

Modeling Pinhole Phenomenon in Sanitary Porcelains Case Study: Isatis Sanitary Porcelain Plant, Yazd, Iran

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Abstract

Sanitary porcelain products might have several defects, causing potential high-grade desirable products be converted into low-grade ones. Some of the defects are such that a few of them in the products will result in a great fall of product rating and consequently reduction of its value and price. Among these defects is a defect called pinhole. In this article, it has been tried to identify, from a list of factors, the most influential factors of the production process which cause the pinhole defect affecting the product rating. It then tries to present a prediction model for the number of pinholes. For this purpose, initially seven factors were chosen to help presenting a suitable prediction model and several statistical tools and artificial intelligence prediction tools were investigated to present a suitable prediction model. The presented model could be used by the company to enhance the product rating through choosing right value for the right factors causing the pinhole defect and to decrease the wastes and the expenditures.

Keywords: sanitary porcelain, pinhole, artificial neural networks, regression, correlation coefficient

1.Introduction

Defects in sanitary-wa	re products affec	t the quality	(rating) of	the produc	ets and the	factory ex	penditures .
If we can predict the	defects through	a model, w	e would be	able to pr	redict the 1	rating, to	enhance the

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Corresponding author.	



quality and to reduce the wastes and expenditures, by choosing right amounts for the factors participating in the model. Several defects (blisters, pinholes, specks, stuck, cracks, deformation, green spots,...) may be found in sanitary porcelains which tend to reduce the rating of these products. Some of these defects are identified before the baking phase and some are identified after the phase. The defective products with defects identifiable after the baking phase are not suitable for reproduction pinholes, which are quality flaw appearing as small holes in the fired glaze surface, are among the defects which could be identified after baking phase.

Fig. 1. Pinholes in a sanitary-ware product

This defect might occur on all part of the surface of sanitary-ware products. Figure 1 shows a surface having this flaw. A survey performed in *Isatis* sanitary porcelain manufacturing co., Yazd, Iran shows that 10.5% of the defective products is due to 'pinhole' flaw and causes severe losses to the manufacturer; due to this reason the manufacturer decided to do a research on pinhole[1]. The present article is based on the research. The manufacturing company would like to know if there is a relationship between "the number of pinholes in the products" and some factors such as the followings:

Glaze viscosity(V)

Surface tension of raw material(ST)

Speed of reaching the maximum temperature(SMT)

Glaze cooling speed(SC)

The maximum temperature of the furnace (MT)

Abrasion of Glaze raw materials(AG)

glaze dying time(TD)

curvature(S=smooth or C =curved)

The purpose of the present research is to find the key factors (if any) causing the pinhole phenomena from the above list and, using the key factors as input, to present a model for predicting the number pinholes in the product and thereby predicting the rating of the products with pinholes. If a suitable model is reached, the quality of the products could be improved by modifying the factors and the plant expenditures be decreased. This research is based on [1] and our literature survey did not result in any significant work in the prediction of pinhole defect; therefore this research could be regarded a new one. However [2] and [3] are helpful references for understanding some concepts regarding ceramics and component analysis used in this research.

2. Data

The data for this research is obtained from producing 42 curved and 122 smooth specimens with dimension of nearly 10cm×10cm at Istatis sanitary-ware plant located in Yazd, Iran with different values for V, ST, SMT, MT, AG & TD. Table 1 shows the mean of the values used for V, ST, SMT, MT, AG & TD variables and the mean number of pinholes created in 164 specimen as well as some other



information (minimum, maximum, median, range, standard deviation) about the mentioned features.

Table 1 mean, median, minimum, maximum, range, standard deviation of the initial data

