## The Impact of Residual Stress Relaxation on Fatigue Life Enhancing Effect of Cold Expansion

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**Abstract.** A numerical analysis was performed, using three-dimensional finite element method to assess the impact of residual stress relaxation on the fatigue strength benefit of cold expansion. Fatigue lives of cold expansion hole made from aluminium alloy 7050-T7451 under different relaxation time are presented, the results reveal that the fatigue life enhancing ratio is inversely proportional to the stress relaxation time, residual stress relaxation can weaken the benefit of cold expansion strongly.

#### Introduction

Mechanical joints are used extensively in aircraft structures. However, these connections are inherently vulnerable to fatigue because the stress concentration around fastener holes, statistics show that fatigue fracture of fastener holes account for 70% in aircraft structures failure [1]. To improve fatigue life of fastener holes, in the 1970s, one technique named as cold expansion was presented by Boeing Company and been widely used in the last decades. Fatigue life improvement is attributed to the presence of residual compressive stress induced by cold expansion as the residual stress can reduce stress concentration effectively at hole edge, the benefits of cold expansion have been well documented in previous studies [2~5].

Generally, the desired service life of many aircraft structures beyond twenty years, for these applications, residual stress relaxation in room temperature become a significant factor in limiting the beneficial effects of cold expansion. To determine residual stress variation, one method is to use a fracture mechanics approach [6], this method is practical but obtain only the average value of residual stress in observation area.

A more popular method of calculating residual stresses is numerically using finite element analysis [7~9]. This paper describes how finite element analysis has been carried out to establish the residual circumferential stress relaxation around a cold expanded hole made from aluminium alloy 7050-T7451; fatigue lives under different relaxation time are presented to study the impact of residual stress relaxation on fatigue life enhancing effect of cold expansion also.

#### Material properties and finite element model

Split sleeve cold expansion is adopted. Specimen was made from aluminium alloy 7050-T7451, the yield strength  $\sigma_y$ =460MPa, tensile strength  $\sigma_b$ =530MPa, and fatigue limit  $\sigma_f$ =142MPa at room temperature, respectively, the Young's modulus and Poisson's ratio were measured to be 71 GPa and 0.33 [10]. For the steel sleeve and mandrel a linear elastic material relationship was assumed with Young's modulus of 210 GPa and Poisson's ratio of 0.3.

A 3-D finite element model was used to simulate the process of split sleeve cold expansion, stress relaxation and fatigue. Only one eighth of specimen and half of mandrel were needed in the simulation due to their symmetry with respect to the X–Y, X–Z and Y–Z planes, 8-node linear brick reduced integration element (C3D8R) was used. In addition, two sets of contact elements were used between the sleeve and the plate, the sleeve and the mandrel. In FEA model, the plate is 80mm long×17.5mm wide×2mm thick, the hole diameter is 4.51mm, the split sleeve outer diameter is

4.10mm and inner diameter is 3.70mm, the mandrel diameter is 4.40mm with 6.43% interference. All analysis was carried out by the finite element package ABAQUS 6.10.

The finite element model is presented in Fig.1.



Fig.1 3-D finite element model

## Numerical simulation method

The whole calculation steps are given in Fig.2.



Fig.2 Illustration of calculation steps

The residual stress relaxation can be obtained by calculating creep strain [9]. For room temperature creep under low stress, the power-law model for creep strain is

$$\dot{\widetilde{\varepsilon}}_{cr} = A\widetilde{\sigma}^n t^m$$

(1)

Where,  $\tilde{\varepsilon}_{cr}$  is the uniaxial equivalent creep strain rate;  $\tilde{\sigma}$  is the mises equivalent stress, t is the total creep time, A, n, and m are material constants depend on temperature, for aluminium alloy 7050-T7451

$$A = 2.7437 \times 10^{-19}, n = 6, m = -0.1471$$

(2) In this paper, Select stress ampltitude  $S_a$ =150Mpa, stress ratio R=-1, 0.06 for calculating fatigue life, a corrected damage law for high cycle fatigue is used for calculating fatigue life [11~12].

## **Results and discussions**

Fig.3 shows the animation process of cold expansion.



Fig.3 Process of cold expansion

Fig.4 shows how the residual circumferential stress(along X-axis) distribution change with time around hole edge.



Fig.4 Residual circumferential stress distribution after different years The residual circumferential stress along path-1 in different time is presented in Fig.5.



Fig.5 Residual circumferential stress distribution along path-1

The residual circumferential stress distribution in fatigue loading and failure elements are shown in Fig.6. The FE simulation shows that the maximum longitudinal stress occurring a distance away from the hole edge, the fact that fatigue cracks initiated and propagated from the hole edge suggest that the effect of residual stress is not enough to eliminate the stress concentration around hole edge.



Fig.6 Illustration for fatigue life calculation

Tab.1 indicates the fatigue lives under different loading situations.

Ta	ab.1 Com	parison	between	fatigue	lives	under	differer	nt loading	situ	ations

stress ampltitude (MPa)	Stress ratio	Cold expansion	Relaxation time (year)	Fatigue life	life enhancing ratio
150	-1	No	/	69500	1.00
		Yes	0	585000	8.42
		Yes	1	345000	4.96
		Yes	5	267500	3.85
		Yes	10	192500	2.77
		Yes	20	142500	2.05

		No	/	82500	1.00
		Yes	0	660000	8.00
150	0.06	Yes	1	385000	4.67
		Yes	5	297500	3.61
		Yes	10	222500	2.70
		Yes	20	175000	2.12

According to the results presented in Tab.1, it can be indicate that the benefit of cold expansion was weakened strongly by residual stress relaxation, the fatigue life enhancing ratio reduce one half within the first year as the residual circumferential stress at hole edge decreased from -160MPa to -96MPa at the same time.

Fatigue life enhancing ratio reduced to 2.05(2.12) after 20 years, which was equal to 25% of its initial value only. The results revealed that the influence of residual stress relaxation on fatigue life enhancing effect of cold expansion the can be significant also.

#### Conclusions

(1) A 3-D finite element model was established to simulate the process of split sleeve cold expansion, stress relaxation and fatigue, fatigue lives under different situations are calculated.

(2) The FE simulation results show that the fatigue life enhancing ratio is inversely proportional to the stress relaxation time, the fatigue life enhancing ratio equivalent to 25% of its initial value after 20 years. The results reveal that the impact of residual stress relaxation on fatigue life enhancing effect of cold expansion is significant, which should be considered in application.

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