

# Research on Image Feature Extraction Method Based on Orthogonal Projection Transformation of Multi-task Learning Technology

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**Abstract**—When the number of labeled training samples is very small, the sample information we can use would be very little. Because of this, the recognition rates of some traditional image recognition methods are not satisfactory. In order to use some related information that always exist in other databases, which is helpful to feature extraction and can improve the recognition rates, we apply multi-task learning to feature extraction of images. Our researches are based on transferring the projection transformation. Our experiments results on the public AR, FERET and CAS-PEAL databases demonstrate that the proposed approaches are more effective than the general related feature extraction methods in classification performance.

**Keywords**—multi-task learning; projection transformation; feature extraction; face recognition

## I. INTRODUCTION

The performance of single task for classification cannot meet our requirement when the number of labeled training samples is very small. When there are relations between the tasks to learn, it can be advantageous to learn all tasks simultaneously instead of following the more traditional approach of learning each task independently of the others. There has been a lot of experimental work showing the benefits of such multi-task learning relative to individual task learning when tasks are related, see [1, 2]. Multi-task learning is a very interesting field, which has been used in many fields of pattern recognition in recent years. With multi-task learning, we can utilize the correlation information of several related tasks to learn a few tasks. By this way, we can improve the efficiency of learning tasks, and prompt the recognition rate under condition of SSS issues [3,4,5]. Multi-task learning was proposed by Caruana in 1997, a multi-task learning mechanism [6, 7], which train a single multi-layer perceptron to perform multi-task. Ghosn and Bengio [8] proposed a idea based on manifold learning. On the other hand, Silver etc [9, 10] also puts forward a kind of multi-task study, which is given continuously. The challenge of this method probably appears interference of disaster or be forgotten. Argyriou [11] etc proposed a technique for dimension reduction, trying to find a representation in all the tasks of the low dimensional feature space. Jebara [12] proposed an idea, which utilizes the choice of kernel function and feature with support vector machine (SVM) to solve the problem of multi-task learning. Obozinski [13] etc researched the same problem with Argyriou in the view of feature selection.

We propose a new approach to extract features from

images with multi-task based on orthogonal projection transformation, which extracts orthogonal feature vectors with related information among several datasets.

## II. ORTHOGONAL PROJECTION TRANSFORMATION OF MULTI-TASK LEARNING TECHNOLOGY

### A. Supervised feature extraction method based on orthogonal projection transformation

Assume that there are three data set A, B, C, and they are related. Based on the Fisher criterion, we firstly calculate the discriminant transformation  $W_A$  on set A through (1)

$$\max_{W_A} J(W_A) = \frac{|W_A^T S_{bA} W_A|}{|W_A^T S_{wA} W_A|} \quad (1)$$

That is to say, we get  $W_A$  through (2)

$$P_A W_A = \lambda W_A, P_A = S_{wA}^{-1} S_{bA} \quad (2)$$

In order to eliminate data the correlation of discriminant transformation between dataset A and B. We set  $W_B^T W_A = 0$

$$\max_{W_B} J(W_B) = \frac{|W_B^T S_{bB} W_B|}{|W_B^T S_{wB} W_B|}, \quad (3)$$

$$s.t. W_B^T W_A = 0$$

According to a general theorem [14], we establish the following objective function:

**Theorem 1:**

$$\max_{W_2} J(W_2) = \frac{|W_2^T S_b W_2|}{|W_2^T S_w W_2|}, \quad (4)$$

$$s.t. W_2^T W_1 = 0$$

We get  $W_A$  through (5)

$$P W_2 = \lambda W_2, \quad (5)$$

$$P = S_w^{-1} \left( I - W_1 (W_1^T S_w^{-1} W_1)^{-1} W_1^T S_w^{-1} \right) S_b,$$

Where  $I$  is a unit matrix, and  $W_2$  is a matrix that consists of  $d$  eigenvectors corresponding to  $d$  different nonzero eigenvalues of  $P$ .

**Proof:** we construct following Lagrange function

$$L(W_2) = W_2^T S_b W_2 - \lambda (W_2^T S_w W_2 - C_1) - \mu (W_2^T W_1 - C_2), \quad (6)$$

where  $\lambda$  and  $\mu$  are the Lagrange multipliers, and  $C_1$  and  $C_2$  are two constant matrices.