Feature Feature							
(dimension)	Curvature	Mean	Median	Minimum	Maximum	Range	Std. Dev.
***	S	138.459	137.00	111.00	181.00	80.000	16.965
V (poise)	С	139.357	139.00	111.50	191.00	89.500	24.697
(poise)	ALL	138.689	137.50	111.00	191.00	90.000	19.163
	S	4.558	4.575	3.33000	5.680	2.350	0.396
ST (G)	С	4.784	4.825	2.79000	6.840	4.050	0.877
(0)	ALL	4.616	4.605	2.79000	6.840	4.050	0.565
	S	312.746	312.80	309.00	315.800	6.800	1.250
SMT (minute)	С	313.371	313.25	307.70	318.800	11.10	2.250
(minute)	ALL	312.906	312.90	307.70	308.800	1.10	1.584
	S	438.302	438.40	428.00	447.000	19.00	3.108
SC (minute)	С	439.867	439.45	424.100	453.000	29.90	5.994
(minute)	ALL	438.703	438.65	424.100	453.000	29.90	4.084
	S	1084.468	1085.45	1061.100	1094.000	33	6.416
MT (centigrade)	С	1084.160	1083.50	1064.20	1109.000	45	8.681
(comigrado)	ALL	1084.389	1084.800	1061.10	1109.000	48	7.038
	S	2.80	2.87	1.84	3.16	1.32	2.633
AG (mesh)	С	2.81	2.80	2.02	3.69	1.67	3.09
(mesh)	ALL	2.80	02.84	1.84	3.69	1.85	2.74
	S	133.211	133.300	130.20	135.90	5.700	1.906
TD (second)	С	133.479	133.550	131.40	135.40	4.00	1.89
(0000114)	ALL	133.280	133.350	130.20	135.90	5.70	1.90
	S	7.21	4.46	0	40	40	7.62
Pinhole	С	10.55	7.16	1	29	28	7.63
	ALL	8.87	5.97	0	40	40	7.69

2.1 Initial evaluation of data

Figure 2 shows the probability plot the number of pinholes in both curved (C) and smooth (S) specimens. According to the figure the pinhole data are not normally distributed.

An algorithm called Johnson transformation was applied on the pinhole data. The resulted data is referred as J-pinhole. As the normal probability plot of J-pinhole in Fig. 3 shows, the J-pinhole data is normally distributed.

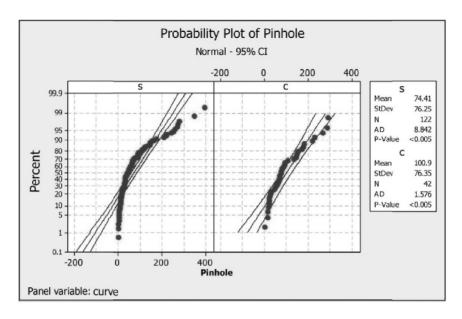


Fig. 2. Normal probability plot for the pinholes in the sample

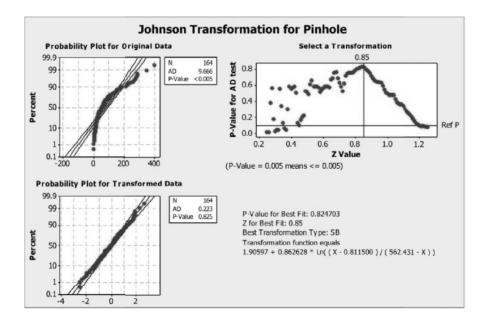


Fig. 3. Normal probability plot for J-pinhole data (i.e. the number of pinholes in the specimens after applying Johnson transformation)

A fit of linear regression model including all variables i.e. V, ST, SMT, MT, AG, TD to predict number of pinholes showed that the model is not appropriate for the pinhole data.

A stepwise regression model was then applied to J-pinhole data. Table 2 shows the result. The model correlation coefficient was 11% which is not acceptable.



Table 2 Stepwise Regression: J Pinhole versus V, ST,

Alpha-to-Enter: 0.15 Alpha-to-Remove: 0.15	
Response is J_Pinhole on 8 predictors, with N = 164	
Step 1 2 Constant -0.1354 -2.1142	SMT 0.148
V 0.0113 0.0113	T-Value 3.08
T-Value 2.82 2.90	P-Value 0.002
P-Value 0.005 0.004	S 0.981 0.957
CURVE0.42 -0.33	R-Sq 7.97 13.12
T-Value -2.39 -1.89	R-Sq(adj) 6.83 11.50
P-Value 0.018 0.061	Mallows Cp 16.1 8.4

These two experiments indicate either the relationship between pinhole data as the response versus V, ST, SMT,.... is not linear or some other variables should be considered or stronger tools are needed to model the relationship.

In the rest of this research J-pinhole data which are normally distributed are used.

What follows is about the effect of curvature on the number of pinholes.

