

An Improved Shuffled Frog Leaping Algorithm with Comprehensive Learning for Continuous Optimization

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Abstract—This paper presents a shuffled frog leaping algorithm (SFLA) with comprehensive learning strategy (SFLA-CL) for global optimization. This algorithm uses a novel learning strategy whereby all other frogs' information of the memplex is used to update the worst frog's position. The strategy enables the diversity of the memplex to be preserved to discourage premature convergence. SFLA-CL also introduces a new search learning coefficient into the formulation of the original SFLA to enhance the convergence performance of SFLA. SFLA-CL has been evaluated, in comparison with existing evolutionary algorithm, such as SFLA, particle swarm optimization (PSO) and fast evolutionary programming (FEP), on five mathematical benchmark functions. Experimental results demonstrate that the SFLA-CL performs much better than SFLA, PSO, and FEP in optimizing these benchmark functions, particularly, in terms of its convergence rates and robustness.

Keywords—Evolutionary computation; Shuffled frog leaping algorithm; Comprehensive learning strategy; Particle swarm optimization; Continuous Optimization

I. INTRODUCTION

Shuffled frog-leaping algorithm (SFLA) is originally developed by M. Eusuff and K. Lansey in 2003^[1]. It combines the advantages of the genetic-based memetic algorithm (MA) and the social behavior-based particle swarm optimization (PSO)^[2]. Recently, there have been a few papers that have reported results of the application of SFLA to various problems^[3-7], ranging from the classical combinatorial optimization problem, such as the Travelling Salesman Problem (TSP), to speaker recognition, assembly line sequencing, water distribution network design and reactive power dispatch. The SFLA, in its original form, is easy to implement and has been empirically shown to perform well on unconstrained problems, but detailed analysis and suitable revisions are still needed to further explore its potential.

In this paper, we propose a shuffled frog leaping Algorithm with comprehensive learning strategy (SFLA-CL). In order to improve SFLA performance on complex continuous optimization problems, we apply a new learning strategy which is involved comprehensive learning PSO^[8]. Instead of using the frog with the best fitness as the exemplars, all frogs' information of the memplex can potentially be used as the exemplars to guide the frog with the worst fitness leaping direction. Instead of learning from the same exemplar frog for all dimensions, each dimension

of the worst frog in general can learn from different frog for different dimensions. In other words, each dimension of the worst frog may learn from the corresponding dimension of different frog. To further improve the search ability of SFLA, the frog's leaping step size is adjusted by adding a search learning coefficient that pull the worst frog toward to speed up convergence. To demonstrate the merits of SFLA-CL, we have evaluated it on five mathematical benchmark functions which cover a range of optimization problems from unimodal and multi-modal to high dimensions. The algorithm evaluation has been undertaken in comparison with SFLA, PSO and fast evolutionary programming (FEP)^[9]. The proposed algorithm is shown to be more superior in performance. Its strong global exploration ability makes its convergence speed very fast, and at the same time it is able to escape from local optima to obtain the global optimum.

II. SHUFFLED FROG LEAPING ALGORITHM

In SFLA, there is a population of possible solutions defined by a set of frogs (solutions) that is divided into different subgroups called memplexes, each performing a local search. Within each memplex, the individual frogs hold ideas that can be affected by the ideas of other frogs. After a defined number of memetic evolution steps, ideas are passed among memplexes in a shuffling process. The local search and the shuffling process continue until defined convergence criteria are satisfied.

In a D -dimension target searching space, generate randomly P frogs (solution) to compose initial population. The i th frog represents the solution of the problem $X_i = (X_{i1}, X_{i2}, \dots, X_{iD})$. Frogs are sorted in a descending order based on their fitness. Afterwards, the frogs are separated into m memplexes, each containing n frogs (i.e. $P=m \times n$). In this procedure, the first frog is distributed to the first memplex, the second frog to the second memplex, the m th frog to the m th memplex, and the $(m + 1)$ th frog to the first memplex and so on.