We set the derivative of  $L(W_2)$  in (6) on  $W_2$  to be zero:

$$\frac{\partial L(W_2)}{\partial W_2} = 2S_b W_2 - 2\lambda S_w W_2 - \mu W_1 = 0. \quad (7)$$

Multiplying (7) by  $W_1^T S_w^{-1}$ , we have

$$2W_1^T S_w^{-1} S_b W_2 - \mu W_1^T S_w^{-1} W_1 = 0. \quad (8)$$

Thus  $\mu$  may be expressed as

$$\mu = 2(W_1^T S_w^{-1} W_1)^{-1} W_1^T S_w^{-1} S_b W_2. \quad (9)$$

Due to (7) and (9), we have

$$S_b W_2 - \lambda S_w W_2 - W_1 (W_1^T S_w^{-1} W_1)^{-1} W_1^T S_w^{-1} S_b W_2 = 0, \quad (10)$$

That is to say

$$S_w^{-1} (I - W_1 (W_1^T S_w^{-1} W_1)^{-1} W_1^T S_w^{-1}) S_b W_2 = \lambda W_2, \quad (11)$$

Similarly, we get  $W_B$  on dataset B through (12)

$$P_B W_B = \lambda W_B, \quad (12)$$

$$P_B = S_w^{-1} (I - W_A (W_A^T S_w^{-1} W_A)^{-1} W_A^T S_w^{-1}) S_{bB},$$

In order to eliminate correlation of discriminant transform between data set C and data set A, and between data set C and data set B. we construct the objective function and constraint:

$$\max_{W_C} J(W_C) = \frac{|W_C^T S_{bC} W_C|}{|W_C^T S_{wC} W_C|}, \quad (13)$$

$$s.t. \quad W_C^T W_A = 0, W_C^T W_B = 0$$

$W = [W_A, W_B], W_C, S_{bC}, S_{wC}$  replace  $W_1, W_2, S_b, S_w$  respectively, (4) convert into(13).

Similarly, we get  $W_C$  through (14):

$$P_C W_C = \lambda W_C, \quad (14)$$

$$P_C = S_w^{-1} (I - W (W^T S_w^{-1} W)^{-1} W^T S_w^{-1}) S_{bC},$$

Where  $W = [W_A, W_B]$ .

### B. Unsupervised feature extraction method based on orthogonal projection transformation

Based on the Local projection preserve criterion, we firstly calculate the discriminant transformation  $W_A$  in set A through (15).

$$\min_w w^T X_A L X_A^T w \quad (15)$$

$$s.t. \quad w^T X_A D X_A^T w = 1$$

Where  $X_A = [x_{A1}, x_{A2}, \dots, x_{AN}]$  is training samples of data set A,  $D$  is a diagonal matrix,  $D_{ii} = \sum_j S_{ji}$ ,  $S$  is a similarity matrix,  $L = D - S$ . Thus, we get discriminant transformation  $W_A$  through (16)

$$X_A L_A X_A^T W_A = \lambda X_A D_A X_A^T W_A \quad (16)$$

Where  $W_A$  is a matrix that consists of  $d_A$  eigenvectors corresponding to  $d_A$  different nonzero eigenvalues of  $(X_A D_A X_A^T)^{-1} X_A L_A X_A^T$ .

In order to eliminate data the correlation of discriminant transform between set A and B data set. We set  $W_B^T W_A = 0$ , where  $W_B$  is discriminant transform through the Local projection preserve criterion in data set A, so we construct following objective function and constraint:

$$\max_{W_B} J(W_B) = \frac{|W_B^T X_B L_B X_B^T W_B|}{|W_B^T X_B D_B X_B^T W_B|}, \quad (17)$$

$$s.t. \quad W_B^T W_A = 0$$

Where  $X_B = [x_{B1}, x_{B2}, \dots, x_{BN}]$  is training samples of data set B,  $D_B$  is a diagonal matrix,  $D_{ii} = \sum_j S_{ji}$ ,  $S$  is a similarity matrix,  $L = D - S$ , it is a Laplacian Matrix.

**Theorem 2:**

$$\max_{W_2} J(W_2) = \frac{|W_2^T X_2 L_2 X_2^T W_2|}{|W_2^T X_2 D_2 X_2^T W_2|}, \quad (18)$$

$$s.t. \quad W_2^T W_1 = 0$$

Where  $W_1, X_2, L_2$  and  $D_2$  are known matrices. We get  $W_A$  through (19)

$$P W_2 = \lambda W_2, \quad (19)$$

$$P = (X_2 D_2 X_2^T)^{-1} * (I - W_1 (W_1^T (X_2 D_2 X_2^T)^{-1} W_1)^{-1} W_1^T (X_2 D_2 X_2^T)^{-1}) * X_2 L_2 X_2^T,$$

Where  $I$  is a unit matrix.  $W_2$  is a matrix that consists of  $d$  eigenvectors corresponding to  $d$  different nonzero eigenvalues of  $P$ .