The relationship between curvature and pinholes

To study the effect of curvature on the number of pinholes the following 2 tests of hypothesis were performed on the smooth and curved specimens:

A)a two sided F-test for the equality of the variance of J-pinhole data concerning curved surface and the variance of J-pinhole data concerning smooth surface;

B)a two sided t-test for the equality of the mean of J-pinhole data concerning curved surface and the mean of J-pinhole data concerning smooth surface.

We were allowed to perform the F-test & t-test on the J-pinholes data, because these data were proved to be normally distributed. Tables 3 &4 shows the results

Table 3 F-test for the equality of variances of J_Pinholes in the smoothed and curved surfaces

	_1 milotes in the smoothed and curved surfaces
A) Test and CI for Two Variances: J_Pinhole vs	Curve
Method	
Null hypothesis $Sigma(S) / Sigma(C) = 1$	
Alternative hypothesis Sigma(S) / Sigma(C) not = 1	
Significance level Alpha = 0.05	
	95% Confidence Intervals
Statistics	CI for
curve N St. Dev Variance	Distribution CI for StDe Variance
s 122 1.021 1.043	of Data Ratio Ratio
c 42 0.944 0.891	Normal (0.827, 1.372) (0.684, 1.882)
Ratio of standard deviations = 1.082	Continuous (0.833, 1.492) (0.695, 2.227)
Ratio of variances = 1.171	
Tests	
Test Method DF1 DF2 Statistic P-Va	lue
F Test (normal) 121 41 1.17 0.57	71
Levene's Test (any continuous) 1 162 0.72 0.3	397



From Table 3 it could be concluded that curvature does not increase or decrease the variance of the number of pinholes.

Table 4 t-test for the equality of mean of J Pinholes in the smoothed and curved surfaces

```
B) Two-Sample t-test and CI: J Pinhole, curvature
          Mean St Dev SE Mean
Cur. N
    122 -0.12 1.02 0.092
    42 0.310 0.944 0.15
Difference = mu(s) - mu(c)
Estimate for difference: -0.431
95% CI for difference: (-0.785, -0.076)
T-Test of difference = 0 (vs not =): T-Value = -2.40 P-Value = 0.017 DF = 162
Both use Pooled StDev = 1.0023
```

The t-test of Table 4 indicate that, on the average, the surface curvature causes more pinholes in comparison to the surface smoothness.

Are variables V, ST, SMT, MT, AG, TD normally distributed?

Utilizing Anderson-Darling test show that some of the variables are normally distributed and some not. The result of the test for both curved and smooth cases is shown in Table 5.

1 abie	Table 5. The status of the normality of the distribution of variables							
Feature	V	ST	SMT	SC	MT	AG	TD	
smooth	$\overline{\Delta}$	$\overline{\mathbf{A}}$		\square	-	-	-	
curved	$\overline{\Delta}$	$\overline{\mathbf{A}}$		\square	-	-	\square	

As Table 5 indicates the variables MT, AG are not normally distributed for both cases (smooth& curved) and TD is not normally distributed for smooth case. As stated earlier, J- pinhole data i.e. the results of Johnson transformation on the pinhole data will be used throughout this research.

3. Description of the method

The steps carried out during our research is as follows:

3.1. Step 1: Evaluation of data-detection of outlier data

In this phase of step 1 the outliers are detected in the multivariate data. Pair-wise scatter plots will not work as it is possible for an outlier to exist in all dimensions but not an outlier in any of the 2 dimensional subspaces.

It is important to realize, cases which are multivariate outliers may not necessarily be univariate outliers. In other words being an outlier on one of the variables under consideration is not necessarily a multivariate outlier.

One of the best ways to check for multivariate outliers is through Mahalanobis' distance. Mahalanobis' distance accounts for the different scale and the variance of each of the variables in a probabilistic way; in other words, if one considers the probability of a case being a member of the multivariate distribution,



then one must account for the density function, or standard deviation, of each variable in the multivariate set. Minitab 16 which does such a multivariate outliers detection resulted in Fig.4.

One smooth specimen which had too much Mahalanobis' distance was excluded from 164 (122 smooth +42 curved) pieces and Table 1 was updated into Table 6 according to the remaining 121 and 42 pieces.