In each memplex, the frogs with the best and worst fitness are determined as X_b and X_w , respectively. Also, the frog with the global best fitness among the memplexes is determined as X_g . Then, a process is applied to improve only the frog with the worst fitness X_w (not all frogs) in each cycle. Accordingly, each frog updates its position to catch up with the best frog as follows:

Frog leaping step update:

$$D_i = rand() \cdot (X_b - X_w) \quad (-D_{max} \leq D_i \leq D_{max})!$$

Position update:

$$\cdot \text{new } X_w = X_w + D_i \cdot$$

Where $rand()$ is a random number between 0 and 1; D_{max} represents the maximum of update step allowed. If this process produces a better solution, it replaces X_w . Otherwise, X_b of (1) is changed to X_g and adapted to (1).

$$\cdot D_i = rand() \cdot (X_g - X_w) \quad (-D_{max} \leq D_i \leq D_{max}) \cdot$$

If the fitness of new X_w still hasn't been improved, a new X_w will be generated randomly.

$$\cdot \text{new } X_w = rand() \cdot (X_{max} - X_{min}) + X_{min} \cdot$$

Repeat this update operation until satisfying the update number.

After the local area deep-searching of all memplex have been finished, to ensure global exploration, the whole memplexes are mixed in the shuffling process. The local search and the shuffling continue until convergence criteria are satisfied.

III. SHUFFLED FROG LEAPING ALGORITHM WITH COMPREHENSIVE LEARNING

SFLA-CL uses a novel learning strategy whereby all other frogs' information of the memplex is used to update the worst frog's position. This strategy enables the diversity of the memplex to be preserved to discourage premature convergence. SFLA-CL also introduces a new search learning coefficient into the formulation of the original SFLA to pull the worst frog toward to speed up convergence.

A. Comprehensive Learning Strategy

In the original SFLA, the worst frog X_w learns from the best frog X_b in each memplex or the global best frog X_g . However, because the worst frog X_w learns from the best frog X_b even if the current is far from the global optimum, frogs may easily be attracted to the region and get trapped in a local optimum if the search environment is complex with numerous local solutions. Liang proposed comprehensive learning strategy to improve the original PSO [8]. In [8], all particles' are used to update the velocity of any one particle. This novel strategy ensures that the diversity of the swarm is preserved to discourage premature convergence. In order to make better use of the beneficial information, we propose a new learning strategy to improve the original SFLA based on [8].

In this new learning strategy, equation (2) can be modified as (5).

$$\cdot D_{ij} = rand() \cdot [X_{s(j)} - X_{wj}] \quad (-D_{maxj} \leq D_{ij} \leq D_{maxj}) \quad (5)$$

Where $s = [s(1), s(2), \dots, s(D)]$ defines which the worst frog X_w should follow. $X_{s(j)}$ can be the corresponding dimension of any frog's position including X_b . We employ

the tournament selection procedure when the frog's dimension X_w learns from another frog's as follows.

1) We first randomly choose two frogs out of the memplex.

2) We compare the fitness of these two frogs and select the better one.

3) We use the winner as the exemplar to learn from for that dimension. The details of choosing are given in Fig. 1.

All these $X_{s(j)}$ can generate new positions in the search space using the information derived from different frogs' positions. To ensure that the worst frog learns from good exemplars and to minimize the time wasted on poor directions, we allow the worst frog to learn from the exemplars. We observe two main differences between the SFLA-CL and the original SFLA.

1) Instead of using memplex' X_b and as the exemplars, all frogs' information can potentially be used as the exemplars to guide the worst frog's leaping direction.

2) Instead of learning from the same exemplar frog for all dimensions, each dimension of the worst frog in general can learn from different frog for different dimensions. In other words, each dimension of the worst frog may learn from the corresponding dimension of different frog.

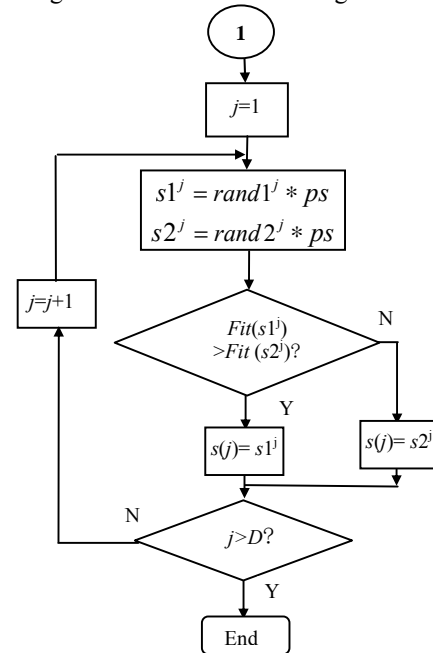


Figure 1. Selection of exemplar dimensions for the frog with worst fitness.

