$ ,  $B=20\text{MHz}$ ,  $T=50\mu\text{s}$ ,  $\lambda = B / T$ . According to system parameter settings, the sinusoidal signal should appear in 20th subband and LMF should appear in 22th to 26th subbands. T-he figure 7 shows the result of 19th to 27th subbands' spectre.

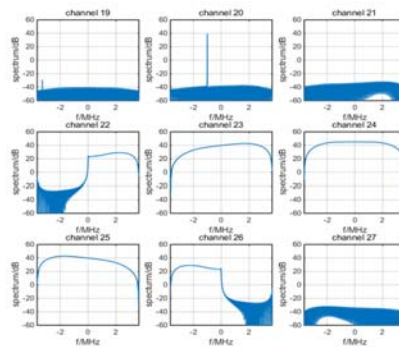


FIG.7. Subband spectrum

After energy detection, the subband existing signals are dynamically reconstruct. Figure 8 shows t-he spectrum of reconstruction signal. Figure 9 shows the comparison of reconstruction errors of DFT and WOLA structure. It can be seen from results that the WOLA dynamical channelization's reconstruction errors is less than  $5 \times 10^{-3}$  and the reconstruction errors of WOLA structure is much smaller than DFT structure. So, the WOLA dynamic channelization structure has a great reconstruction feature.

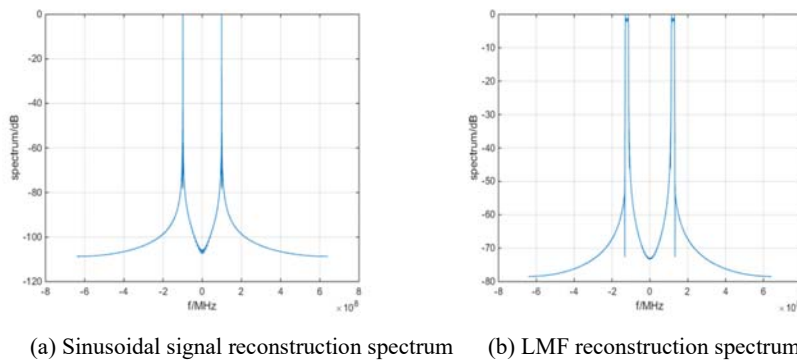


FIG.8. Spectrum of reconstruction signal

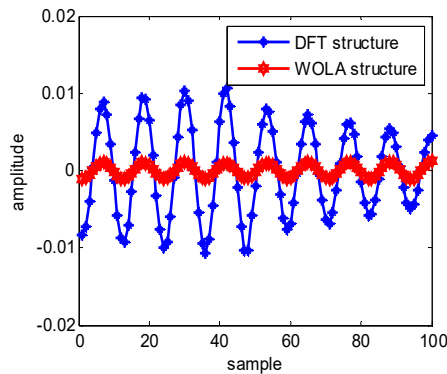


FIG.9. Comparison of reconstruction errors

## SUMMARY

The dynamic channelization structure based on WOLA filter bank is proposed to improve the flexibility of parameter setting. And the reconstruction errors are less than traditional structure.

It has important application value in the field of electronic reconnaissance.

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