Table 6 (revised Table 1) Data for model development

Feature		14010	(10/1504 14010	Data for mode	l de veropinent		
(dimension)	Curve	Mean	Median	Minimum	Maximum	Range	Std. Dev.
	S	138.34	137.00	101.00	181.0000	80.00	16.99
V (poise)	С	139.35	139.00	101.500	191.0000	89.50	24.69
(poise)	ALL	138.60	137.00	101.000	191.0000	90.00	19.19
CT	S	4.55	4.57	3.3300	5.6800	2.35	0.39443
ST (G)	С	4.78	4.82	2.790	6.8400	4.05	0.87
(0)	ALL	4.61	4.60	2.790	6.8400	4.05	0.56
CNAT	S	312.72	312.80	309.00	315.8000	6.80	1.23
SMT (minute)	С	313.37	313.25	307.70	318.8000	11.10	12.25
(minute)	ALL	312.89	312.90	307.70	318.8000	11.10	11.58
G.C.	S	438.30	438.40	428.00	447.0000	19.00	13.12
SC (minute)	С	439.86	439.45	424.10	453.0000	28.90	15.99
(minute)	ALL	438.70	438.70	424.10	453.0000	28.90	14.09
MT	S	1084.46	1085.50	1061.10	1094.0000	32.90	6.44
MT (centigrade)	С	1084.15	1083.50	1064.20	1109.0000	44.80	8.68
(centigrade)	ALL	1084.38	1084.80	1061.10	1109.0000	47.90	7.05
4.0	S	2.80	2.87	1.84	3.16	1.32	0.26
AG (mesh)	С	2.81	2.80	2.02	3.69	1.67	0.30
(IIIesii)	ALL	2.80	2.84	1.84	3.69	1.85	0.27
TD	S	133.20	133.30	130.20	135.90	5.70	1.90
TD (second)	С	133.47	133.55	131.40	135.40	4.0	1.89
(second)	ALL	133.27	133.30	130.20	135.90	5.70	1.90
	S	7.47	5.10	4	40	36	7.64
Pinhole	С	10.08	7.80	4	29	25	7.63
	ALL	8.144	5.80	4	40	36	7.70

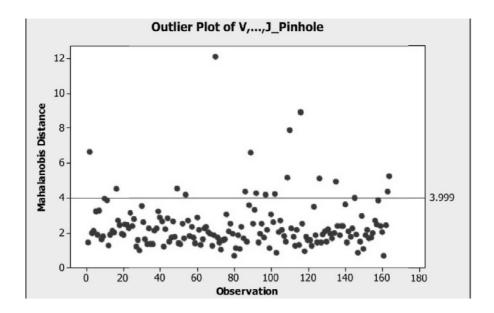


Fig. 4. Mahalanobis interval for the factors causing pinhole defect

3.1.1 The relationship between variables V, ST, SMT, MT, AG, TD and J-pinhole

The scatter plot of J-pinhole versus individual variables as well as scatter plot of every pair of variables are given in the matrix plot shown in Fig. 5. The red cycle have been used for curved specimens and the black cycle for smooth specimens.

As Fig. 5 shows AG & MT, and also SC&SMT are strongly linearly correlated.

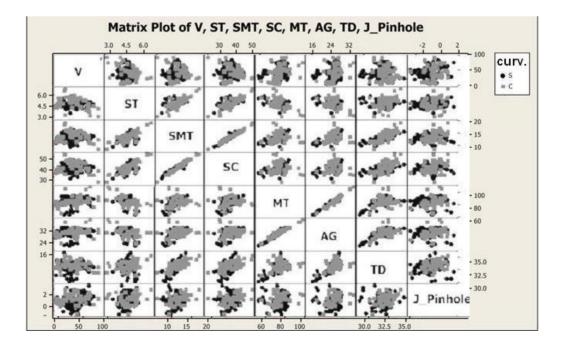


Fig. 5. Matrix plot of V, ST, SMT, SC, MT, AG, TD and J-pinhole



Table 7 shows the correlation coefficient (R) between the J-pinhole and individual variables as well as between each pair of the variables, calculated using SPSS software.