B. Search learning coefficient

In the original SFLA, restricting the frog with worst fitness to jump toward X_b or X_g with a random number between 0 and 1 makes SFLA converge slow. In order to make SFLA converge faster, equation (5) can be modified as (6), and equation (3) can be modified as (7).

$$\cdot D_{ij} = C \cdot rand() \cdot [X_{s(j)} - X_{wj}] \quad (-D_{maxj} \leq D_{ij} \leq D_{maxj}) \quad (6)$$

$$D_i = C \cdot rand() \cdot (X_g - X_w) \quad (-D_{max} \leq D_i \leq D_{max}) \quad (7)$$

where C is a search learning coefficient. It is constant greater than 1 that represents the searching scale for frogs' leaping step size. It is obvious that C cannot be set too large; otherwise, the local search tends to be lost in the random search with little improvement or even cause premature convergence.

IV. EXPERIMENTS AND RESULTS

A. The benchmark functions

In order to evaluate the performance of SFLA-CL, five widely used benchmark continuous functions selected from [9], are listed below.

Sphere's Function:

$$f_1(\mathbf{x}) = \sum_{i=1}^{30} x_i^2$$

where $x \in [-100, 100]^{30}$

Generalized Rosenbrock's Function:

$$f_2(\mathbf{x}) = \sum_{i=1}^{29} [100(x_{i+1} - x_i^2)^2 + (x_i - 1)^2]$$

where $x \in [-2.048, 2.048]^{30}$

Generalized Rastrigin's Function:

$$f_3(\mathbf{x}) = \sum_{i=1}^{30} [x_i^2 - 10 \cos(2\pi x_i) + 10]$$

where $x \in [-5.12, 5.12]^{30}$

Ackley's Function:

$$f_4(\mathbf{x}) = -20 \exp\left(-0.2 \sqrt{\frac{1}{30} \sum_{i=1}^{30} x_i^2}\right) - \exp\left(\frac{1}{30} \sum_{i=1}^{30} \cos 2\pi x_i\right) + 20 + e$$

where $x \in [-32, 32]^{30}$

Griewank's Function:

$$f_5(\mathbf{x}) = \frac{1}{4000} \sum_{i=1}^{30} x_i^2 - \prod_{i=1}^{30} \cos\left(\frac{x_i}{\sqrt{i}}\right) + 1$$

where $x \in [-600, 600]^{30}$

In the experiment studies, SFLA-CL is evaluated on the benchmark functions in comparison with SFLA, PSO with constriction factors (PSO-cf)^[10], and FEP. Here, the evaluation number of an objective function in each algorithm is adopted for comparison purpose. The total evaluation number for each algorithm, taken in a complete optimization process, is 200,000.

B. Initialisation parameters setting

For the shuffled frog-leaping algorithm, we follow the parameter settings in [11]. There are 20 memplexes, each containing 10 frogs. The local exploration in each memplex is executed for 10 iterations. The parameters settings for SFLA-CL are the same as those of SFLA, with Search learning coefficient C equal to 1.5, which is was obtained through trial. For the PSO-cf, the cognitive and social scaling parameters, i.e., c_1 and c_2 , are both equal to 1.4962; the inertia weight w is 0.7298; and the population size is set to 40. For the FEP, we follow the parameter settings in [9].

C. Experimental results

SFLA-CL, SFLA, FEP and PSO-cf are used to optimize the benchmark functions respectively. Each algorithm ran 50 times to give a mean value of the best solutions and a standard deviation obtained from the 50 runs. Table I demonstrates the results obtained by four algorithms applied on the five benchmark functions respectively. From Table I, it can be seen clearly that SFLA-CL can provide a better optimization solution with a much smaller deviation for three out of five benchmark functions, encompassing both uni-modal and multi-modal problems with high dimensions. The merits and characteristics of SFLA-CL are discussed in comparison with SFLA, FEP and PSO-cf as follows.