**Proof:** we construct following Lagrange function:

$$L(W_2) = W_2^T X_2 L_2 X_2^T W_2 - \quad (20)$$

$$\lambda (W_2^T X_2 D_2 X_2^T W_2 - C_1) - \mu (W_2^T W_1 - C_2),$$

where  $\lambda$  and  $\mu$  are the Lagrange multipliers, and  $C_1$  and  $C_2$  are two constant matrices.

We set the derivative of  $L(W_2)$  in (20) on  $W_2$  to be zero:

$$\frac{\partial L(W_2)}{\partial W_2} = 2 X_2 L_2 X_2^T W_2 - \quad (21)$$

$$2 \lambda X_2 D_2 X_2^T W_2 - \mu W_1 = 0.$$

Multiplying (21) by  $W_1^T (X_2 D_2 X_2^T)^{-1}$ , we have

$$2W_1^T (X_2 D_2 X_2^T)^{-1} X_2 L_2 X_2^T W_2 - \quad (22)$$

$$\mu W_1^T (X_2 D_2 X_2^T)^{-1} W_1 = 0.$$

Thus  $\mu$  may be expressed as

$$\mu = 2 \left( W_1^T (X_2 D_2 X_2^T)^{-1} W_1 \right)^{-1} W_1^T (X_2 D_2 X_2^T)^{-1} X_2 L_2 X_2^T W_2. \quad (23)$$

Due to (21) and (23), we have

$$\begin{aligned} & X_2 L_2 X_2^T W_2 - \lambda X_2 D_2 X_2^T W_2 - \\ & W_1 \left( W_1^T (X_2 D_2 X_2^T)^{-1} W_1 \right)^{-1} W_1^T (X_2 D_2 X_2^T)^{-1} X_2 L_2 X_2^T W_2 = 0, \end{aligned} \quad (24)$$

That is to say

$$(X_2 D_2 X_2^T)^{-1} \left( I - W_1 \left( W_1^T (X_2 D_2 X_2^T)^{-1} W_1 \right)^{-1} W_1^T (X_2 D_2 X_2^T)^{-1} \right) \quad (25)$$

$$X_2 L_2 X_2^T W_2 = \lambda W_2,$$

where  $I$  is a unit matrix. (25) is equivalent to (19).

$W_A, W_B, X_B L_B X_B^T, X_B D_B X_B^T$  replace  $W_1, W_2, X_2 L_2 X_2^T, X_2 D_2 X_2^T$  respectively. (18) is converted into (17).

Similarly, we get  $W_B$  through (26):

$$\begin{aligned} & P_B W_B = \lambda W_B, \\ & P_B = (X_B D_B X_B^T)^{-1} \\ & * \left( I - W_A \left( W_A^T (X_B D_B X_B^T)^{-1} W_A \right)^{-1} W_A^T (X_B D_B X_B^T)^{-1} \right) \\ & * X_B L_B X_B^T, \end{aligned} \quad (26)$$

In order to eliminate correlation of discriminant transform between data set C and data set A, and between data set C and data set B, we construct the objective function and constraint:

$$\max_{W_C} J(W_C) = \frac{W_C^T X_C L_C X_C^T W_C}{W_C^T X_C D_C X_C^T W_C}, \quad (27)$$

$$s.t. \quad W_C^T W_A = 0, W_C^T W_B = 0$$

$X_C = [x_{C1}, x_{C2}, \dots, x_{CN}]$  is training samples of dataset C,  $W = [W_A, W_B], W_C, X_C L_C X_C^T, X_C D_C X_C^T$  replace  $W_1, W_2, X_2 L_2 X_2^T, X_2 D_2 X_2^T$  respectively. (28) is converted into (27).

Similarly, we get  $W_B$  through (28):

$$\begin{aligned} & P_C W_C = \lambda W_C, \\ & P_C = (X_C D_C X_C^T)^{-1} \\ & * \left( I - W \left( W^T (X_C D_C X_C^T)^{-1} W \right)^{-1} W^T (X_C D_C X_C^T)^{-1} \right) \\ & * X_C L_C X_C^T, \end{aligned} \quad (28)$$

where  $W = [W_A, W_B], I$  is a unit matrix.  $W_C$  is a matrix that consists of  $d_c$  eigenvectors corresponding to  $d_c$  different nonzero eigenvalues of  $P$ .