	rable / Correlation coefficients(K)							
Correlations	V	ST	SMT	SC	MT	AG	TD	
ST	-0.176							
SMT	-0.004	0.666						
SC	-0.001	0.733	0.983					
MT	0.263	-0.549	0.227	0.153				
AG	0.219	-0.43	0.376	0.274	0.97			
TD	0.004	0.109	0.667	0.523	0.462	0.658		
J-Pinhole	0.219	0.168	0.26	0.251	0.09	0.135	0.178	

Table 7 Correlation coefficients(R)

3.1.2 Problem Dimension reduction

As the last row of Table 7 shows, J-pinhole has the greatest correlation with SMT and the least correlation with MT. There are several filtering (feature selection) approaches to removing irrelevant data, eliminating redundant features from a set of features and reducing the number of features or variables. Correlation-based Feature Selection (CFS), Principal Component Analysis (PCA), Fast Correlation based Feature selection, Gain Ratio Attribute Evaluation, Chi-square Feature Selection, Fast Information-Gain-Ratio Feature selection, and Markov Blanket Filter are among the feature selection techniques proposed by researchers for feature selection. In this research, CFS and PCA were utilized for finding the principal components of data and reducing the problem dimension.

Some softwares such as MINITAB have the capability of reducing the number of variables of the problem utilizing Principal component analysis (PCA) tool. For the variables causing pinhole defect, MINITAB was used to do the analysis. Table 8 shows the result of the analysis.

Principal Component Analysis on Factors : V, ST, SMT, SC, MT, AG, TD							
Eigen analysis	of the Corr	elation Mat	rix				
Eigen value	3.1892	2.4881	0.9361	0.3745	0.0095	0.0022	0.0005
Proportion	0.456	0.355	0.134	0.053	0.001	0.000	0.000
Cumulative	0.456	0.811	0.945	0.998	1.000	1.000	1.000
Variable	PC1	PC2	PC3	PC4	PC5	PC6	PC7
V	0.066	0.221	-0.953	0.197	-0.001	-0.005	-0.000
ST	0.166	-0.598	-0.134	-0.034	-0.762	0.124	0.016
SMT	0.507	-0.263	-0.046	0.106	-0.279	-0.404	0.647
SC	0.469	-0.316	-0.109	-0.322	0.412	0.252	-0.576
MT	0.330	0.487	0.051	-0.398	-0.199	0.587	0.330
AG	0.406	0.428	0.104	-0.130	-0.364	-0.594	-0.372
TD	0.466	0.068	0.216	0.818	0.013	0.245	-0.040

Table 8 Principal component analysis (PCA)



The first 4 variables i.e. V, ST, SMT, SC were selected using PCA.

The data of V, ST, SMT, SC as well as curvature and J-pinhole data are identified as "PCA data set".

Some softwares, such as WEKA, do CFS study to reduce a problem dimension. Table 9 shows the result of applying this study on our problem.

Table 9 A correlation-based feature selection (CFS)) on factors causing pinholes

=== Run information ===	>>>>>>
	=== Attribute Selection on all input data ===
Evaluator:	•
weka.attributeSelection.CfsSubsetEval	Search Method:
Search: weka.attributeSelection.BestFirst -D	Best first.
1 -N 5	Start set: no attributes
Relation: FINAL-	Search direction: forward
weka.filters.unsupervised.attribute.Remove-R9-10	Stale search after 5 node expansions
Instances: 163	Total number of subsets evaluated: 39
Attributes: 9	Merit of best subset found: 0.287
V	
Curve	Attribute Subset Evaluator (supervised, Class
ST	(numeric): 9 J_Pinhole):
SMT	CFS Subset Evaluator
SC	Including locally predictive attributes
MT	
AG	Selected attributes: 1,2,4 : 3
TD	V
J_Pinhole	Curve
Evaluation mode: evaluate on all training data	SMT

This CFS study selects variables V, SMT as well as curvature as the principal characteristics causing pinhole flaw in the products of Isatis sanitary-ware plant. V, SMT as well as curvature and J-pinhole data are identified as "CFS data set".

3.2 Step 2: Data pre-processing

The other variables are modified according the following relationship:

$$X^* = \frac{X - \min(X)}{\max(X) - \min(X)}$$

Curvature is a an attribute and not a variable. Using the following indicator, we could change our only qualitative attribute in this study i.e. curvature into a variable:

$$X = \begin{cases} 1 & \text{If smooth} \\ 0 & \text{If curved} \end{cases}$$

3.3 Step 3: Choosing right variables for the regressors

In this research neural network and regression modeling are used to predict the number of pinholes in the products.



