

# Study on Control Strategy for Regenerative Braking in a Pure Electric Vehicle

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**Abstract:** Regenerative braking is one of the important ways to extend the driving mileage of pure electric vehicle. Through analyzing the brake regulations and the vehicle dynamics, a control strategy was proposed to solve the problem on braking force distribution for the pure electric vehicle. The rate of regenerative braking<sup>[1]</sup>, the rate of energy-saving and the rate of extended driving mileage were served as evaluating indexes of the control strategy. Finally the simulation was carried out by MATLAB/simulink and AVL-Cruise under different profiles. The control strategy was also validated by vehicle experiment. The results show that the strategy can distribute the brake forces rightly and recover relatively more energy.

## Introduction

With the increasing shortage of petroleum, new energy vehicle has become an important theme in the auto industry<sup>[2]</sup>. Regenerative braking is one of major technologies to save energy and reduce emission for hybrid electric vehicle, pure electric vehicle and fuel-cell electric vehicle. This paper put forward a regenerative braking control strategy which can distribute the force under braking regulations. At last the strategy was validated by simulation and vehicle experiment.

## Design of regenerative braking strategy

According to the automobile theory, the following definitions (1) and (2) were given<sup>[3]</sup>:

$$\varphi_f = \frac{\beta z}{\frac{1}{L}(b+zh_g)} \quad (1)$$

$$\varphi_r = \frac{(1-\beta)z}{\frac{1}{L}(a-zh_g)} \quad (2)$$

Where:

$\varphi_f$ —Front axle utilized road friction coefficient

$\varphi_r$ —Rear axle utilized road friction coefficient

$\beta$ —Braking force distribution coefficient

$z$ —Severity of braking

$L$ —Wheel base

$a$ —Distance between center of gravity and front axle

$b$ —Distance between center of gravity and rear axle

$h_g$ —Height of center of gravity

Based on the ECE regulations, the following inequality (3) was derived:

$$\begin{cases} \varphi_f > \varphi_r \\ z \geq 0.1 + 0.85(\varphi_f - 0.2) \\ z \geq 0.1 + 0.85(\varphi_r - 0.2) \end{cases} \quad (3)$$

After calculating the inequalities by MATLAB, the relation curve between braking force distribution rate ( $\beta$ ) and severity of braking ( $z$ ) can be received, as figure.1 shows. From figure.1 we can come to a conclusion that when  $z < 0.13$ , front axle is permitted to generate the whole vehicle brake force. At the same time, the demands of regulations are always fulfilled by making  $\beta = 0.7$ . So the strategy of braking force distribution is shown in figure.2.

In figure.2, the horizontal axis is for the total brake force of front axle and the vertical axis is for the total braking force of rear axle, and the following observations can be obtained:

- ① When  $z < 0.13$ , braking force distribution rate  $\beta$  is equal to 1. As the adhesion coefficient of ice-snow road is 0.15~0.25, the front wheel will not be locked at this time and the vehicle stability will also be maintained. If possible all of the front axle braking force will be supplied by motor;
- ② When  $0.13 < z < 0.2$ , the increase of the front axle braking force will break the regulation, so the rear axle braking force will increase with the front axle force remaining unchanged;
- ③ When  $0.2 < z < 0.81$ , to guarantee the consistency of driver braking feel and the demand of brake regulations, the braking force distribution rate  $\beta$  is set to 0.7;
- ④ When  $z > 0.81$ , the wheel has great possibility to be locked. Considering the vehicle safety, the regenerative braking will quit<sup>[4]</sup>. If ABS works, the actual braking force distribution curve will go along the ideal braking force distribution curve.