### C. Algorithm description

The brief of our approach is given as follows:

Step 1: Calculate  $W_A, W_B, W_C$  by using (2), (12), (14) on

training set A, B and C, respectively.

Step 2: Project all samples on  $W_A' = [W_A; W_B; W_C]$ , then classify the test sample with the nearest neighbor classifier.

Step 3: Calculate  $W_B, W_C$  in the same way, then classify the test sample with the cosine distance classifier.

## III. EXPERIMENTS

Our experiments are carried out on the AR, FERET and CAS-PEAL face database.

The AR face database contains over 4000 color face images of 126 people (70 men and 56 women), including frontal views of faces with different facial expressions, under different lighting conditions and with various occlusions. Most of the pictures were taken in two sessions (separated by two weeks). Each session yielded 13 color images, with 119 individuals (65 men and 54 women) participating in each session. We selected images from 119 individuals for use in our experiment for a total number of 3094 ( $=119 \times 26$ ) samples. All color images are transformed into gray images and each image was scaled to  $60 \times 60$  with 256 gray levels. Fig. 1 illustrates all of the samples of one subject.

The FERET face database contains 2200 face images belonging to 200 persons, and there are 11 images corresponding to each person. Each image is  $384 \times 256$  with 256 gray levels. Considering many images in this database include the background and the body chest region, we automatically cropped every image sample. We scaled the intercepted images to  $60 \times 48$ . Fig. 2 shows 11 images of an individual of the FERET face database.

The CAS-PEAL face database we employed contains 1060 images of 106 individuals (10 images each person) with varying lighting. A frontal image of each subject was captured under variable illumination. In the experiment, each image was automatically cropped and scaled to  $60 \times 48$ . Fig. 3 shows 10 images of an individual of the CAS-PEAL face database.

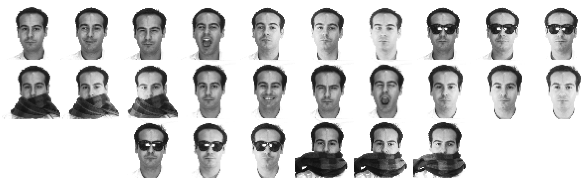


Figure 1. Demo images of one subject from the AR face database.



Figure 2. Demo images of one subject from the FERET face database.

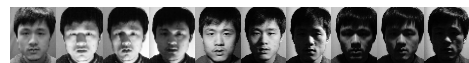


Figure 3. Demo images of one subject from the CAS-PEAL face database.

We scaled the intercepted images to 60× 48 on three face data set. Our supervised and unsupervised approach are carried out on the AR, FERET and CAS-PEAL face database and the training samples range from 2 to 6. Experimental results on these three public face databases demonstrate that the proposed approach acquires higher recognition rates when comes to small sample size.

From Table1 and Table2, we can see that the training samples range from 2 to 6, and the recognition rate of every training sample of our approach high than that of LDA on three face dataset. Our approach improves recognition rate when the number of labeled training samples is very small.

TABLE I. RECOGNITION RATES(%) OF LDA AND OUR APPROACH ON THREE DATASET

		Number of training samples				
		2	3	4	5	6
AR	LDA	68.00	68.32	69.52	70.43	77.69
	Our Approach	69.22	73.62	74.03	76.71	82.52
FERET	LDA	42.33	48.88	51.50	61.50	54.40
	Our Approach	47.83	57.19	64.00	81.75	75.60
CAS-PEAL	LDA	75.00	88.68	91.20	91.89	92.45
	Our Approach	75.23	89.26	92.04	92.16	92.75

TABLE II. RECOGNITION RATES(%) OF LPP AND OUR APPROACH ON THREE DATASET

		Number of training samples				
		2	3	4	5	6
AR	LDA	66.11	67.81	68.83	69.03	75.13
	Our Approach	69.96	71.79	73.53	74.47	79.87
FERET	LDA	29.44	34.16	35.93	38.67	33.80
	Our Approach	48.33	55.50	59.79	77.17	71.90
CAS-PEAL	LDA	61.67	59.16	63.68	75.47	74.06
	Our Approach	63.44	65.90	77.67	78.87	84.91

IV. CONCLUSIONS

The experiments demonstrate our proposed image feature extraction method based on orthogonal projection transformation of multi-task learning technology improves the recognition rate relative to LDA and LPP. When the number of labeled training samples is very small, the sample information we can use would be very little and the recognition rates of traditional image recognition methods are not satisfactory. Our approach apply the useful information contained in other databases to help extract the features more effectively and improve the recognition rates.

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