We have identified 3 sets of data so far: Full set data including V, ST, SMT, SC, MT, AG, TD, curvature and J-pinhole," PCA data set" and "CFS data set". In step 3 we will try to find which set(s) should be chosen for modeling.

Using 3 sets of data, several multi-layer perception (MLP), Radial Basis Functions(RBF), generalized regression neural networks (GRNN) were trained as well as Additive Regression . The efficiency of the model was calculated using the mean squared error(MSE) and also correlation coefficient (R) of the observed set of data and the corresponding set predicted by the model. Table 10 shows the result.

	Table 10 Comparison of the efficiency of different models								
	GF	RNN	MLP		RBF		Additive Regression		
Data set	MSE	R	MSE	R	MSE	R	MSE	R	
Full	0.80835	0.289185	1.165752	0.2344	1.055551	0.0402	1.006812	0.3343	
PCA	0.78939	0.29601	0.041047	0.2586	0.037018	0.1412	0.043765	0.1737	
CFS	0.52889	0.316223	1.12169281	0.205	1.061724	0.0308	0.975551	0.3262	

Table 10 shows that the RBF neural networks used for the research produced poor correlation coefficient; therefore it was excluded.

Figure 6 shows the coefficient of variation between observed and predicted pinhole data using different regressor and different inputs. The PCA and CFS sets of data produced better results compared to the full set, as evident from MSE and R indices.

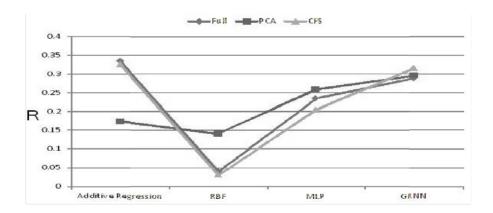


Fig. 6. Correlation coefficient for different repressors using different input sets

More study lead to choosing MLP and GRNN networks as well as Additive Regression with the following inputs for entering the next step.

Table 11 Inputs suitable for the modeling tools

Tueste II impute suitueste for the mouening teens						
regressor	Input data set					
	CFS	PCA				
MLP	×	$\overline{\checkmark}$				
Additive regression		\square				
GRNN		×				

3.4 Step 4: Training

MATLAB was used to train GRNN. MLP was trained with WEKA. Additive regression was applied by WEKA. To train the regressor networks each data set were divided into two subsets i.e. a subset for training and a subset for testing the regressor with the proportion of 2 to 1. The efficiency of the 3 modeling tools was determined by R and MSE as shown in Table 12 and figures 7&8.

Table 12 Efficiency of the 3 modeling tool

	MSE	,	R(%)		
	training	test	training	test	
MLP (PCA)	0.731367	0.975946	57.68	42.47	
Additive regression					
(PCA)	0.569119	1.197711	67.79	36.90	
Additive regression					
(CFS)	0.912579	0.957601	58.49	0.49.75	
GRNN (CFS)	0.246	0.9119	88	20	

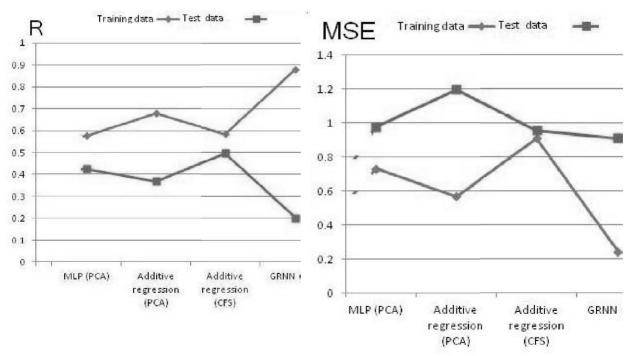


Fig 7. Correlation coefficient of observed and predicted data for different regressors

Fig 8. Mean squared error of observed and predicted data for different regressors



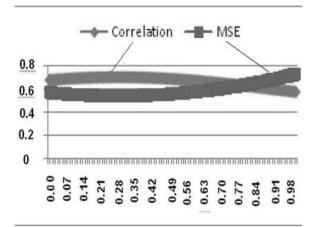
GRNN correlation coefficient for the training data is high, while this index for test data is low; which might be due to over-fitting. This inference could also be made from evaluating the MSE for the training and the test data sets. This observation lead in the exclusion of the GRNN network. Although one could make a similar argument for Additive Regression (with PCA data set as input); but we do not exclude it because the way it has dealt with the test data is not that different from the other methods.