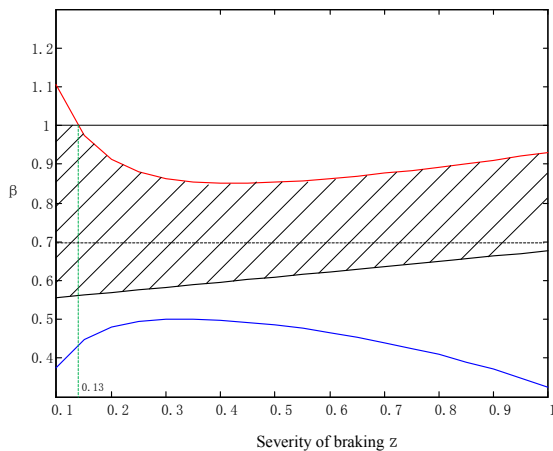


Figure.1 Demand of regulation

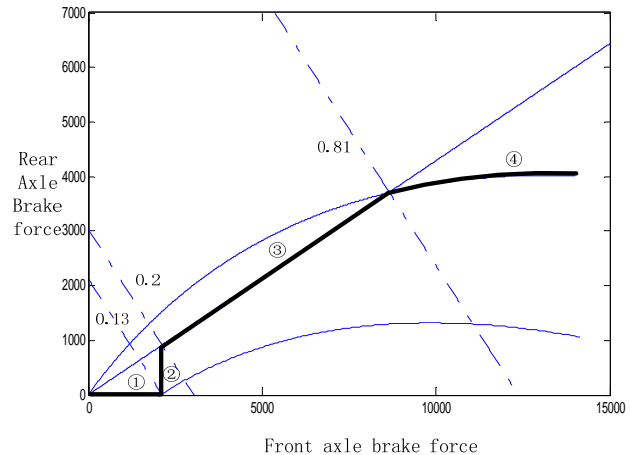


Figure.2 Brake force distribution

The process diagram of the strategy was shown in figure.3.

## Simulation

**Evaluating index.** In order to evaluate the amount of recovered energy, this paper verified the strategy by three evaluating indexes, namely rate of regenerative braking, rate of energy-saving and rate of extended driving mileage.

Where:

Rate of regenerative braking is derived from energy recovered by battery divided by brake kinetic energy

Rate of energy-saving is derived from energy recovered by battery divided by dissipated energy

Rate of extended driving mileage is derived from the difference between mileage with regenerative brake and mileage without regenerative brake, divided by mileage without regenerative brake.

**Simulation result.** The model was simulated on MATLAB/Simulink and AVL-Cruise<sup>[5]</sup>. Part of the simulation parameters can be seen in table 1. In the simulation, three profiles: NEDC, Jap-1015 and Jap-08 were used. The result was shown in table 2.