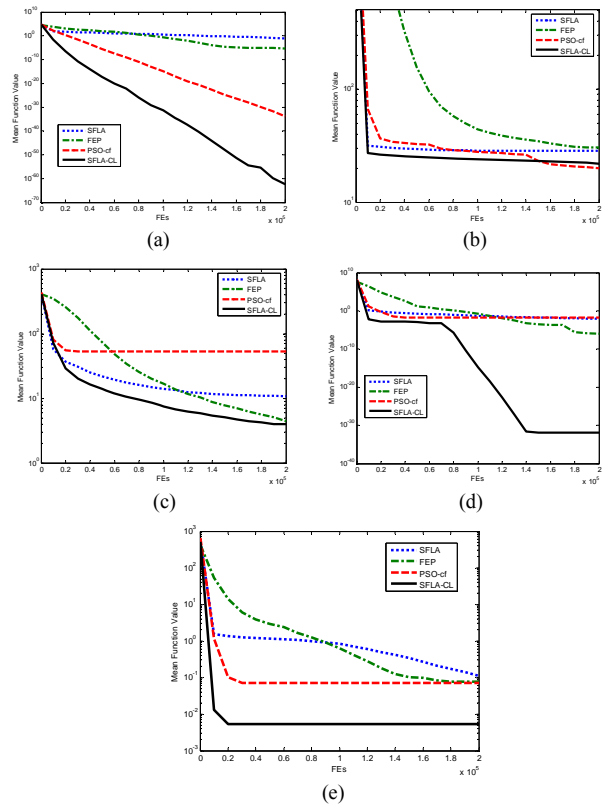


Figure 2. The median convergence characteristics of test functions. (a) Sphere function. (b) Rosenbrock's function. (c) Rastrigin's function. (d) Ackley's function. (e) Griewank's function.

1) Convergence

Figures 2 show the convergence process of SFLA-CL, SFLA, FEP and PSO-cf respectively, conducted on the five benchmark functions. For a comparison purpose, we use the number of evaluations to plot the convergence performance of the four algorithms. All the figures illustrate the average best fitness in a population obtained from 50 runs of the program, which is plotted using a logarithmic scale in order to reduce the biggest and smallest values in the whole optimization process.

SFLA-CL has also demonstrated a better ability of global searching for functions Sphere, Rastrigin, Ackley and Griewank. SFLA-CL performs almost as well as PSO-cf in

Rosenbrock. From the results presented in Table I, it can be seen that SFLA-CL performs the best in average for most of the benchmark functions. This is because that, the comprehensive learning and search learning coefficient of SFLA-CL enables its capability of searching global optimum in multi-modal continuous functions.

2) *Robustness*

In most of evolutionary algorithms (EAs), the algorithm robustness is a crucial issue, as EAs are based on stochastic research and random selections. Although the sensitivity to the initial positions and the instability in different functions have been noted during the course of the experiment studies, the experimental results show that the standard deviations obtained, for most of benchmark functions, by SFLA-CL are smaller than those obtained by SFLA, FEP and PSO-cf.

V. CONCLUSIONS

The novel SFLA-CL algorithm has been developed to improve the stability and global search ability for high-dimensional continuous function optimization. In this algorithm, a novel learning strategy whereby all other frogs' information of the memplex is used to update the worst frog's position. This strategy enables the diversity of the memplex to be preserved to discourage premature convergence. And the frog's leaping step size is adjusted by adding a search learning coefficient that pulls the worst frog toward to speed up convergence. SFLA-CL has been evaluated on five benchmark problems, which include uni-modal and multi-modal functions in high dimension domains. The convergence rates and robustness of SFLA-CL have been well discussed in this paper. The experimental results have shown that SFLA-CL has superior performance in comparison with SFLA, FEP and PSO. Through the SFLA-CL experiment studies, it has been seen that SFLA-CL possesses a great potential for global optimization of complex problems.

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TABLE I. COMPARISON RESULTS FOR FEP, PSO-CF, SFLA, AND SFLA-CL

Function	FEP Mean Best ± Std Dev	PSO-cf Mean Best ± Std Dev	SFLA Mean Best ± Std Dev	SFLA-CL Mean Best ± Std Dev
Sphere	5.84e-06±2.13e-06	1.73e-34±9.56e-34	8.79e-02±1.04e-01	4.20e-63±2.94e-62
Rosenbrock	3.03e+01±1.77e+01	1.99e+01±1.36e+01	2.84e+01±2.37e-01	2.20e+01±1.64e-01
Rastrigin	4.44e+00±2.78e+00	5.25e+01±1.72e+01	1.07e+01±3.98e+00	7.87e+00±3.67e+00
Ackley	9.87e-07±5.71e-07	1.49e-02±3.74e-02	8.85e-03±9.51e-03	1.35e-32±2.74e-48
Griewank	7.79e-02±1.19e-01	1.49e-02±3.74e-02	1.09e-01±8.19e-02	5.53e-03±7.06-03