3.5 Combination of the regressors

In this phase of step 4, the weighted average of the results of each two different regressors is calculated and the pair with the better R & MSE is determined. Various weights were tested. Figures 9 and 10 are the plots for showing how efficiency varies with the weight for one combination i.e.

"MLP(PCA)+Additive Regression (PCA)" as an example.

The best MSE occurs at weight=0.28 for the training data and weight=0.76 for the test data. The best R occurs at weight=0.28 for the training data and weight=0.66 for the test data.



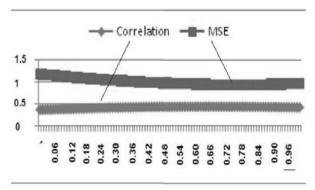


Fig. 9. The efficiency versus weight for "MLP+Additive regression" (PCA)-training data

Fig. 10. The efficiency versus weight for "MLP+Additive regression" (PCA)-test data

Table 13 shows the result of identifying the weights with the best efficiency based on R and MSE, for 3 different combinations.



Table 13 The efficiency of combined regressors *

		R(%))	weight		MSE		weight	
	bined essors	training	test	training	test	training	test	training	test
Additive Regressi on (PCA)	MLP (PCA)	70.19	44.07	0.28	0.66	0.5407454 41	0.952535	0.28	0.76
Additive Regressi on (CFS)	MLP (PCA)	63.13	50.72	0.40	0.20	0.6348606	0.839146	0.44	0.07
Additive Regressi on (CFS)	Additive Regressio n (PCA)	70.14	47.26	0.64	0.55	0.5538054 9	0.795623	0.75	0.73

Figure 11 compares R for the 3 combinations.

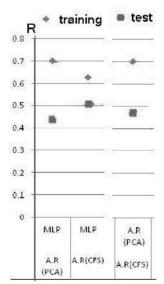


Fig. 11 Correlation coefficient of the observed and predicted data for combination of regressors

Our criteria for choosing the suitable combination is having relative high efficiency based on R & MSE and the closeness of the R & MSE for training data set with those for the test data set. This lead us in choosing the combination of MLP and the additive regression with the input obtained from CFS analysis, which has the best results among the combinations.

Table 14 shows that the efficiency of the combination of the 2 regressors is better than the efficiency of the individuals.



Table 14 Comparison of the chosen combination and the components

Tuble 11 Comparison of the chosen combination and the components							
	MSE		R (%)				
	training	test	training	test			
Additive regression (CFS)							
+	0.63486065	0.839146	63.13	50.72			
MLP (PCA)							
MLP (PCA)	0.731367	0.975946	57.68	42.47			
Additive regression (CFS)	0.912579	0.957601	58.49	49.75			

According to the result of CFS analysis V,SMT as well as curvature have the most influence on the number of pinholes and according to the PCA analysis V, ST, SMT, SC as well as curvature are the most influential variables.

Based on a sensitivity analysis SMT is the most influential variable affecting the number of pinholes.

Conclusions

This research shows that

- 1) In the production process of sanitary-ware products at Isatis sanitary porcelain plant, Yazd, Iran, Glaze viscosity (V) and the speed of reaching the maximum temperature (SMT) as well as curvature (as opposed to smoothness of the product) and also the surface tension of raw material (ST) and glaze cooling speed (SC) are the most influential characteristics affecting the number of pinholes occurring in the finished product of the plant.
- 2) Multilayer perception neural networks and additive regression proved to be efficient in predicting the number of pinholes and thereby the rating of the product. Trial and error with giving different values for the input variables of these models could yield a design the production design experiment which could result in low wastes and reduction of costs.

For future research, other factors (other than V, ST, SMT, MT, AG & TD as well as curvature) might be studied and other modeling tools such as other neural networks might be tested.

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