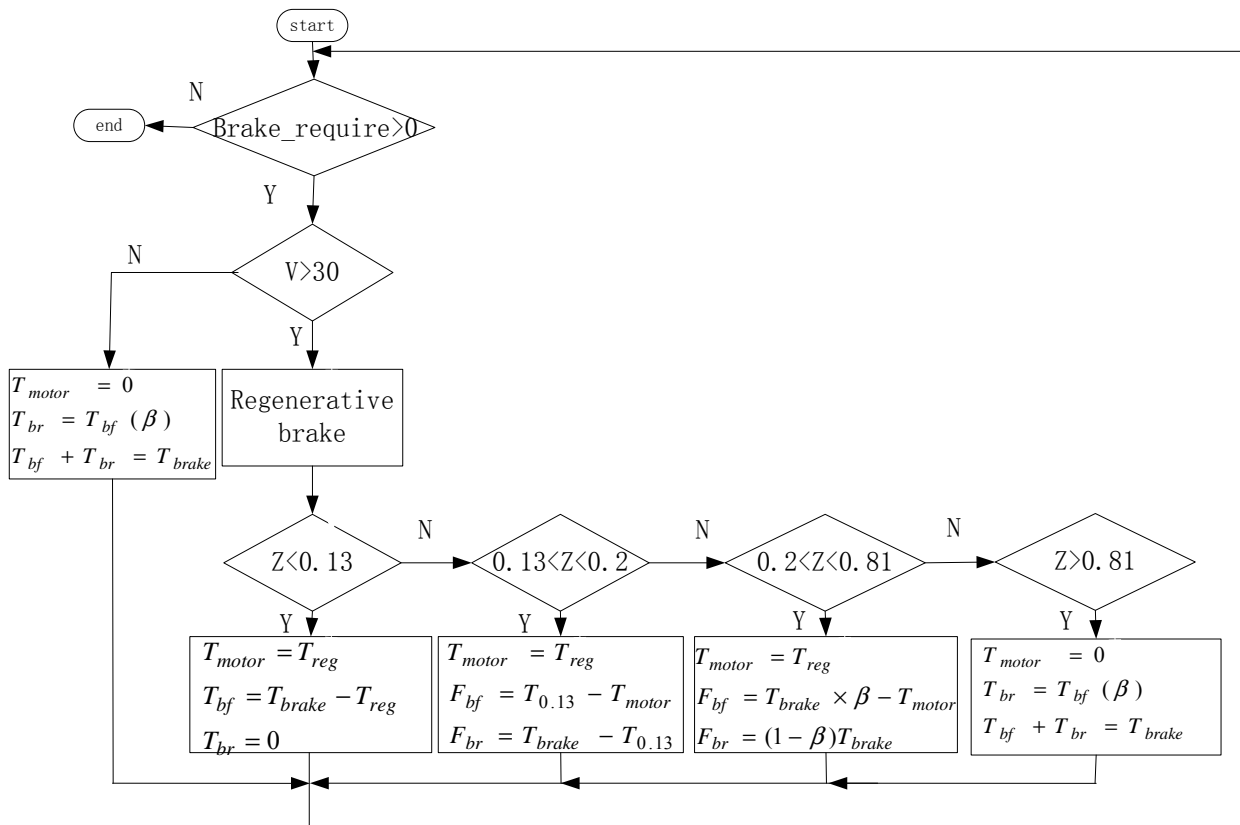


Figure.3 Process diagram of the strategy

Table 1 Part of the simulation parameters

parameter	value
Curb weight [M/kg]	1554
Rolling resistance coefficient	0.01
Frontal area [m <sup>2</sup> ]	1.98
Drag coefficient	0.30
Air density [kg/m <sup>3</sup> ]	1.23
Correction coefficient of rotating mass	1.03

Table 2 Simulation result

index \ profile	Jap-1015	Jap-08	NEDC
Rate of regenerative braking	62.69%	62.96%	56.33%
Rate of energy-saving	49.20%	46.99%	21.04%
Rate of extended driving mileage	59.30%	31.64%	16.84%
Energy recovered by battery[KJ]	18374	19465	12998
Brake kinetic energy[KJ]	29309	30916	23073
Energy dissipated	37346	41425	61775
Mileage with regenerative brake[km]	94.89023	86.97827	115.11859
Mileage without regenerative brake[km]	59.5670	66.07283	98.53022

According to the simulation result, the amount of regenerative braking recovered energy is related to the profile. However the strategy proposed in this paper can reach satisfactory indexes in every single profile.

### Vehicle validation

The strategy was put into an electric car which didn't have regenerative braking strategy. The car was tested on the chassis dynamometer. The tested profile was NEDC. The result was in figure 4, figure 5 and table 3.

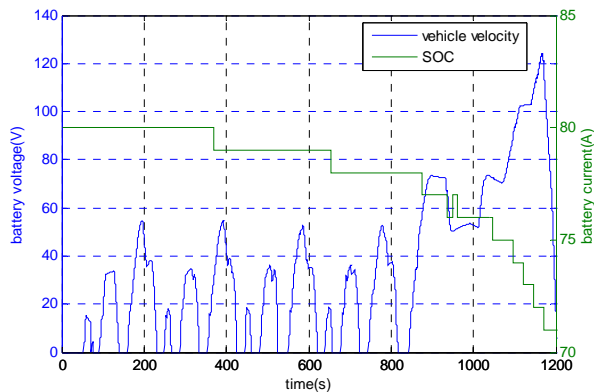


Figure.4 Vehicle velocity and SOC

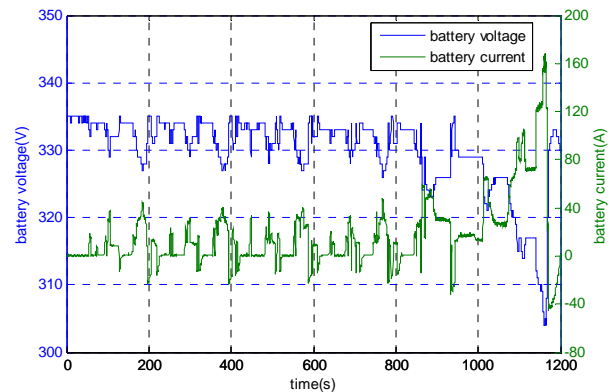


Figure.5 Battery voltage and current

Table 3 Vehicle verification result

Index	Rate of regenerative braking	Rate of energy-saving	Rate of extend driving mileage
value	41.60%	10.62%	8.31%

According to the result, in vehicle test the strategy can still realize the function of regenerative braking.

## Conclusion

This paper puts forward a control strategy for regenerative braking. The strategy is validated by software simulation and vehicle test. The combined simulation platform is based on MATLAB/Simulink and AVL-Cruise. The vehicle test is implemented on the chassis dynamometer. Three evaluating indexes are used to evaluate the energy-saving effect of the proposed strategy, which are the rate of regenerative braking, the rate of energy-saving and the rate of extended driving mileage. The results show that the strategy is feasible and can get satisfactory indexes.

## Acknowledgment

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